

# **Recommendation Algorithms**

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# Overview

- ❖ TF-IDF
- ❖ Vector Space Model
- ❖ Latent Semantic Analysis
- ❖ PageRank
- ❖ Collaborative Filtering



Google collaborative filtering

Web Images Maps Shopping Patents More Search tools

About 1,570,000 results (0.27 seconds)

**Collaborative filtering** - Wikipedia, the free encyclopedia **more relevant**  
[en.wikipedia.org/wiki/Collaborative\\_filtering](http://en.wikipedia.org/wiki/Collaborative_filtering) ▼  
Collaborative filtering (CF) is a technique used by some recommender systems. Collaborative filtering has two senses, a narrow one and a more general one.  
Introduction - Methodology - Types - Application on social web

**Amazon.com recommendations item-to-item collaborative filtering ...**  
[ieeexplore.ieee.org/iel5/4236/26323/01167344.pdf](http://ieeexplore.ieee.org/iel5/4236/26323/01167344.pdf)  
by G Linden - 2003 - Cited by 2167 - Related articles  
Item-to-Item Collaborative Filtering. Recommendation algorithms are best known for their use on e-commerce Web sites, where they use input about a cus-.

**[PPT] Collaborative Filtering: A Tutorial - Carnegie Mellon University**  
[www.cs.cmu.edu/~wcohen/collab-filtering-tutorial.ppt](http://www.cs.cmu.edu/~wcohen/collab-filtering-tutorial.ppt) ▼  
Collaborative Filtering: A Tutorial. William W. Cohen. Center for Automated Learning and Discovery. Carnegie Mellon University. Everyday Examples of ...

**[PDF] Collaborative Filtering with Temporal Dynamics**  
[sydney.edu.au/engineering/it/~josiah/lemma/kdd-fp074-koren.pdf](http://sydney.edu.au/engineering/it/~josiah/lemma/kdd-fp074-koren.pdf) ▼  
by Y Koren - 2009 - Cited by 411 - Related articles  
Jun 28, 2009 - Accordingly, we revamp two leading collaborative filtering ... Algorithms. Keywords collaborative filtering, recommender systems, concept drift.





















**[PDF] Learning Collaborative Filtering and Its Application to People to ...**  
[www.cse.unsw.edu.au/~wobcke/papers/learning-to-rank.pdf](http://www.cse.unsw.edu.au/~wobcke/papers/learning-to-rank.pdf) ▼  
by X Cai - Cited by 12 - Related articles  
of items or people becomes essential. Approaches to recommender systems can be categorised as content-based or collaborative filtering (CF) methods.

**GraphLab - Collaborative filtering** **less relevant**  
[graphlab.org/toolkits/collaborative-filtering/](http://graphlab.org/toolkits/collaborative-filtering/) ▼  
The collaborative filtering toolkit provides tools to identify patterns of user interests and make targeted recommendations. Most of the algorithms take the rating ...





# Information Overload

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| <br><b>¥1099.00</b><br>华为 (Mate 9) 32G 32G 铂钻黑 移动联通电信4G手机, 双卡双待<br>已售23724件         | <br><b>¥5688.00</b><br>Apple iPhone 6s (A1700) 64G 玫瑰金 移动联通电信4G手机<br>已售421091件        | <br><b>¥1199.00</b><br>华为 畅享35 移动联通电信4G手机, 双卡双待<br>已售25890件                     | <br><b>¥1099.00</b><br>小米 (Mi) 小米4c 5.5英寸 32G 铂钻黑 移动联通电信4G手机, 双卡双待<br>已售22320件  | <br><b>¥1499.00</b><br>小米 Note 2 移动联通电信4G手机, 双卡双待<br>已售112274件                   |
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**Today a person is subjected to more new information in a day than a person in the middle ages in his entire life!**

# Recommendation Systems

- ❖ A system that predicts a user's rating or preference to an item.
  - Help people **discover** interesting or informative stuff that they **wouldn't** have thought to **search** for.
  - One of the most influential applications of data mining.
- ❖ Content-Based Filtering
  - Focuses on the characteristics of items.
  - Recommends items similar to those that a user liked in the past.
- ❖ Collaborative Filtering
  - Predicts what users will like based on their similarity to other users.
  - Similar to asking the opinions of friends.
  - Does not rely on machine analysable contents.

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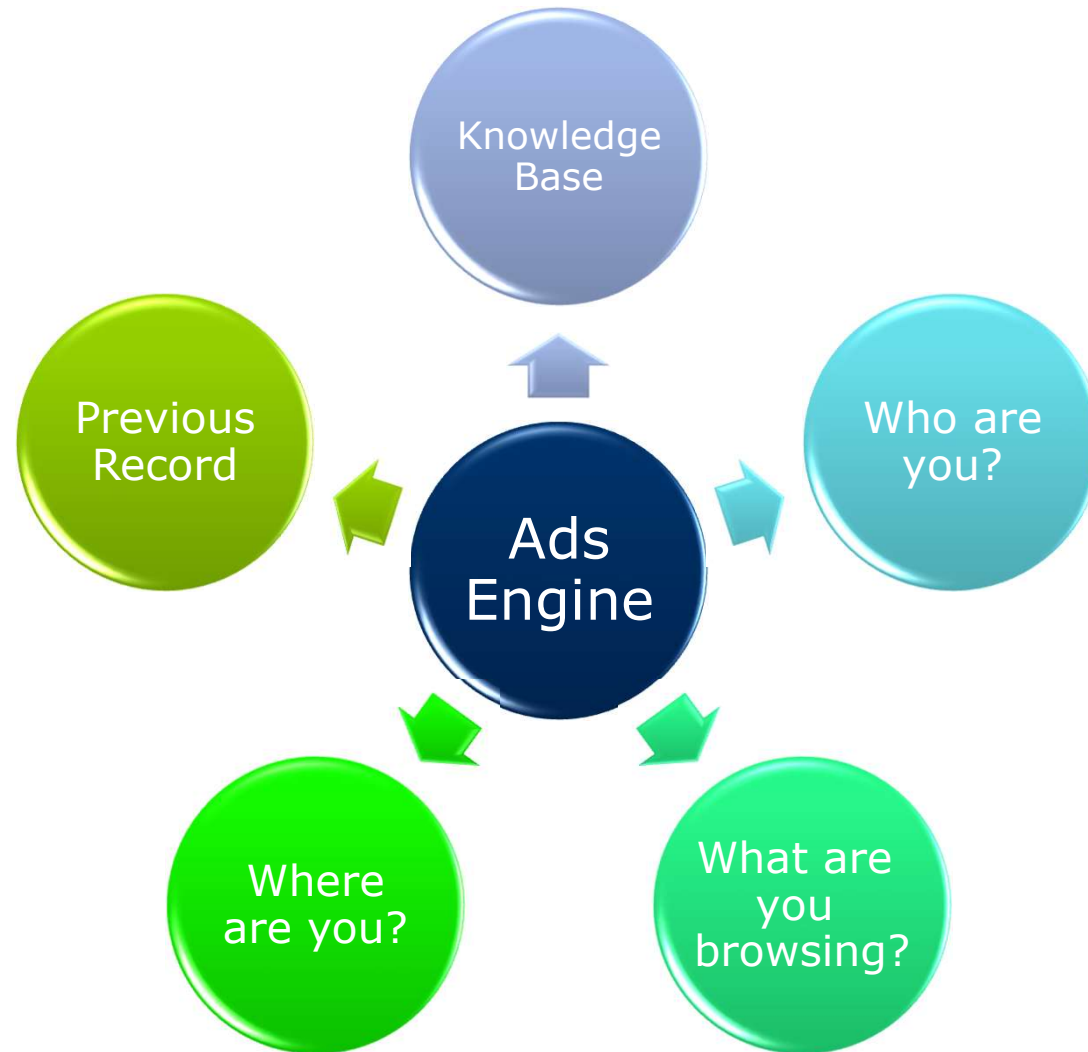
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Google<sup>™</sup>  
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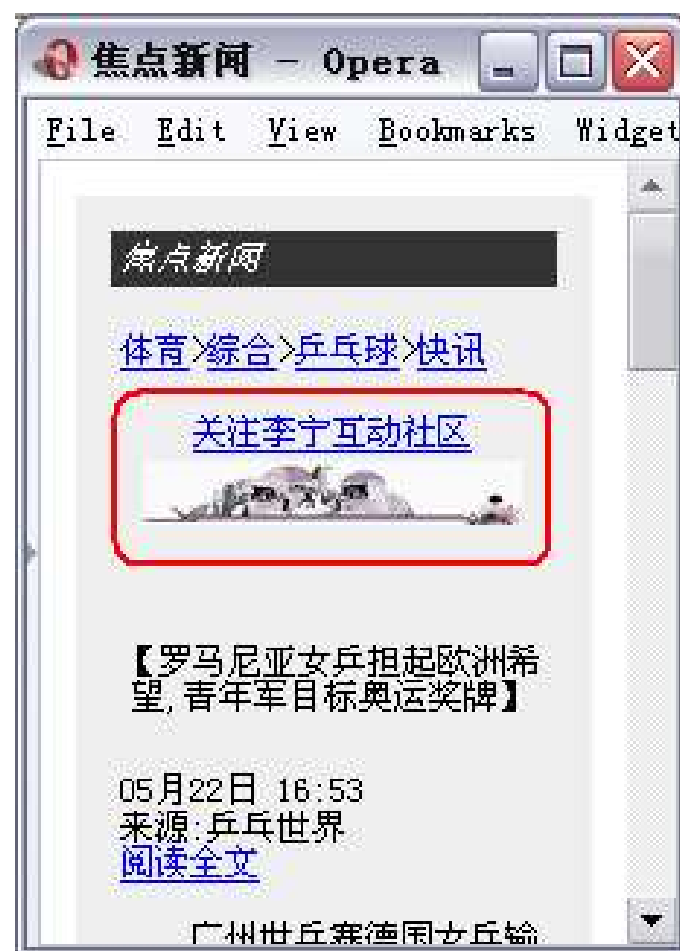
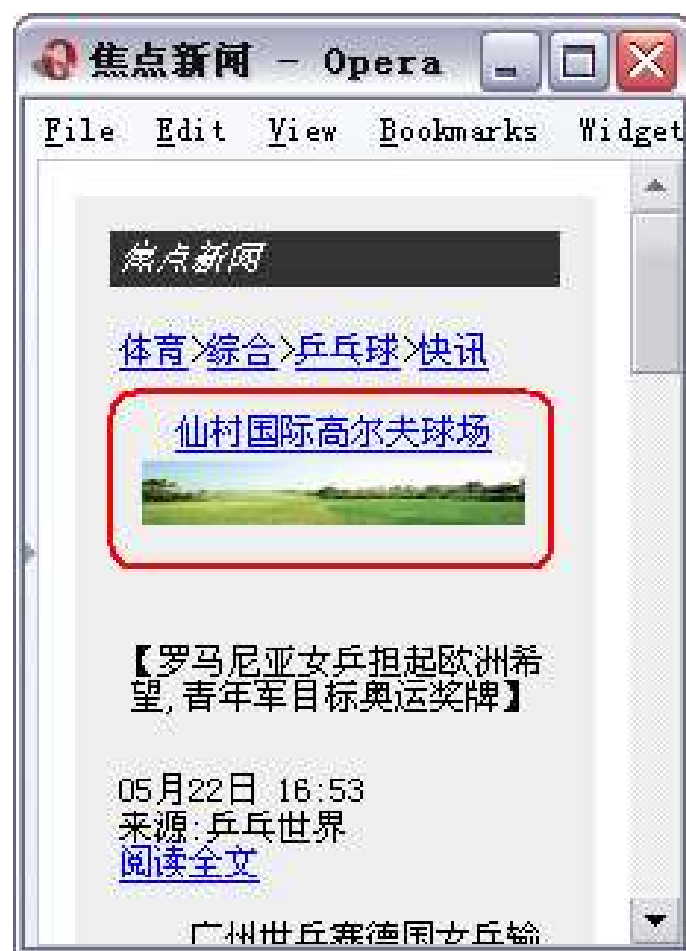
admob<sup>((((( )))</sup>

