

Functional Design Patterns

@ScottWlaschin

fsharpforfunandprofit.com

fsharpWorks

Practices?

Approaches?

Functional Design Patterns



Tips?

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Functional Design Patterns

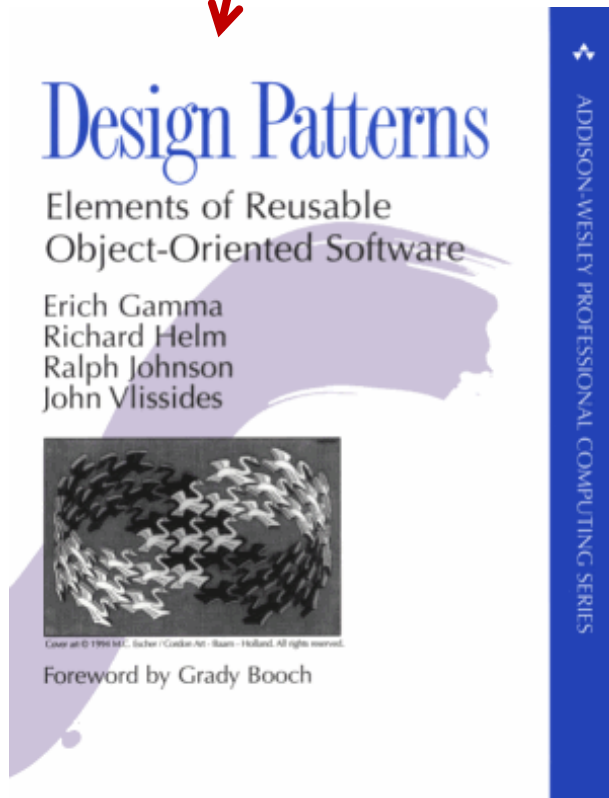
*So I'll reluctantly
stick with this...*

@ScottWlaschin

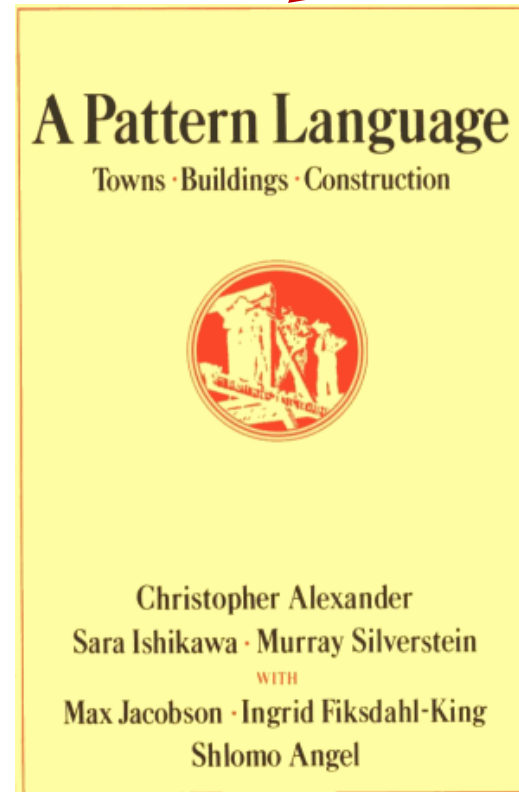
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Not this kind of pattern



nor this



These kind of patterns



All about recognizing repetition.

This kind of pattern!

Anne Adams Instructor



4683

42
SIZE

MADE ONLY IN WOMEN'S SIZES 34, 36, 38, 40, 42, 44, 46, 48, 50.

REQUIREMENTS FOR FABRICS WITHOUT NAP

SIZES	Band Sleeve Dress		Band Sleeve Dress With Contrast	
	35" FABRIC	39" FABRIC	35" FABRIC	39" FABRIC
34	4 yds.	3-7/8 yds.	3-3/8 yds.	3-3/8 yds.
36	4 "	3-7/8 "	3-5/8 "	3-1/2 "
38	4-1/8 "	4 "	3-3/4 "	3-5/8 "
40	4-5/8 "	4-3/8 "	3-7/8 "	3-5/8 "
42	4-3/4 "	4-3/8 "	4 "	3-5/8 "
44	4-3/4 "	4-3/8 "	4-1/8 "	3-3/4 "
46	4-7/8 "	4-1/2 "	4-1/8 "	3-3/4 "
48	5 "	4-1/2 "	4-3/8 "	3-7/8 "
50	5 "	4-1/2 "	4-1/2 "	3-7/8 "

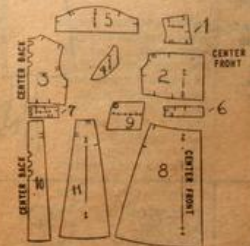
SIZES	Contrast Yokes, Pockets, Collar and Sleeves		Optional Ric rac
	35" FABRIC	39" FABRIC	
34	7/8 yd.	7/8 yd.	1-7/8 yds.
36	7/8 "	7/8 "	1-7/8 "
38	1 "	7/8 "	1-7/8 "
40	1 "	7/8 "	2 "
42	1 "	7/8 "	2 "
44	1 "	1 "	2 "
46	1 "	1 "	2 "
48	1 "	1 "	2 "
50	1 "	1 "	2-1/8 "

3" hem allowed on lower edge of dress.

PATTERN PARTS IDENTIFICATION GUIDE

CONSISTS OF 11 PARTS.