adshandy<sup>™</sup>

有米广告

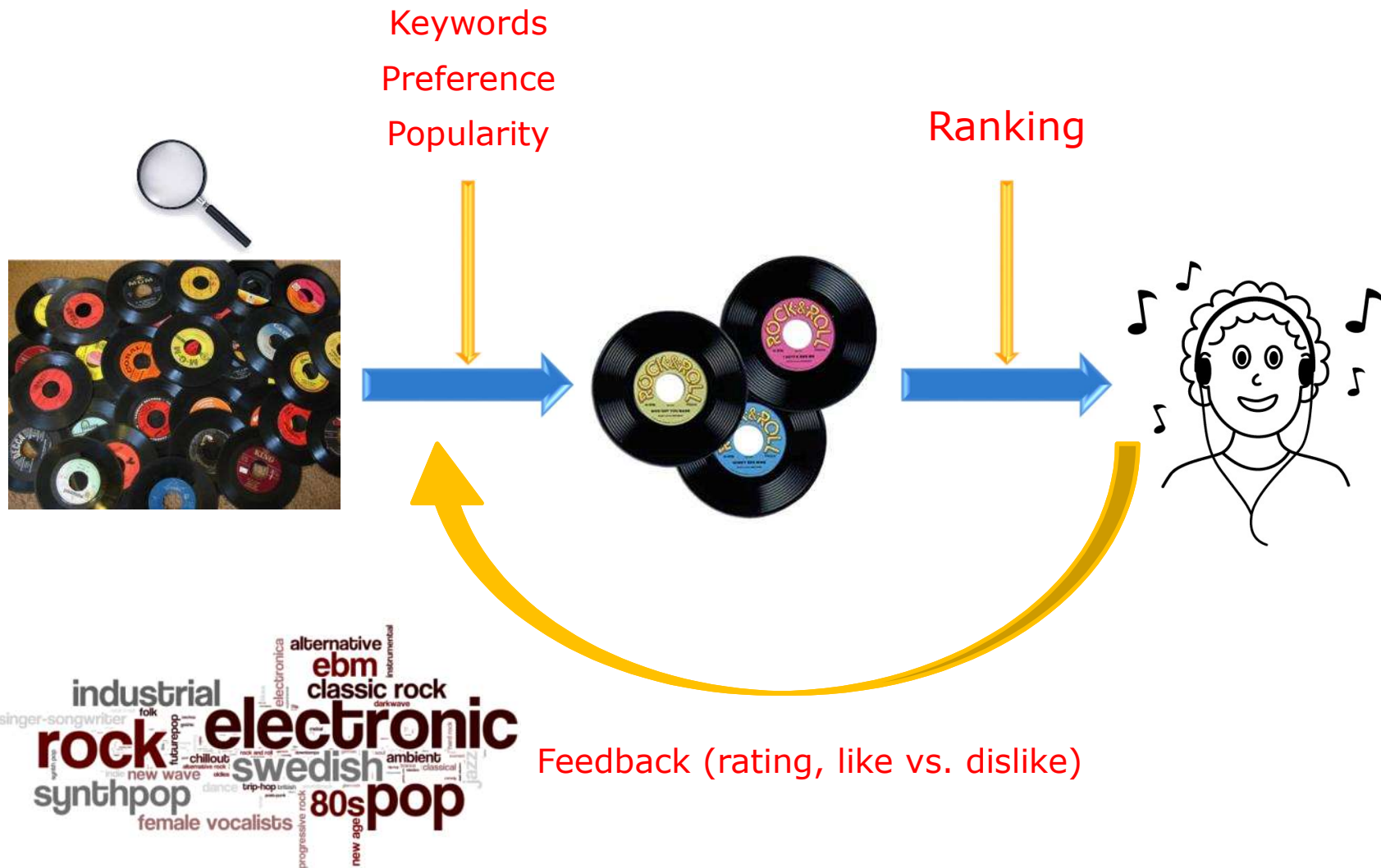


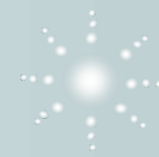
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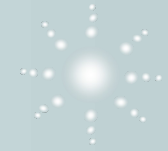


# Music Recommendation





- [illegible]



## ❖ Multiple query words

$$Score(q, d) = \sum_{t \in q} tf - idf(t, d, D)$$

|      | Doc 1 | Doc 2 | Doc 3 | Doc 4 |
|------|-------|-------|-------|-------|
| the  | 20    | 10    | 15    | 8     |
| best | 0     | 1     | 0     | 2     |
| car  | 3     | 5     | 0     | 0     |

Term-Document Matrix



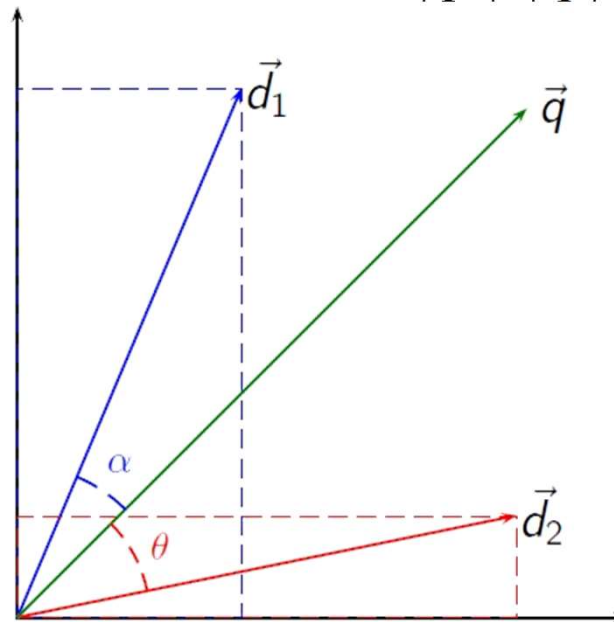
# Vector Space Model

- ❖ An algebraic model for representing text documents as vectors.

$$p = (w_{1,p}, w_{2,p}, \dots, w_{t,p})$$

- ❖ Cosine Similarity

$$\text{sim}(p, q) = \cos(\theta) = \frac{p \cdot q}{|p| \cdot |q|}$$



# Vector Space Model

## ❖ Synonymy

- Different words, same meaning
- Car, Vehicle, Automobile
- Small cosine values → unrelated
- Poor recall

## ❖ Polysemy

- One word, different meanings
- Apple Computer vs. Apple Juice
- Large cosine values → related
- Poor precision



## ❖ Let's work in a more informative space.

- Merge dimensions with similar meanings.
- Singular Value Decomposition

# Latent Semantic Analysis

$$X = TSD^T$$

$$X : m \times n; T : m \times r; S : r \times r; D : n \times r; r = \text{rank}(X)$$

$$XX^T = (TSD^T)(TSD^T)^T = T(SS^T)T^T,$$

$T$  is the eigenvectors of  $XX^T$  (dot products of terms)

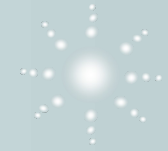
Rows of  $TS$ : Coordinates of terms

$$X^T X = (TSD^T)^T (TSD^T) = D(S^T S)D^T,$$

$D$  is the eigenvectors of  $X^T X$  (dot products of documents)

Rows of  $DS$ : Coordinates of documents

# Latent Semantic Analysis



## Technical Memo Example

### Titles:

- c1: *Human machine interface for Lab ABC computer applications*
- c2: *A survey of user opinion of computer system response time*
- c3: *The EPS user interface management system*
- c4: *System and human system engineering testing of EPS*
- c5: *Relation of user-perceived response time to error measurement*
  
- m1: *The generation of random, binary, unordered trees*
- m2: *The intersection graph of paths in trees*
- m3: *Graph minors IV: Widths of trees and well-quasi-ordering*
- m4: *Graph minors: A survey*

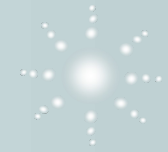


# Original Matrix



| Terms            | Documents |    |    |    |    |    |    |    |    |
|------------------|-----------|----|----|----|----|----|----|----|----|
|                  | c1        | c2 | c3 | c4 | c5 | m1 | m2 | m3 | m4 |
| <i>human</i>     | 1         | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  |
| <i>interface</i> | 1         | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0  |
| <i>computer</i>  | 1         | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| <i>user</i>      | 0         | 1  | 1  | 0  | 1  | 0  | 0  | 0  | 0  |
| <i>system</i>    | 0         | 1  | 1  | 2  | 0  | 0  | 0  | 0  | 0  |
| <i>response</i>  | 0         | 1  | 0  | 0  | 1  | 0  | 0  | 0  | 0  |
| <i>time</i>      | 0         | 1  | 0  | 0  | 1  | 0  | 0  | 0  | 0  |
| <i>EPS</i>       | 0         | 0  | 1  | 1  | 0  | 0  | 0  | 0  | 0  |
| <i>survey</i>    | 0         | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 1  |
| <i>trees</i>     | 0         | 0  | 0  | 0  | 0  | 1  | 1  | 1  | 0  |
| <i>graph</i>     | 0         | 0  | 0  | 0  | 0  | 0  | 1  | 1  | 1  |
| <i>minors</i>    | 0         | 0  | 0  | 0  | 0  | 0  | 0  | 1  | 1  |

# Decomposition



T =

|         |         |         |         |         |         |         |         |         |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| -0.2214 | -0.1132 | 0.2890  | -0.4148 | -0.1063 | -0.3410 | -0.5227 | 0.0605  | 0.4067  |
| -0.1976 | -0.0721 | 0.1350  | -0.5522 | 0.2818  | 0.4959  | 0.0704  | 0.0099  | 0.1089  |
| -0.2405 | 0.0432  | -0.1644 | -0.5950 | -0.1068 | -0.2550 | 0.3022  | -0.0623 | -0.4924 |
| -0.4036 | 0.0571  | -0.3378 | 0.0991  | 0.3317  | 0.3848  | -0.0029 | 0.0004  | -0.0123 |
| -0.6445 | -0.1673 | 0.3611  | 0.3335  | -0.1590 | -0.2065 | 0.1658  | -0.0343 | -0.2707 |
| -0.2650 | 0.1072  | -0.4260 | 0.0738  | 0.0803  | -0.1697 | -0.2829 | 0.0161  | 0.0539  |
| -0.2650 | 0.1072  | -0.4260 | 0.0738  | 0.0803  | -0.1697 | -0.2829 | 0.0161  | 0.0539  |
| -0.3008 | -0.1413 | 0.3303  | 0.1881  | 0.1148  | 0.2722  | -0.0330 | 0.0190  | 0.1653  |
| -0.2059 | 0.2736  | -0.1776 | -0.0324 | -0.5372 | 0.0809  | 0.4669  | 0.0363  | 0.5794  |
| -0.0127 | 0.4902  | 0.2311  | 0.0248  | 0.5942  | -0.3921 | 0.2883  | -0.2546 | 0.2254  |
| -0.0361 | 0.6228  | 0.2231  | 0.0007  | -0.0683 | 0.1149  | -0.1596 | 0.6811  | -0.2320 |
| -0.0318 | 0.4505  | 0.1411  | -0.0087 | -0.3005 | 0.2773  | -0.3395 | -0.6784 | -0.1825 |

S =

|        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 3.3409 | 0      | 0      | 0      | 0      | 0      | 0      | 0      | 0      |
| 0      | 2.5417 | 0      | 0      | 0      | 0      | 0      | 0      | 0      |
| 0      | 0      | 2.3539 | 0      | 0      | 0      | 0      | 0      | 0      |
| 0      | 0      | 0      | 1.6445 | 0      | 0      | 0      | 0      | 0      |
| 0      | 0      | 0      | 0      | 1.5048 | 0      | 0      | 0      | 0      |
| 0      | 0      | 0      | 0      | 0      | 1.3064 | 0      | 0      | 0      |
| 0      | 0      | 0      | 0      | 0      | 0      | 0.8459 | 0      | 0      |
| 0      | 0      | 0      | 0      | 0      | 0      | 0      | 0.5601 | 0      |
| 0      | 0      | 0      | 0      | 0      | 0      | 0      | 0      | 0.3637 |

# Decomposition



D =

|         |         |         |         |         |         |         |         |         |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| -0.1974 | -0.0559 | 0.1103  | -0.9498 | 0.0457  | -0.0766 | -0.1773 | 0.0144  | 0.0637  |
| -0.6060 | 0.1656  | -0.4973 | -0.0286 | -0.2063 | -0.2565 | 0.4330  | -0.0493 | -0.2428 |
| -0.4629 | -0.1273 | 0.2076  | 0.0416  | 0.3783  | 0.7244  | 0.2369  | -0.0088 | -0.0241 |
| -0.5421 | -0.2318 | 0.5699  | 0.2677  | -0.2056 | -0.3689 | -0.2648 | 0.0195  | 0.0842  |
| -0.2795 | 0.1068  | -0.5054 | 0.1500  | 0.3272  | 0.0348  | -0.6723 | 0.0583  | 0.2624  |
| -0.0038 | 0.1928  | 0.0982  | 0.0151  | 0.3948  | -0.3002 | 0.3408  | -0.4545 | 0.6198  |
| -0.0146 | 0.4379  | 0.1930  | 0.0155  | 0.3495  | -0.2122 | 0.1522  | 0.7615  | -0.0180 |
| -0.0241 | 0.6151  | 0.2529  | 0.0102  | 0.1498  | 0.0001  | -0.2491 | -0.4496 | -0.5199 |
| -0.0820 | 0.5299  | 0.0793  | -0.0246 | -0.6020 | 0.3622  | -0.0380 | 0.0696  | 0.4535  |

T\*S\*D'

|         |         |         |         |         |         |         |         |         |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1.0000  | 0.0000  | 0.0000  | 1.0000  | -0.0000 | -0.0000 | -0.0000 | -0.0000 | -0.0000 |
| 1.0000  | 0.0000  | 1.0000  | 0.0000  | 0.0000  | 0.0000  | -0.0000 | -0.0000 | -0.0000 |
| 1.0000  | 1.0000  | 0.0000  | -0.0000 | -0.0000 | 0.0000  | 0.0000  | 0.0000  | 0.0000  |
| -0.0000 | 1.0000  | 1.0000  | 0.0000  | 1.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  |
| -0.0000 | 1.0000  | 1.0000  | 2.0000  | 0.0000  | -0.0000 | -0.0000 | -0.0000 | -0.0000 |
| -0.0000 | 1.0000  | 0.0000  | 0.0000  | 1.0000  | -0.0000 | -0.0000 | 0.0000  | 0.0000  |
| -0.0000 | 1.0000  | 0.0000  | 0.0000  | 1.0000  | -0.0000 | -0.0000 | 0.0000  | 0.0000  |
| -0.0000 | 0.0000  | 1.0000  | 1.0000  | 0.0000  | 0.0000  | 0.0000  | -0.0000 | -0.0000 |
| -0.0000 | 1.0000  | 0.0000  | -0.0000 | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 1.0000  |
| -0.0000 | 0.0000  | -0.0000 | -0.0000 | 0.0000  | 1.0000  | 1.0000  | 1.0000  | 0.0000  |
| -0.0000 | -0.0000 | -0.0000 | -0.0000 | 0.0000  | 0.0000  | 1.0000  | 1.0000  | 1.0000  |
| -0.0000 | 0.0000  | -0.0000 | -0.0000 | 0.0000  | 0.0000  | 0.0000  | 1.0000  | 1.0000  |