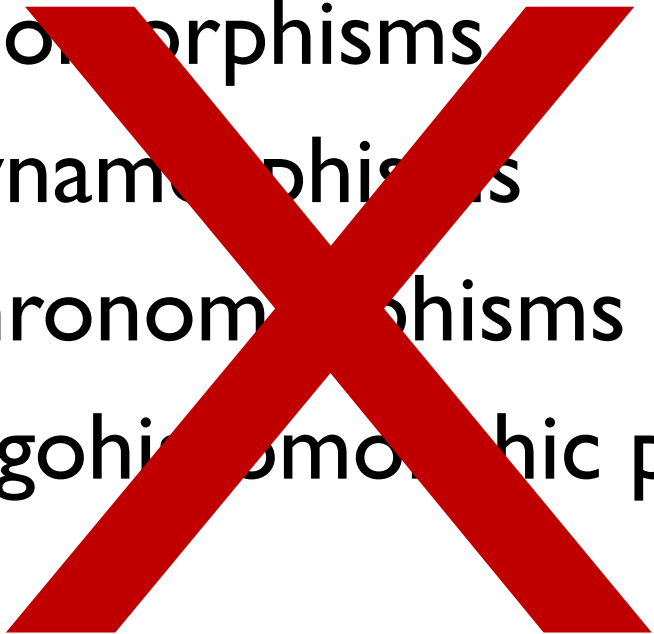
1. Yoke
2. Front
3. Back
4. Collar
5. Sleeve
6. Front set-in belt
7. Back set-in belt
8. Front skirt
9. Pocket
10. Back skirt
11. Side back skirt



PRINTED IN U.S.A.

A mixture of guidelines, templates, & construction advice

Functional patterns

- Apomorphisms
 - Dynamic morphisms
 - Chronomorphisms
 - Zygomorphic prepromorphisms
- 

Functional patterns

- Core Principles of FP design
 - Functions, types, composition
- Functions as parameters
 - Abstraction, Dependency injection
 - Partial application, Continuations, Folds,
- Chaining functions
 - Error handling, Async
 - Monads
- Dealing with wrapped data
 - Lifting, Functors
 - Validation with Applicatives
- Aggregating data and operations
 - Monoids

This talk



Functional programming is **scary**

Functor
Currying
Catamorphism

Applicative

Monad

Monoid



Functional programming is ^{unfamiliar} scary

“Mappable”

Currying

“Composables”

Applicative

“Chainable”

“Aggregatable”



Object oriented programming ^{This!} is scary

Generics
Interface
Polymorphism

Inheritance

SRP, OCP, LSP, ISP, DIP, Oh noes..

SOLID

Covariance

...don't forget IoC, DI,
ABC, MVC, etc., etc...

OO pattern/principle

- Single Responsibility Principle
- Open/Closed principle
- Dependency Inversion Principle
- Interface Segregation Principle
- Factory pattern
- Strategy pattern
- Decorator pattern
- Visitor pattern

FP pattern/principle

- Functions
- Functions
- Functions, also
- Functions
- Yes, functions
- Oh my, functions again!
- Functions
- Functions 😊

Seriously, FP patterns are different

A short and mostly wrong history of programming paradigms

Object-Oriented programming

- What we envisioned:
 - Smalltalk
 - What we got:
 - C++
 - Object oriented Cobol
 - PHP
 - Java
- “Worse is better”

Functional programming

- What we envisioned:
 - Haskell, OCaml, F#, etc
- What we got:
 - ??

Please don't let this happen to FP!

Important to understand!



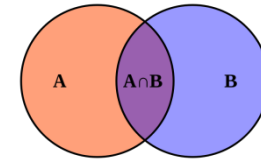
CORE PRINCIPLES OF FP DESIGN

Core principles of FP design

Steal from mathematics

$$\begin{array}{ccc} T^3 & \xrightarrow{T\mu} & T^2 \\ \mu T \downarrow & & \downarrow \mu \\ T^2 & \xrightarrow{\mu} & T \end{array} \quad \begin{array}{ccc} T & \xrightarrow{\eta T} & T^2 \\ T\eta \downarrow & \searrow & \downarrow \mu \\ T^2 & \xrightarrow{\mu} & T \end{array}$$

Types are not classes



Functions are things



Composition everywhere



Core principle: Steal from mathematics

“Programming is one of the most difficult branches of applied mathematics”
- E. W. Dijkstra

$$\begin{array}{ccc} T^3 & \xrightarrow{T\mu} & T^2 \\ \mu T \downarrow & & \downarrow \mu \\ T^2 & \xrightarrow{\mu} & T \end{array} \quad \begin{array}{ccc} T & \xrightarrow{\eta T} & T^2 \\ T\eta \downarrow & \searrow & \downarrow \mu \\ T^2 & \xrightarrow{\mu} & T \end{array}$$

Why mathematics

Dijkstra said:

- Mathematical assertions tend to be unusually **precise**.
- Mathematical assertions tend to be **general**.
They are applicable to a large (often infinite) class of instances.
- Mathematics embodies a discipline of reasoning allowing assertions to be made with an **unusually high confidence level**.