# Rank K Approximation



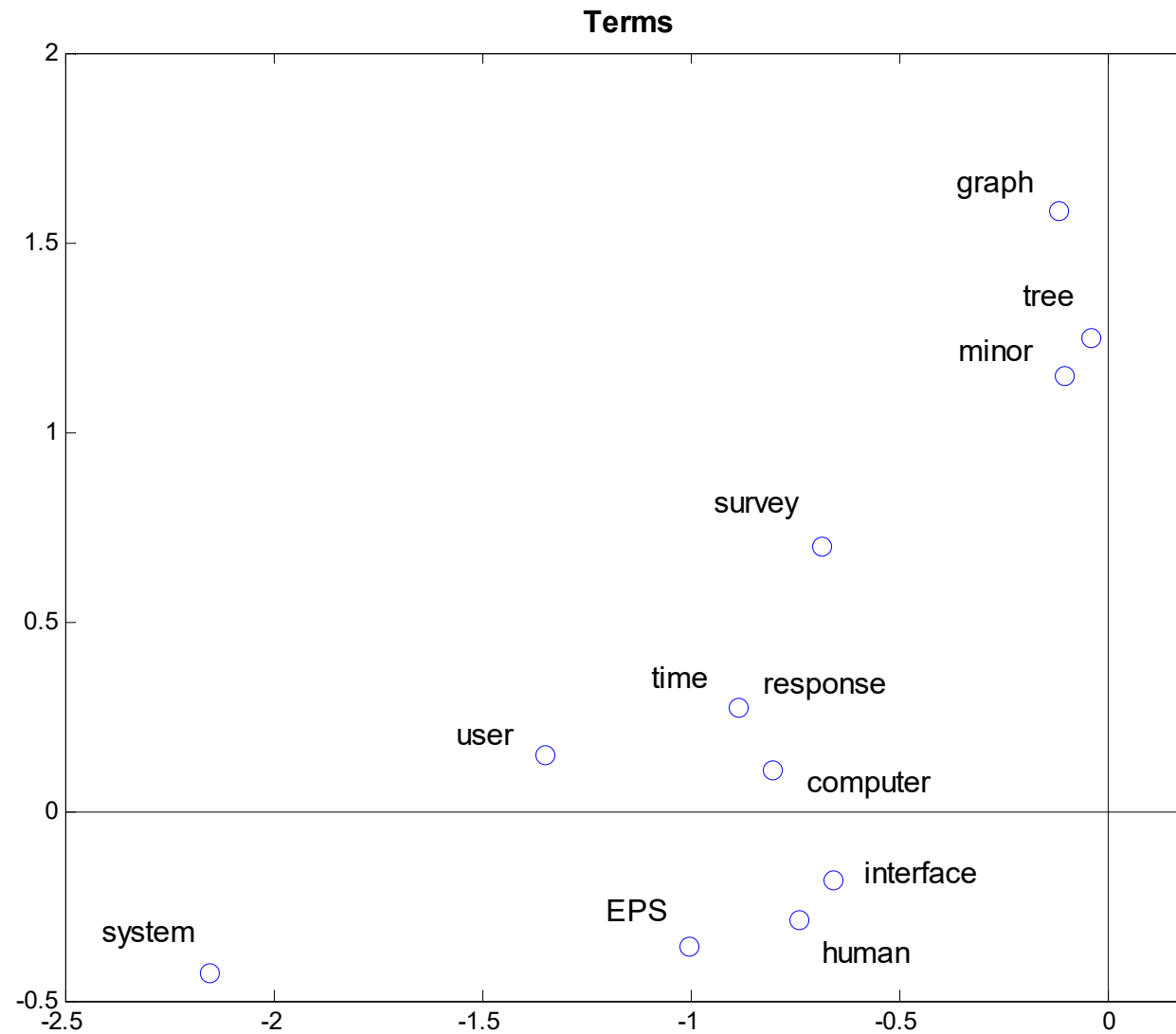
K=2

| T(:, 1:2) |         | S(1:2, 1:2) |        | D(:, 1:2)' |         |         |         |         |         |         |         |         |  |
|-----------|---------|-------------|--------|------------|---------|---------|---------|---------|---------|---------|---------|---------|--|
| -0.2214   | -0.1132 | 3.3409      | 0      | -0.1974    | -0.6060 | -0.4629 | -0.5421 | -0.2795 | -0.0038 | -0.0146 | -0.0241 | -0.0820 |  |
| -0.1976   | -0.0721 | 0           | 2.5417 | -0.0559    | 0.1656  | -0.1273 | -0.2318 | 0.1068  | 0.1928  | 0.4379  | 0.6151  | 0.5299  |  |
| -0.2405   | 0.0432  |             |        |            |         |         |         |         |         |         |         |         |  |
| -0.4036   | 0.0571  |             |        |            |         |         |         |         |         |         |         |         |  |
| -0.6445   | -0.1673 |             |        |            |         |         |         |         |         |         |         |         |  |
| -0.2650   | 0.1072  |             |        |            |         |         |         |         |         |         |         |         |  |
| -0.2650   | 0.1072  |             |        |            |         |         |         |         |         |         |         |         |  |
| -0.3008   | -0.1413 |             |        |            |         |         |         |         |         |         |         |         |  |
| -0.2059   | 0.2736  |             |        |            |         |         |         |         |         |         |         |         |  |
| -0.0127   | 0.4902  | 0.1621      | 0.4005 | 0.3790     | 0.4676  | 0.1760  | -0.0527 | -0.1151 | -0.1591 | -0.0918 |         |         |  |
| -0.0361   | 0.6228  | 0.1406      | 0.3698 | 0.3290     | 0.4004  | 0.1650  | -0.0328 | -0.0706 | -0.0968 | -0.0430 |         |         |  |
| -0.0318   | 0.4505  | 0.1524      | 0.5050 | 0.3579     | 0.4101  | 0.2362  | 0.0242  | 0.0598  | 0.0869  | 0.1240  |         |         |  |
|           |         | 0.2580      | 0.8411 | 0.6057     | 0.6974  | 0.3923  | 0.0331  | 0.0832  | 0.1218  | 0.1874  |         |         |  |
|           |         | 0.4488      | 1.2344 | 1.0509     | 1.2658  | 0.5563  | -0.0738 | -0.1547 | -0.2096 | -0.0489 |         |         |  |
|           |         | 0.1596      | 0.5817 | 0.3752     | 0.4169  | 0.2765  | 0.0559  | 0.1322  | 0.1889  | 0.2169  |         |         |  |
|           |         | 0.1596      | 0.5817 | 0.3752     | 0.4169  | 0.2765  | 0.0559  | 0.1322  | 0.1889  | 0.2169  |         |         |  |
|           |         | 0.2185      | 0.5496 | 0.5110     | 0.6281  | 0.2425  | -0.0654 | -0.1425 | -0.1966 | -0.1079 |         |         |  |
|           |         | 0.0969      | 0.5321 | 0.2299     | 0.2118  | 0.2665  | 0.1368  | 0.3146  | 0.4444  | 0.4250  |         |         |  |
|           |         | -0.0613     | 0.2321 | -0.1389    | -0.2656 | 0.1449  | 0.2404  | 0.5461  | 0.7674  | 0.6637  |         |         |  |
|           |         | -0.0647     | 0.3353 | -0.1456    | -0.3014 | 0.2028  | 0.3057  | 0.6949  | 0.9766  | 0.8487  |         |         |  |
|           |         | -0.0431     | 0.2539 | -0.0967    | -0.2079 | 0.1519  | 0.2212  | 0.5029  | 0.7069  | 0.6155  |         |         |  |

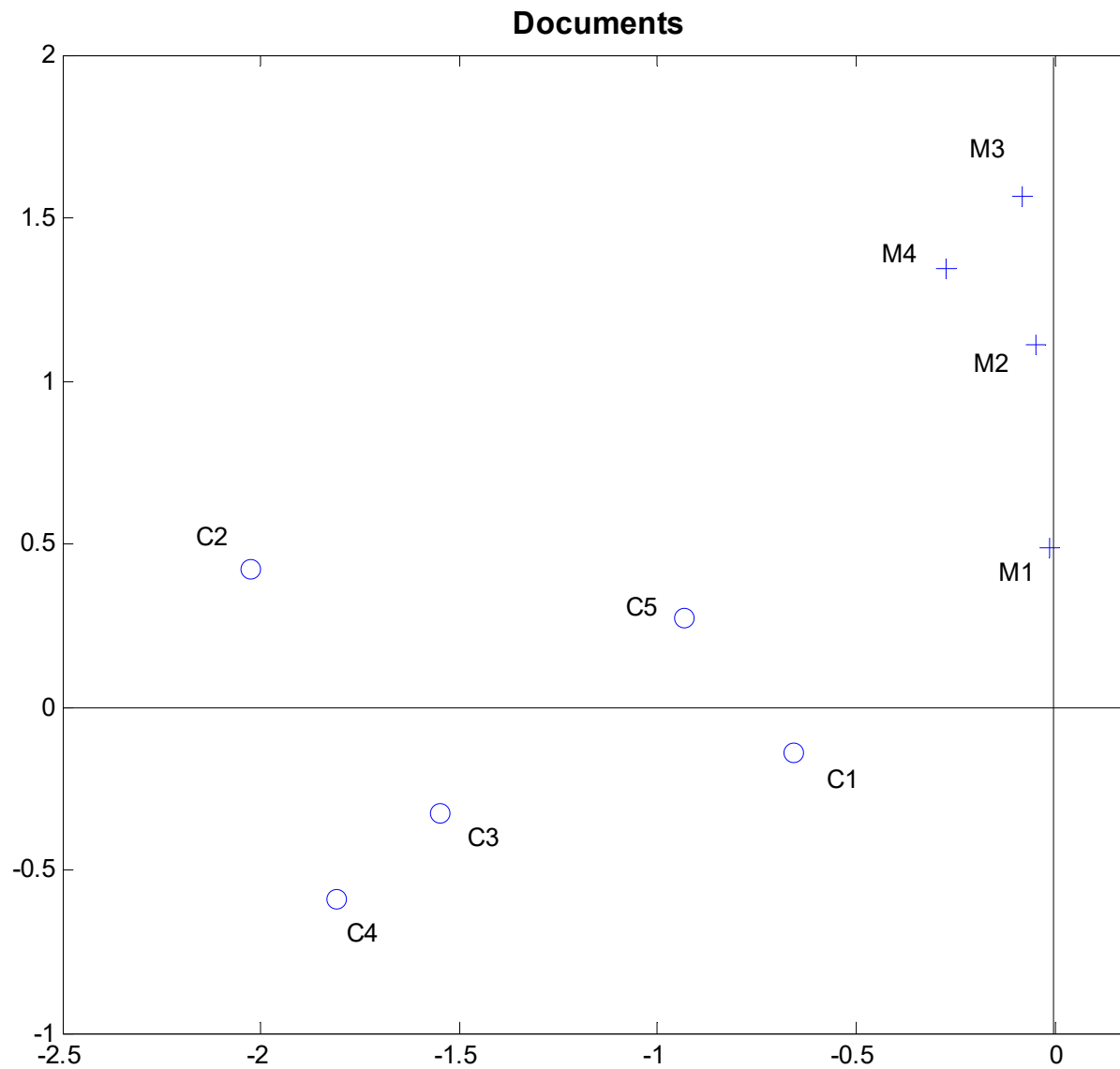
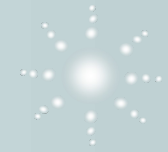
$\hat{X}$



# Items in 2D Space



# Documents in 2D Space



# Document Cosine Similarity



|         |        |         |         |        |         |         |         |         |
|---------|--------|---------|---------|--------|---------|---------|---------|---------|
| 0       | 0.9142 | 1.0000  | 0.9948  | 0.8799 | -0.1852 | -0.1676 | -0.1600 | -0.0117 |
| 0.9142  | 0      | 0.9166  | 0.8681  | 0.9970 | 0.2289  | 0.2463  | 0.2537  | 0.3945  |
| 1.0000  | 0.9166 | 0       | 0.9942  | 0.8827 | -0.1793 | -0.1617 | -0.1541 | -0.0057 |
| 0.9948  | 0.8681 | 0.9942  | 0       | 0.8268 | -0.2845 | -0.2673 | -0.2599 | -0.1137 |
| 0.8799  | 0.9970 | 0.8827  | 0.8268  | 0      | 0.3040  | 0.3210  | 0.3282  | 0.4648  |
| -0.1852 | 0.2289 | -0.1793 | -0.2845 | 0.3040 | 0       | 0.9998  | 0.9997  | 0.9848  |
| -0.1676 | 0.2463 | -0.1617 | -0.2673 | 0.3210 | 0.9998  | 0       | 1.0000  | 0.9878  |
| -0.1600 | 0.2537 | -0.1541 | -0.2599 | 0.3282 | 0.9997  | 1.0000  | 0       | 0.9889  |
| -0.0117 | 0.3945 | -0.0057 | -0.1137 | 0.4648 | 0.9848  | 0.9878  | 0.9889  | 0       |

Transformed

|        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0      | 0.2357 | 0.2887 | 0.2357 | 0      | 0      | 0      | 0      | 0      |
| 0.2357 | 0      | 0.4082 | 0.3333 | 0.7071 | 0      | 0      | 0      | 0.2357 |
| 0.2887 | 0.4082 | 0      | 0.6124 | 0.2887 | 0      | 0      | 0      | 0      |
| 0.2357 | 0.3333 | 0.6124 | 0      | 0      | 0      | 0      | 0      | 0      |
| 0      | 0.7071 | 0.2887 | 0      | 0      | 0      | 0      | 0      | 0      |
| 0      | 0      | 0      | 0      | 0      | 0      | 0.7071 | 0.5774 | 0      |
| 0      | 0      | 0      | 0      | 0      | 0.7071 | 0      | 0.8165 | 0.4082 |
| 0      | 0      | 0      | 0      | 0      | 0.5774 | 0.8165 | 0      | 0.6667 |
| 0      | 0.2357 | 0      | 0      | 0      | 0      | 0.4082 | 0.6667 | 0      |

Original

# Query

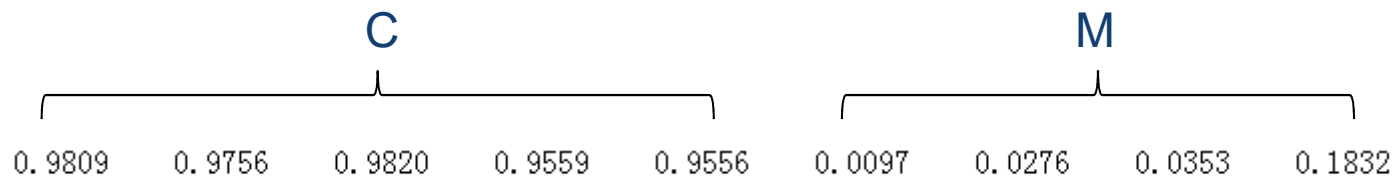


*Query* = "human response"

$$q = [1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0]^T$$

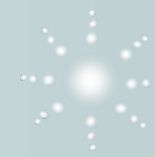
$$\hat{q} = S_k^{-1} T_k^T q = [-0.1456, -0.0024]^T$$