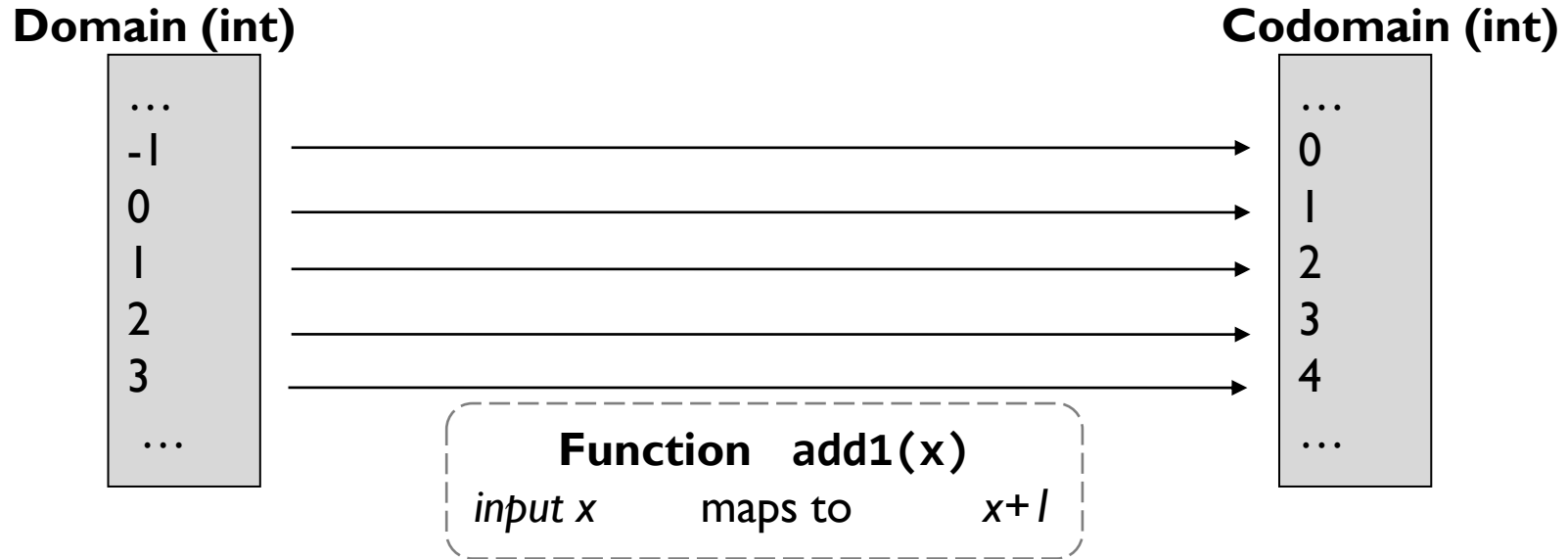
“Object-oriented programming is an exceptionally bad idea which could only have originated in California.”

E.W. Dijkstra

“You probably know that arrogance, in computer science, is measured in nanodijkstras.”

- Alan Kay

Mathematical functions



```
let add1 x = x + 1
```

```
val add1 : int -> int
```

Mathematical functions

A function doesn't "do" anything

Domain (int)

...
-1
0
1
2
3
...

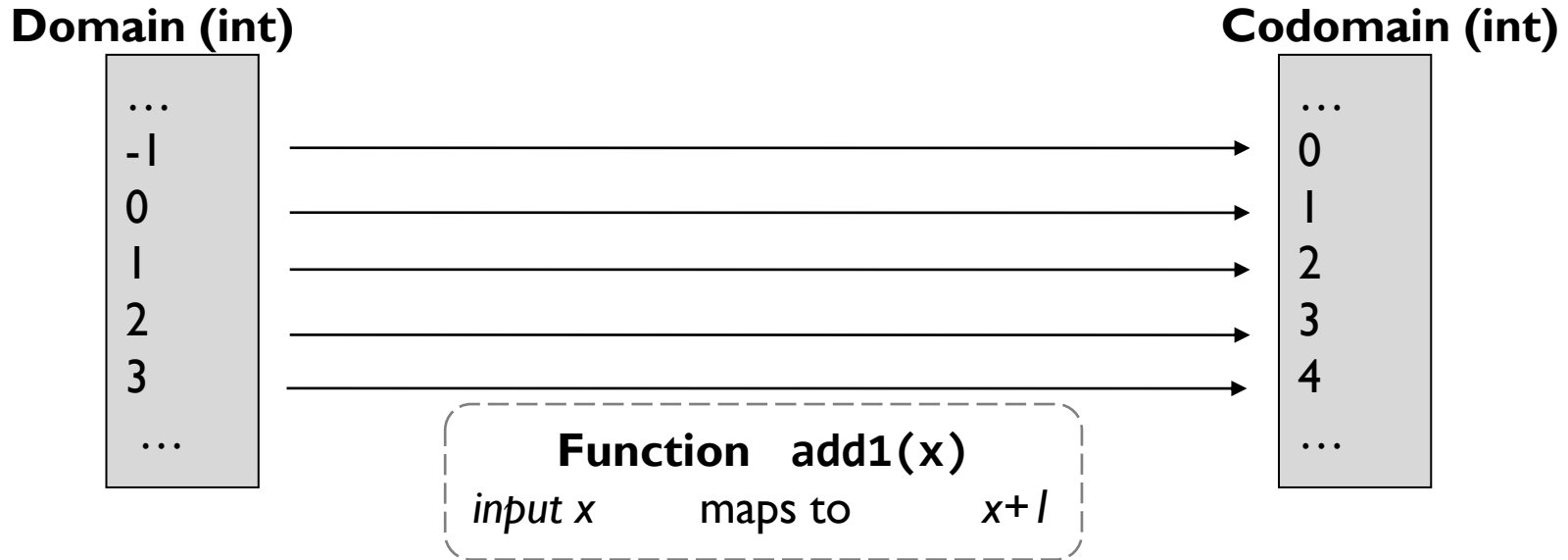
```
int add1(int input)
{
    switch (input)
    {
        case 0: return 1;
        case 1: return 2;
        case 2: return 3;
        case 3: return 4;
        etc ad infinitum
    }
}
```

Codomain (int)

...
0
1
2
3
4
...