$$\hat{q}^T S = [-0.4864, -0.0060]$$

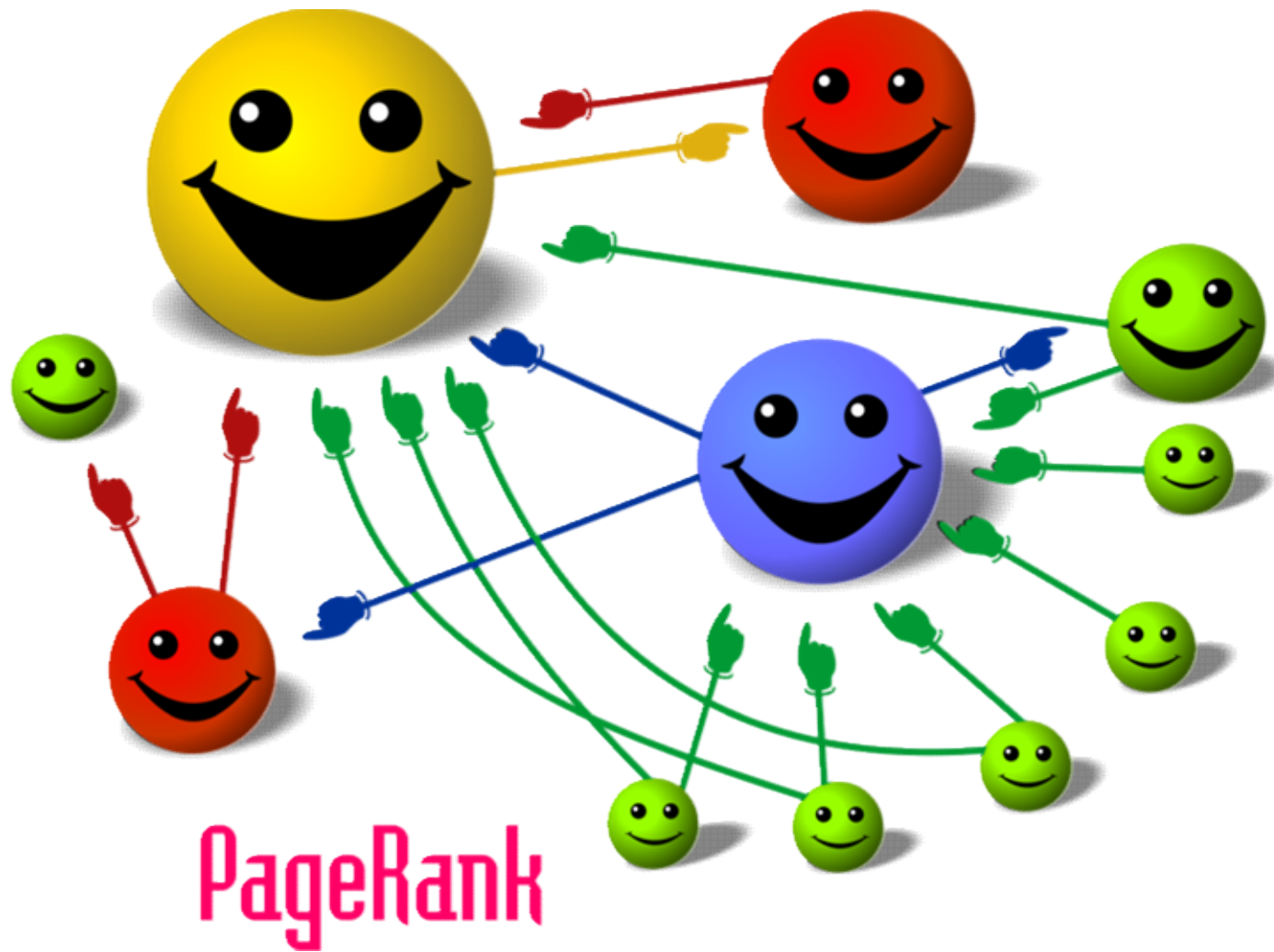


Cosine Similarity to Current Documents

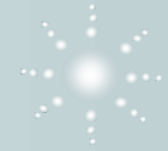




# *Linked Documents*

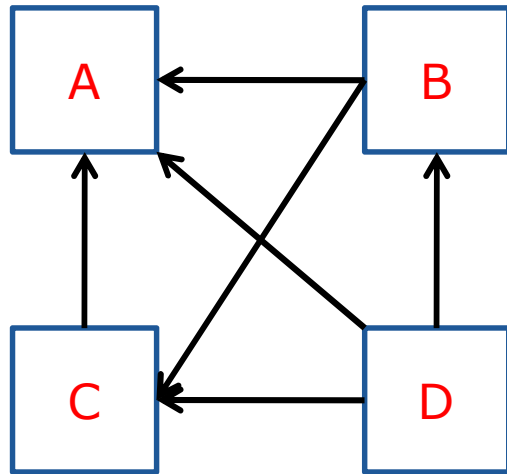


# PageRank



- ❖ Given a set of hyperlinked documents, how to evaluate the relative importance of each document?
- ❖ A hyperlink to a page counts as a vote of support.
  - The importance of vote from a page depends on its own PageRank and the number of outbound links.
- ❖ The PageRank of a page is determined by the number and PageRank metric of all pages that link to it.
- ❖ The outbound links of a page do not affect its PageRank value.
  - Difficult to manipulate inbound links.
- ❖ A key factor determining a page's ranking in the search results of Google.

# PageRank



$$PR(A) = \frac{PR(B)}{2} + \frac{PR(C)}{1} + \frac{PR(D)}{3}$$

$$PR(P_i) = \sum_{p_j \in M(p_i)} \frac{PR(p_j)}{L(p_j)}$$

$$PR(P_i; t + 1) = \frac{1 - d}{N} + d \sum_{p_j \in M(p_i)} \frac{PR(p_j; t)}{L(p_j)}$$

d: damping factor (0.85)

# PageRank

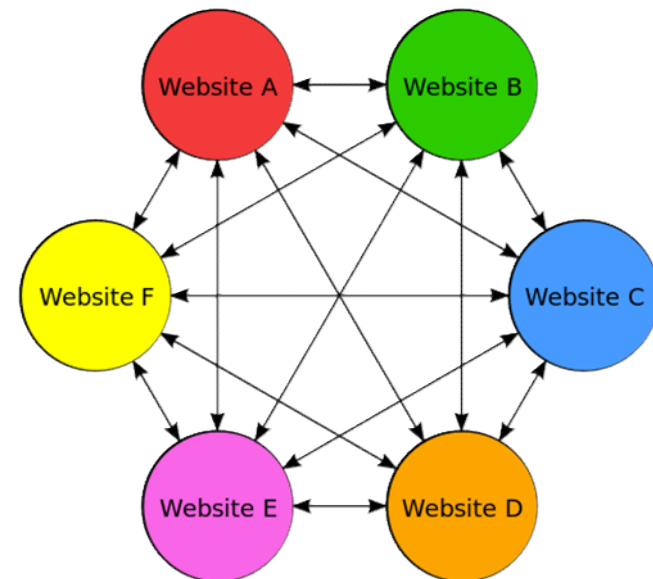
$$R(t+1) = dMR(t) + \frac{1-d}{N}l$$

$$R_i(t) = PR(p_i; t) \quad PR(p_i; 0) = \frac{1}{N} \quad d = 0.85$$

$$M_{ij} = \begin{cases} 1/L(p_j), & \text{if } j \text{ links to } i \\ 0, & \text{otherwise} \end{cases} \quad l = \text{ones}(N, 1)$$

$$R = dMR + \frac{1-d}{N}l, \quad \text{for } t \rightarrow \infty$$

$$R = (I - dM)^{-1} \frac{1-d}{N}l$$



# Monetary Success



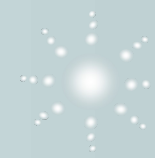
- ❖ Stanford University received 1.8 million shares for allowing Google Inc. to use this technique.
  - Sergey Brin: US\$ 37 billion (2016)
  - Larry Page: US\$ 38 billion (2016)
- ❖ Made totally US\$ 336 million in return by 2005.
  - Within two years after Google's IPO
  - Around US\$ 187 per share
  - How about if the shares are sold today?
- ❖ Current Endowment: US\$ 22 billion
- ❖ One of the largest single academic licensing transactions
  - Cloning Technology: US\$ 225 million in royalties

Google Inc

NASDAQ: GOOG - 27/11 4:00 pm ET

1,063.11 ↑ 4.70 (0.44%)





# Collaborative Filtering

## ❖ Core Idea:

- People get the best recommendation from others with similar tastes.



## ❖ Workflow:

- Creates a rating or purchase matrix.
- Finds similar people by matching their ratings.
- Recommends items that similar people rate highly.

## ❖ Memory-Based CF

- User-Based vs. Item-Based



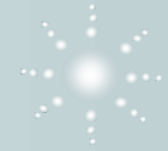
## ❖ Model-Based CF

## ❖ Things to know:

- Gray Sheep
- Shilling Attack
- Cold Start



## User-Based CF

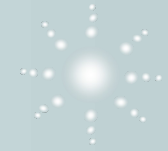


|       | $I_1$ | $I_2$ | $I_3$ | $I_4$ |
|-------|-------|-------|-------|-------|
| $U_1$ | 4     | ?     | 5     | 5     |
| $U_2$ | 4     | 2     | 1     |       |
| $U_3$ | 3     |       | 2     | 4     |
| $U_4$ | 4     | 4     |       |       |
| $U_5$ | 2     | 1     | 3     | 5     |

$$w_{u,v} = \frac{\sum_{i \in I} (r_{u,i} - \bar{r}_u)(r_{v,i} - \bar{r}_v)}{\sqrt{\sum_{i \in I} (r_{u,i} - \bar{r}_u)^2} \sqrt{\sum_{i \in I} (r_{v,i} - \bar{r}_v)^2}}$$

$$P_{a,i} = \bar{r}_a + \frac{\sum_{u \in U} (r_{u,i} - \bar{r}_u) \cdot w_{a,u}}{\sum_{u \in U} |w_{a,u}|}$$