- Input and output values already exist
- A function is not a calculation, just a mapping
- Input and output values are unchanged (**immutable**)

Mathematical functions



- A (mathematical) function always gives the **same output value** for a given input value
- A (mathematical) function has **no side effects**

Functions don't have to be about arithmetic

Customer (domain)

...
Cust1
Cust2
Cust3
Cust3
...

```
Name CustomerName(Customer input)
{
    switch (input)
    {
        case Cust1: return "Alice";
        case Cust2: return "Bob";
        case Cust3: return "Sue";
        etc
    }
}
```

Name (codomain)

...
Alice
Bob
Sue
John
Pam
...

*The universe of
Customers*

*The universe of
Personal Names*

Functions can work on functions

int->int

...
add1
times2
subtract3
add42
...

int list -> int list

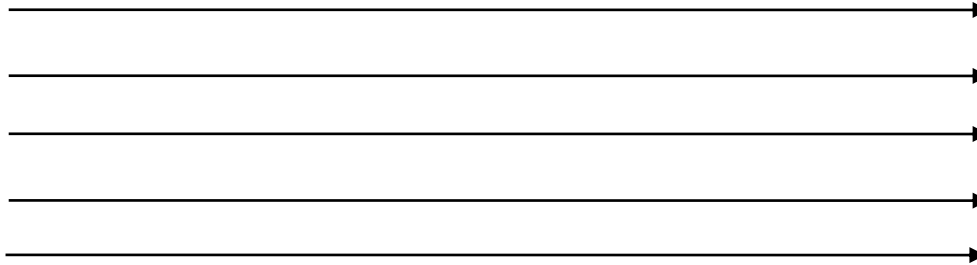
...
eachAdd1
eachTimes2
eachSubtract3
eachAdd42
...

Function List.map

int->int maps to *int list->int list*

The universe of
int->int
functions

The universe of
int list -> int list
functions



Guideline:
Strive for purity

↑
not always achievable
or desirable

The practical benefits of pure functions

Pure functions are easy to reason about

Reasoning about code that might not be pure:

```
customer.SetName(newName);
```

```
var name = customer.GetName();
```

Is the customer
being changed?

Reasoning about code that is pure:

```
let newCustomer = setCustomerName(aCustomer, newName)
```

```
let name, newCustomer = getCustomerName(aCustomer)
```

The customer is
being changed.

??? I can tell something is funny
just by looking at the code

“Don’t trust the name — trust the signature”

The practical benefits of pure functions

Pure functions are easy to **refactor**

```
let x = doSomething()  
let y = doSomethingElse(x)  
return y + 1
```

The practical benefits of pure functions

Pure functions are easy to **refactor**

```
let x = doSomething()  
let y = doSomethingElse(x)  
return y + 1
```



This can be extracted into a new function with cut/paste!

The practical benefits of pure functions

Pure functions are easy to **refactor**

```
let helper() =  
  let x = doSomething()  
  let y = doSomethingElse(x)  
  return y
```

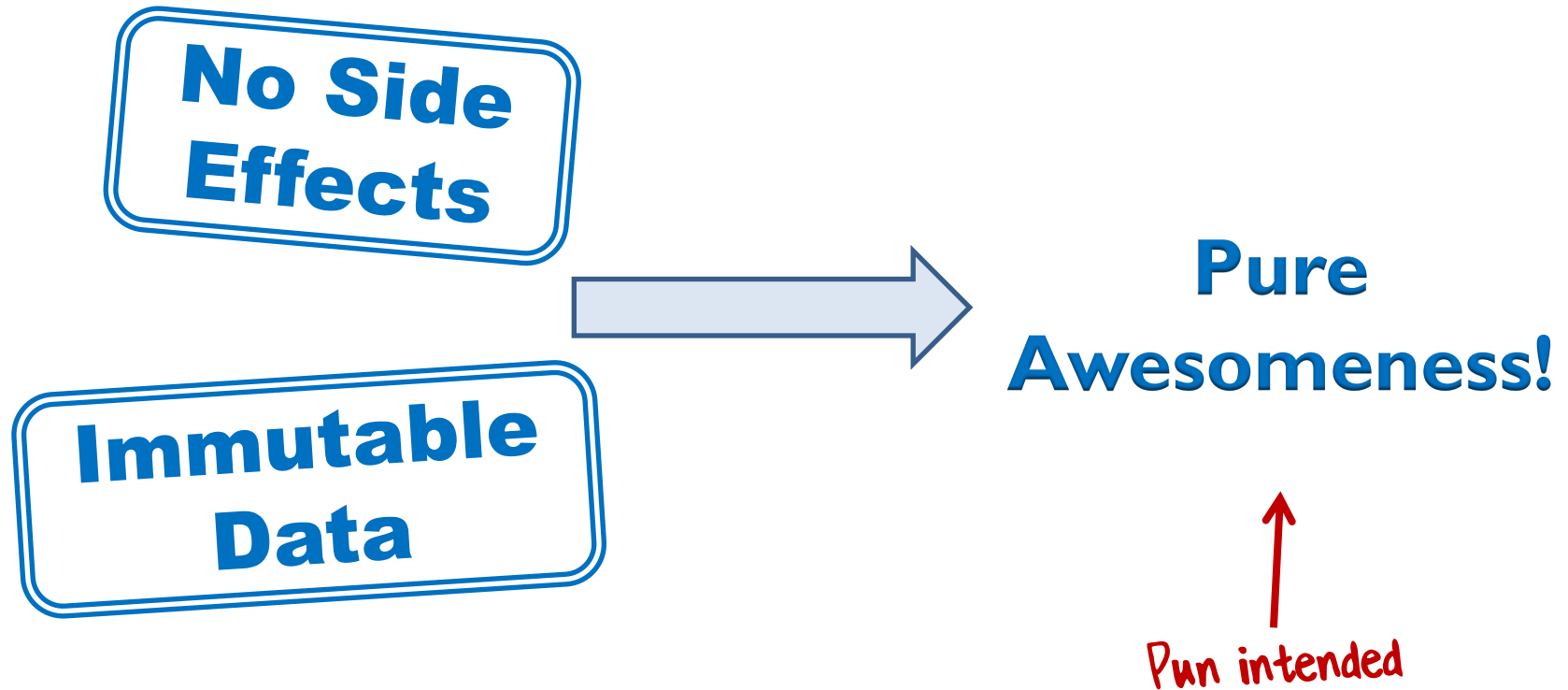
```
return helper() + 1
```

No Resharper needed!

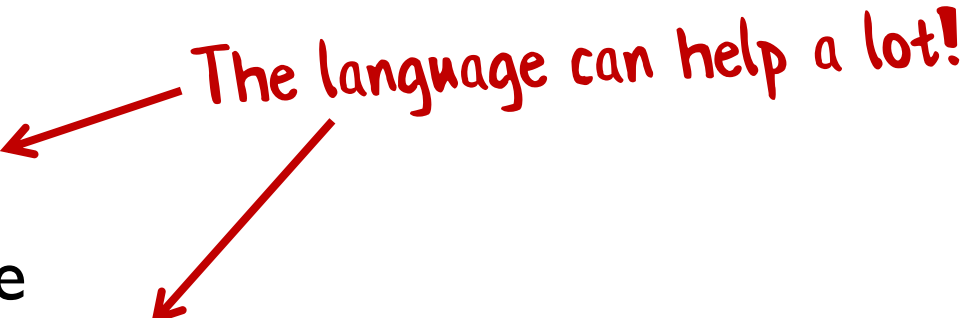
More practical benefits of pure functions

- Laziness
 - only evaluate when I need the output
- Cacheable results
 - same answer every time
 - "memoization"
- No order dependencies
 - I can evaluate them in any order I like
- Parallelizable
 - "embarrassingly parallel"

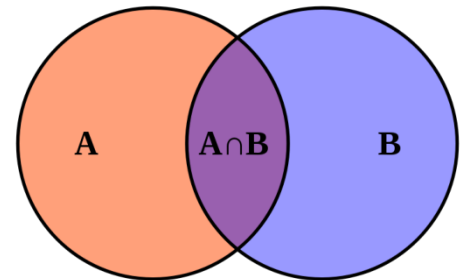
How to design a pure function

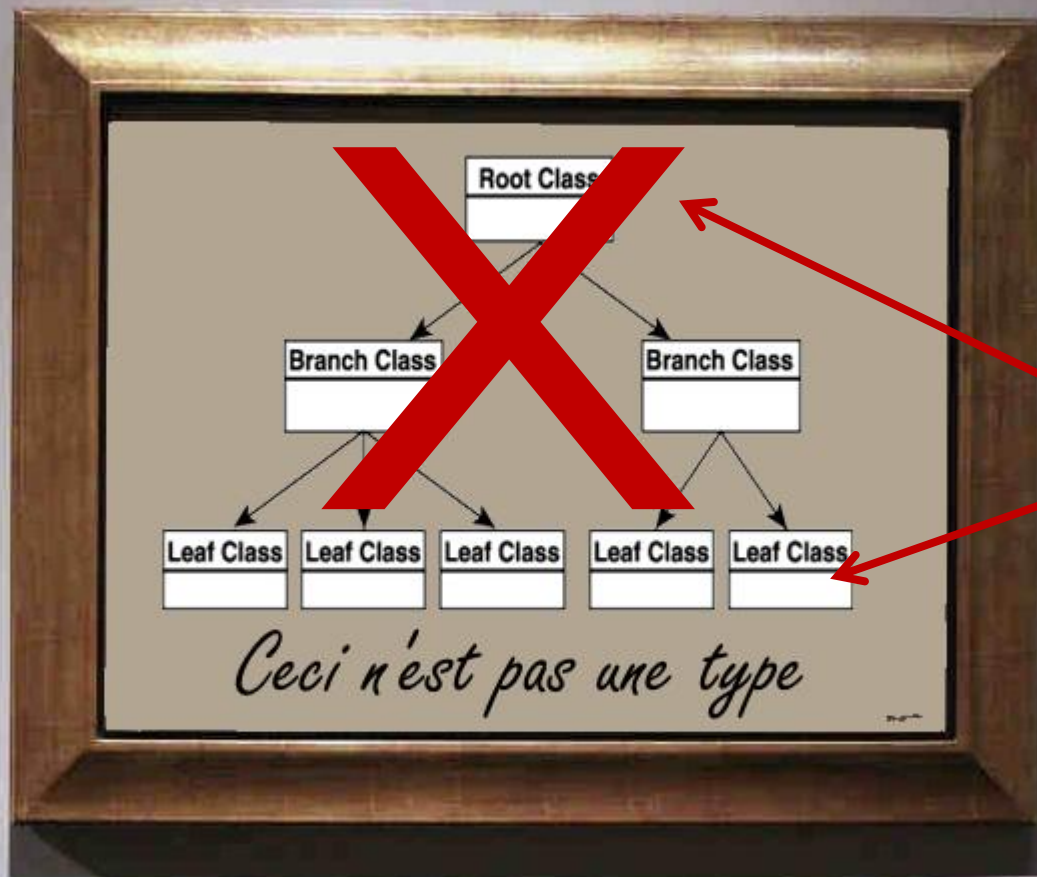


How to design a pure function

- 
- Haskell
 - very pure
 - F#, OCaml, Clojure, Scala
 - easy to be pure
 - C#, Java, JavaScript
 - have to make an effort