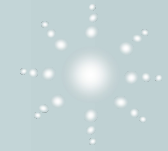
## User-Based CF



|       | $I_1$ | $I_2$ | $I_3$ | $I_4$ |
|-------|-------|-------|-------|-------|
| $U_1$ | 4     | ?     | 5     | 5     |
| $U_2$ | 4     | 2     | 1     |       |
| $U_3$ | 3     |       | 2     | 4     |
| $U_4$ | 4     | 4     |       |       |
| $U_5$ | 2     | 1     | 3     | 5     |

$$\begin{aligned}P_{1,2} &= \bar{r}_1 + \frac{\sum_u (r_{u,2} - \bar{r}_u) \cdot w_{1,u}}{\sum_u |w_{1,u}|} \\&= \bar{r}_1 + \frac{(r_{2,2} - \bar{r}_2)w_{1,2} + (r_{4,2} - \bar{r}_4)w_{1,4} + (r_{5,2} - \bar{r}_5)w_{1,5}}{|w_{1,2}| + |w_{1,4}| + |w_{1,5}|} \\&= 4.67 + \frac{(2 - 2.5)(-1) + (4 - 4)0 + (1 - 3.33)0.756}{1 + 0 + 0.756} \\&= 3.95.\end{aligned}$$

# Item-Based CF



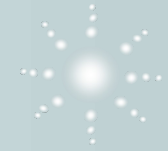
$$w_{i,j} = \frac{\sum_{u \in U} (r_{u,i} - \bar{r}_i)(r_{u,j} - \bar{r}_j)}{\sqrt{\sum_{u \in U} (r_{u,i} - \bar{r}_i)^2} \sqrt{\sum_{u \in U} (r_{u,j} - \bar{r}_j)^2}}$$

**U**: Users that have rated both *i* and *j*.

$$P_{a,i} = \frac{\sum_{j \in I} w_{i,j} \cdot r_{a,j}}{\sum_{j \in I} |w_{i,j}|}$$

**I**: All items that have been rated by User *a*.

# Item-Based CF



$$P_{a,i} = \bar{r}_a + \frac{1}{|U|} \sum_{u \in U} (r_{u,i} - \bar{r}_u)$$

**U**: Users that have rated *i*.

$$dev_{i,j} = \frac{1}{|U|} \sum_{u \in U} (r_{u,i} - r_{u,j})$$

**U**: Users that have rated both *i* and *j*.

$$P_{a,i} = \frac{1}{|I|} \sum_{j \in I} (dev_{i,j} + r_{a,j})$$

**I**: Items that the user has rated and have *dev* values.



# Item-Based CF



| Customer | Item 1         | Item 2 | Item 3         |
|----------|----------------|--------|----------------|
| John     | 5              | 3      | 2              |
| Mark     | 3              | 4      | Didn't rate it |
| Lucy     | Didn't rate it | 2      | 5              |

$$P_{Lucy,1} = \frac{2+5}{2} + \frac{5-2.5+3-4}{2} = 4.25$$

$$dev_{1,2} = \frac{2-1}{2} = 0.5 \quad dev_{1,3} = \frac{3}{1} = 3$$

$$P_{Lucy,1} = \frac{1}{2} (0.5 + 2 + 3 + 5) = 5.25$$

$$P_{Lucy,1} = \frac{2 \times 2.5 + 1 \times 8}{2+1} = 4.33$$

Slope One

# Model-Based CF

Class Label

The diagram illustrates a classification model. A central table has columns labeled  $I_1, I_2, I_3, I_4$  and rows labeled  $U_1, U_2, U_3, U_4, U_5$ . Above the table, the text 'Class Label' has three arrows pointing to the column headers. To the left of the table, the text 'Attributes' has four arrows pointing to the row headers. Below the table, the text 'Training Samples' has three arrows pointing to the column headers. The row for  $U_1$  is highlighted with a red line.

|       | $I_1$ | $I_2$ | $I_3$ | $I_4$ |
|-------|-------|-------|-------|-------|
| $U_1$ | 4     | ?     | 5     | 5     |
| $U_2$ | 4     | 2     | 1     |       |
| $U_3$ | 3     |       | 2     | 4     |
| $U_4$ | 4     | 4     |       |       |
| $U_5$ | 2     | 1     | 3     | 5     |

Training Samples

$$class = \arg \max_{j \in classSet} P(class_j) \prod_o P(X_o = x_o | class_j)$$

# Model-Based CF

|       | $I_1$ | $I_2$ | $I_3$ | $I_4$ |
|-------|-------|-------|-------|-------|
| $U_1$ | 4     | ?     | 5     | 5     |
| $U_2$ | 4     | 2     | 1     |       |
| $U_3$ | 3     |       | 2     | 4     |
| $U_4$ | 4     | 4     |       |       |
| $U_5$ | 2     | 1     | 3     | 5     |

$$class = \arg \max_{c_j \in \{1,2,3,4,5\}} P(c_j)P(U_2 = 2|c_j)P(U_4 = 4|c_j)P(U_5 = 1|c_j)$$

$$= \arg \max_{c_j \in \{1,2,3,4,5\}} \{0, 0, 0, 0.0031, 0.0019\} = 4$$

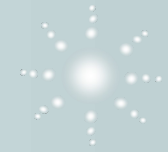
$$P(5)P(U_2 = 2|5)P(U_4 = 4|5)P(U_5 = 1|5)$$

$$= \frac{2}{3} \times \frac{0+1}{2+5} \times \frac{0+1}{2+5} \times \frac{0+1}{2+5} = 0.0019$$

$$P(4)P(U_2 = 2|4)P(U_4 = 4|4)P(U_5 = 1|4)$$

$$= \frac{1}{3} \times \frac{0+1}{1+5} \times \frac{1+1}{1+5} \times \frac{0+1}{1+5} = 0.0031$$

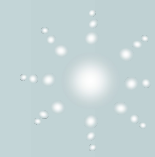
# Model-Based CF



|                | <b>I<sub>1</sub></b> | <b>I<sub>2</sub></b> | <b>I<sub>3</sub></b> | <b>I<sub>4</sub></b> | <b>I<sub>5</sub></b> |
|----------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| U <sub>1</sub> | Like                 | Dislike              | Dislike              |                      | Like                 |
| U <sub>2</sub> | Dislike              |                      |                      | Dislike              | Dislike              |
| U <sub>3</sub> |                      | Like                 | Like                 |                      | Like                 |
| Class Label    | Like                 | Dislike              | Like                 | Like                 | ?                    |



|                        | <b>I<sub>1</sub></b> | <b>I<sub>2</sub></b> | <b>I<sub>3</sub></b> | <b>I<sub>4</sub></b> | <b>I<sub>5</sub></b> |
|------------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| U <sub>1</sub> like    | 1                    | 0                    | 0                    | 0                    | 1                    |
| U <sub>1</sub> dislike | 0                    | 1                    | 1                    | 0                    | 0                    |
| U <sub>2</sub> like    | 0                    | 0                    | 0                    | 0                    | 0                    |
| U <sub>2</sub> dislike | 1                    | 0                    | 0                    | 1                    | 1                    |
| U <sub>3</sub> like    | 0                    | 1                    | 1                    | 0                    | 1                    |
| U <sub>3</sub> dislike | 0                    | 0                    | 0                    | 0                    | 0                    |
| Class Label            | Like                 | Dislike              | Like                 | Like                 | ?                    |



# Netflix Prize

- ❖ A public company providing DVD-rental service
- ❖ Target:
  - To predict whether someone will enjoy a movie based on how much they liked or disliked other movies.
  - To improve the score of its own Cinematch by 10%
  - RMSE (Root Mean Squared Error)
- ❖ Training Set:
  - <user, movie, date of grade, grade>
  - 480,189 users, 17,770 movies, 100,480,507 ratings



| Rank  | Team Name                                 | Best Test Score | <u>%</u><br>Improvement | Best Submit Time    |
|---|---|-----------------|-------------------------|---------------------|
| Grand Prize - RMSE = 0.8567 - Winning Team: BellKor's Pragmatic Chaos |   |                 |                         |                     |
| 1   | <a href="#">BellKor's Pragmatic Chaos</a> | 0.8567          | 10.06                   | 2009-07-26 18:18:28 |
| 2   | <a href="#">The Ensemble</a>              | 0.8567          | 10.06                   | 2009-07-26 18:38:22 |

# KDD Cup



**Jobs You May Be Interested In** *beta*

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买满即送 限时限量 抢到就是赚到!