Core principle:
Types are not classes

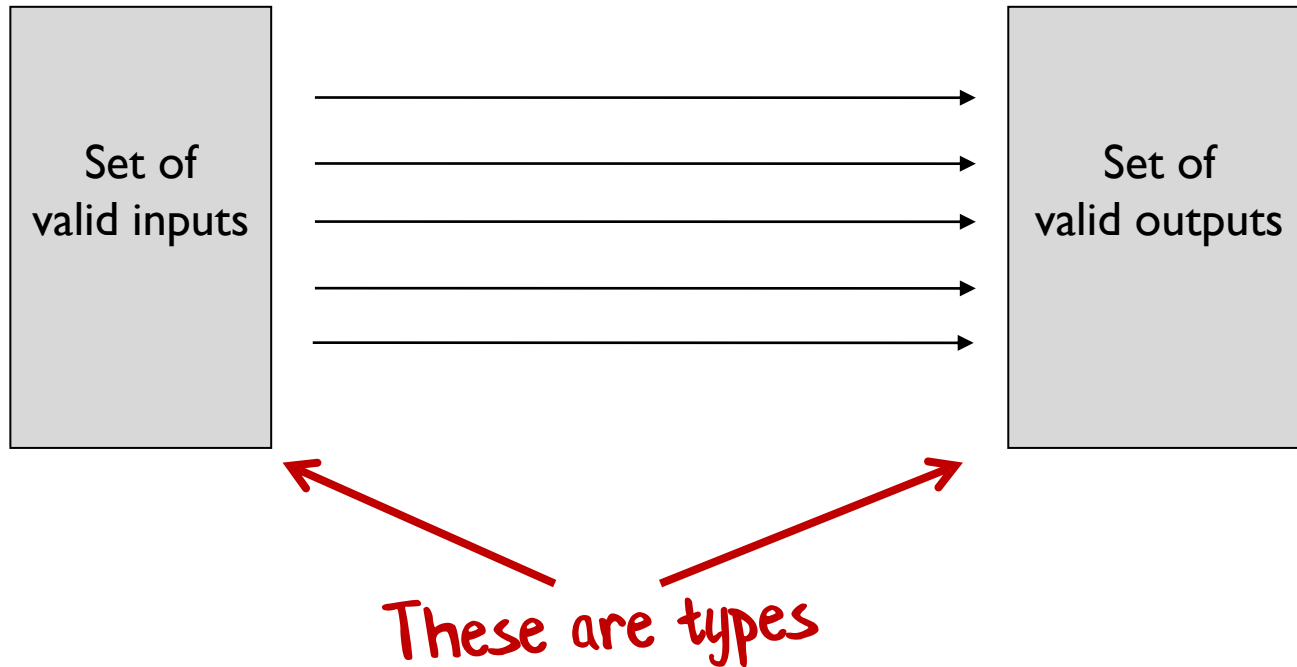




These are
not types

Types are not classes

So what is a type?

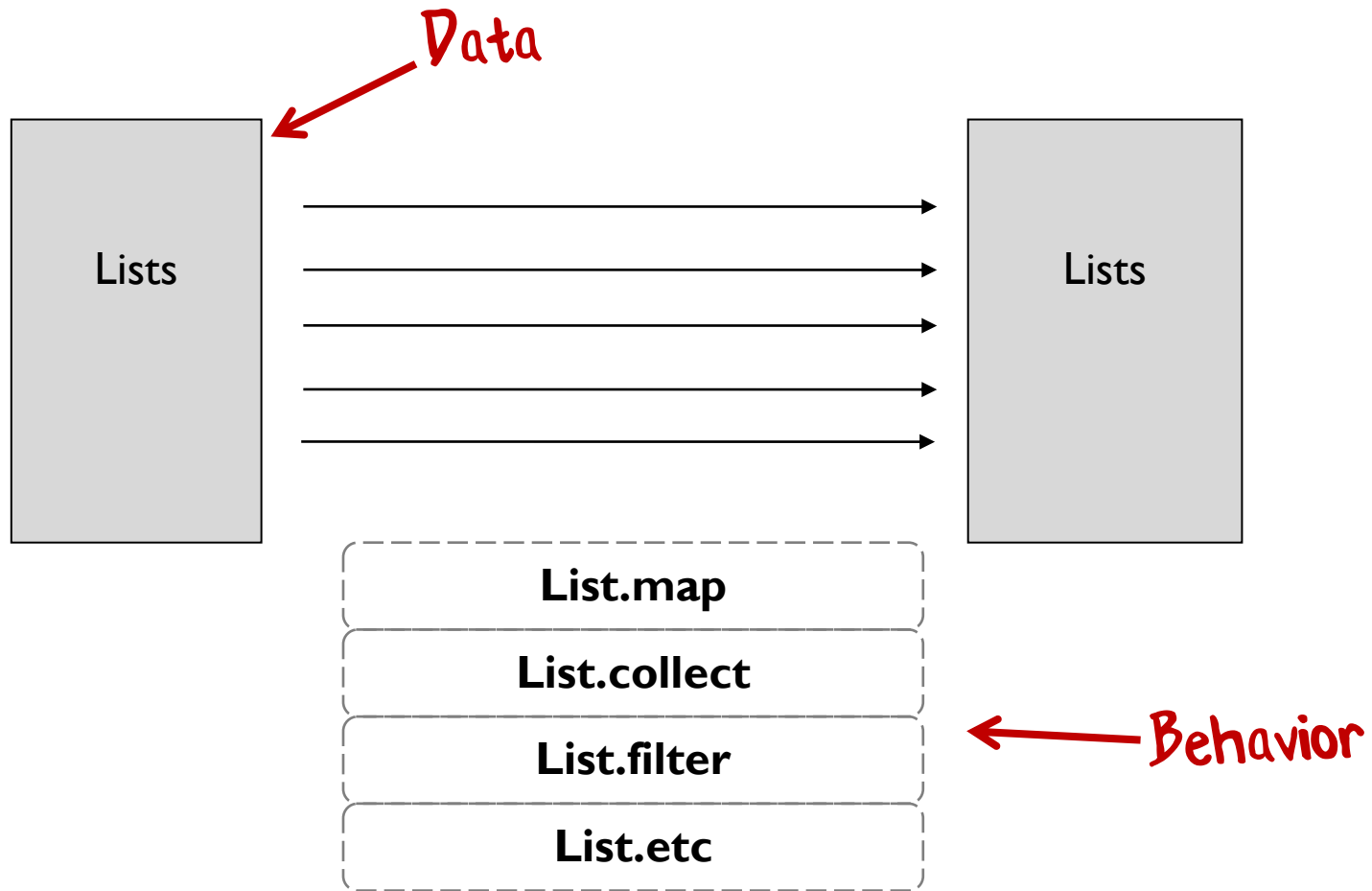


"Int" is a type

"Customer" is a type

"int->int" is a type

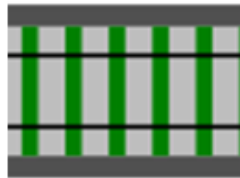
Types separate data from behavior



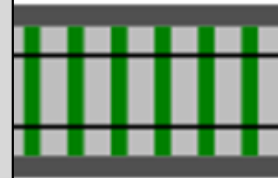
Core principle:
Functions are things



Functions as things

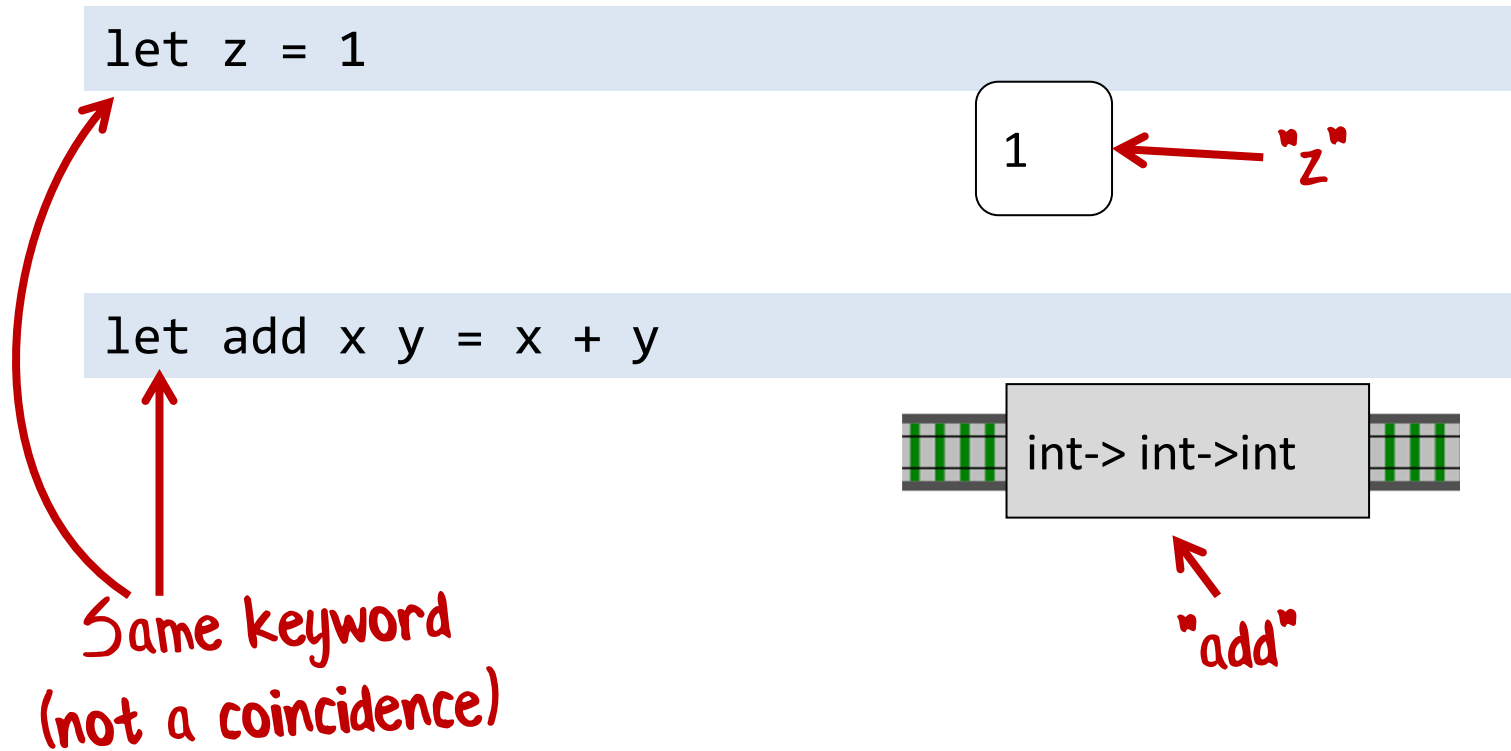


Function
apple -> banana



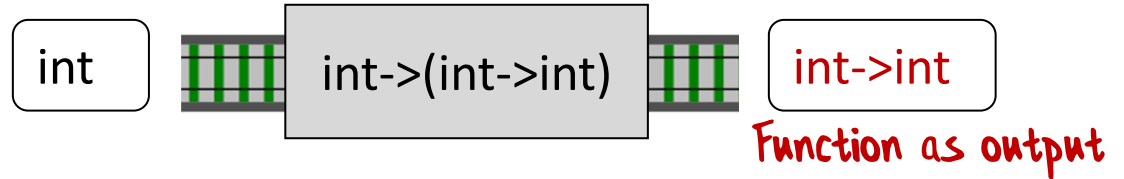
A function is a standalone thing,