活动时间: 11月5日-11月8日



13周年  
店庆月  
惹火行动  
第③波

2012.11.5-2012.11.11  
家居爆品 低至 **2折**

最高 满减飓风  
直减 **400元**

家纺 厨具 生活日用 家具装饰 宠物

满149减50  
满300减100  
满600减220  
满1000立减400

13周年  
店庆月  
惹火行动  
第③波

童装童鞋 百家名店

当当价

**5折**

基础上



仅3天

满500送100现金券

## 1元抢大牌

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13周年  
店庆月  
惹火行动  
第③波

11.5-11  
家电品牌旗舰店  
**大牌暴降**

秒杀  
低至 **1元**

**1000元**

周年庆钜惠



2012.11.11

支付宝总交易额

191 亿元

其中 天猫

132 亿元

淘宝

59 亿元

11.11  
购物狂欢节

上天猫 就购了

13时38分  
支付宝总交易额

100 亿元

11.11  
购物狂欢节

上天猫 就购了  
淘宝论坛  
http://taobao.com

11时18分  
支付宝总交易额

79 亿元

11.11  
购物狂欢节

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# 双11狂欢



# 奇迹大揭密



支付宝交易额 **超10亿**

6分07秒

38分05秒

支付宝交易额 **超50亿**



文胸成交 **16000000** 件  
叠放= **3** 个珠穆朗玛峰高度

1小时

1小时零10秒

手机淘宝的支付宝交易额  
**突破10亿**



广东人民还在奋力拼搏  
成为全国省份购买力榜首  
交易金额 **超9亿**

凌晨3点

13点04分

支付宝交易额  
**突破191亿**  
超越2012年

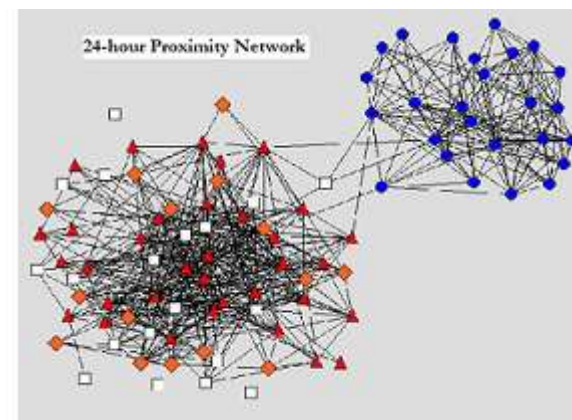
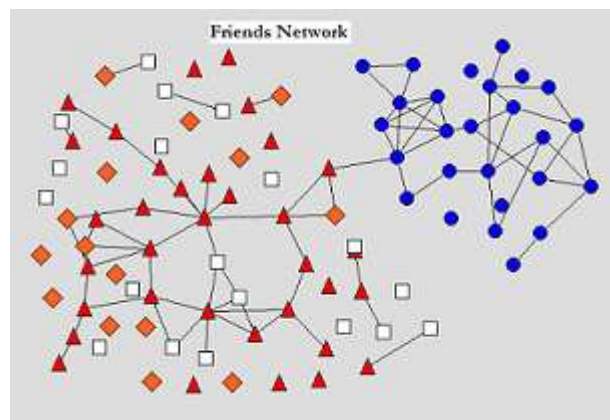
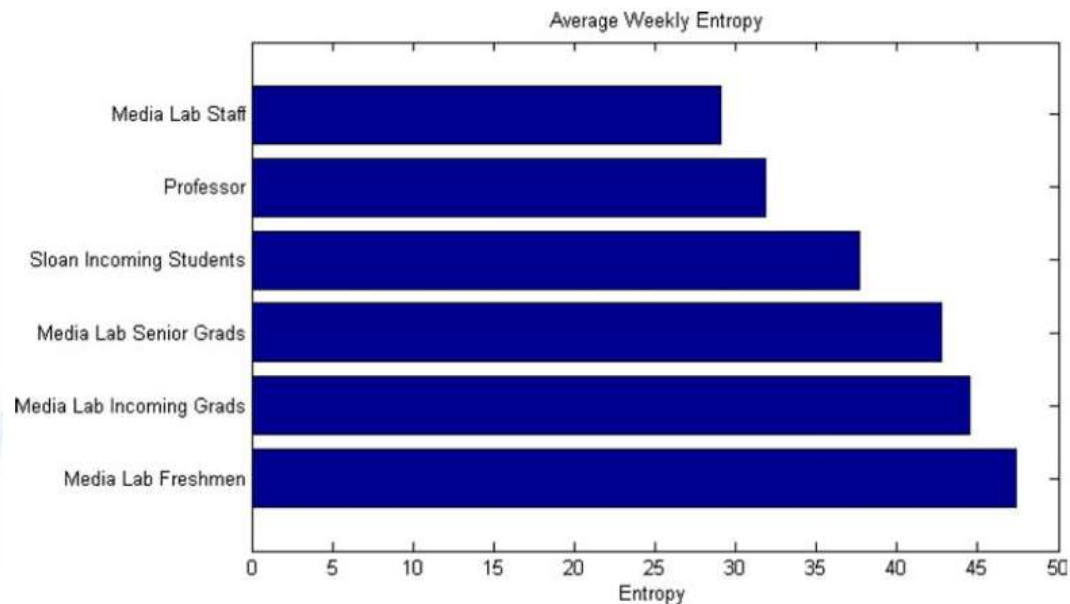
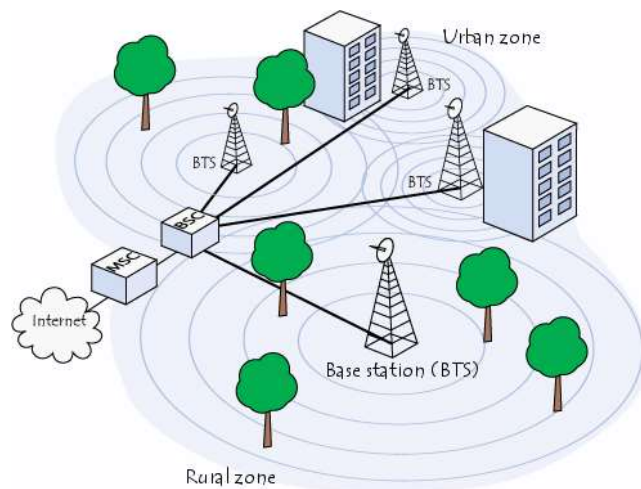


同时在线购物人数 **超1700万**  
= 香港人口的 **2.5倍**

13点17分

截止24:00  
支付宝交易额 **突破350.19亿**

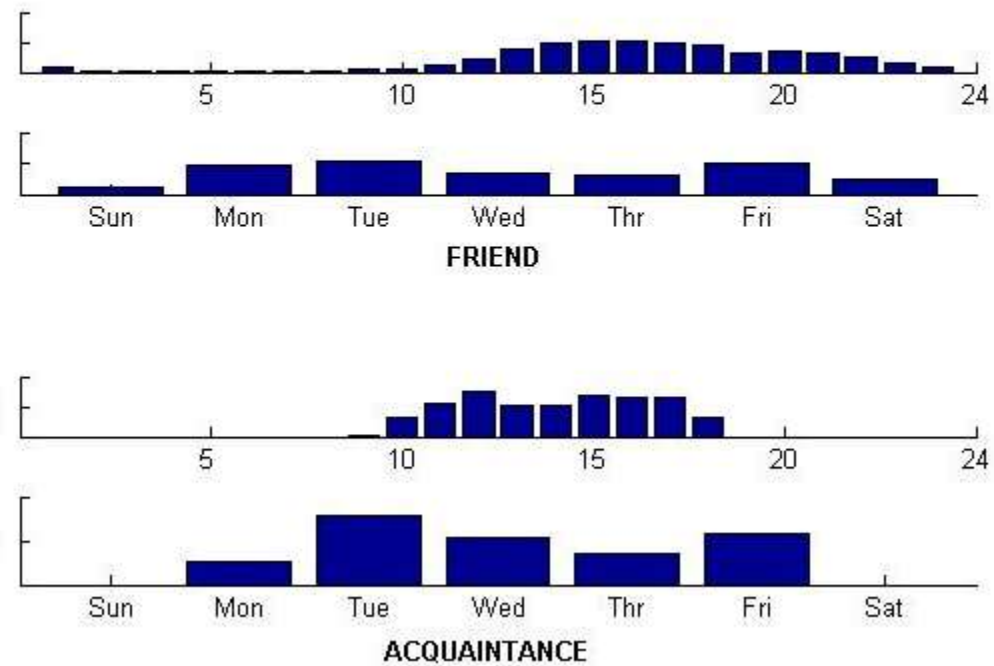
# Reality Mining



# Reality Mining



Friend vs. Acquaintance





缤点



HanYid  
韩衣



衣为饰



雪贝蕾  
xuebeile



水晶玛俐



Mel Gibson Helen Hunt

# What Women Want

He has the power  
to hear everything women  
are thinking.

Finally...a man  
is listening.

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PRODUCED BY MATT WILLIAMS SUSAN CARLSON AND GINA MATTHEWS WRITTEN BY BROCK DAVEY DIRECTED BY NANCY MEYERS AND TRANE SPRAKE AND JOSH GILDSMITH & CATHY YUSPA  
SOUNDTRACK AVAILABLE ON SONY MUSIC SOUNDTRACK  
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December 15

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# Open Questions

- ❖ Customers are analyzed based solely on purchasing records.
  - More dimensions are to be added.
  - Just imagine how to recommend something to your friend ...
- ❖ People have different **personalities**.
  - Different strategies may be required.
  - Selling insurance: Emotional vs. Mature
- ❖ People buy things for different **reasons**.
  - Impulse Buying vs. Planned Buying
  - Time Variant



# Reading Materials

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- ❖ E. Nathan and A. Pentland, "Reality Mining: Sensing Complex Social Systems", Personal and Ubiquitous Computing, vol. 10(4), pp. 255-268, 2006.