not attached to a class

Functions as things

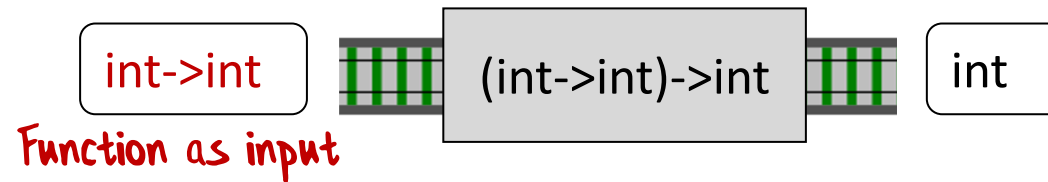


Functions as inputs and outputs

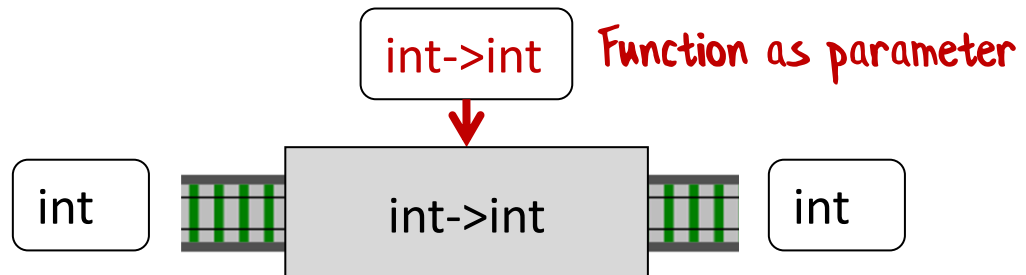
```
let add x = (fun y -> x + y)
```



```
let useFn f = f() + 1
```



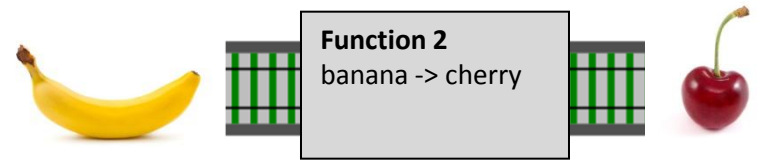
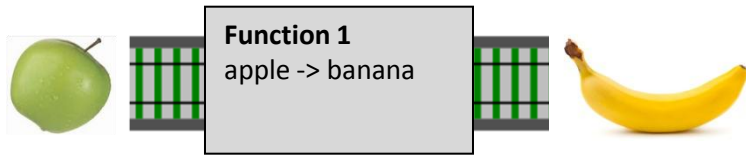
```
let transformInt f x = (f x) + 1
```



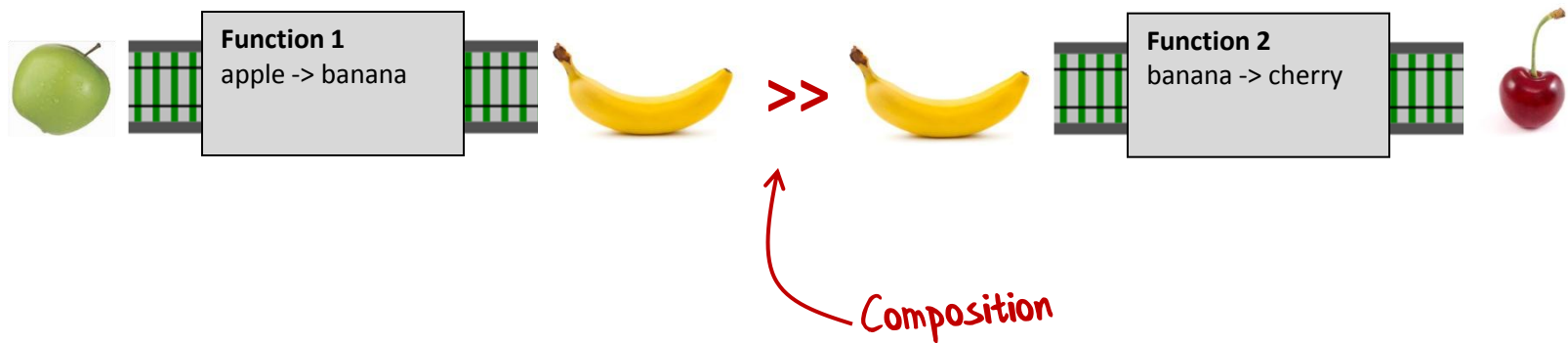
Core principle:
Composition everywhere



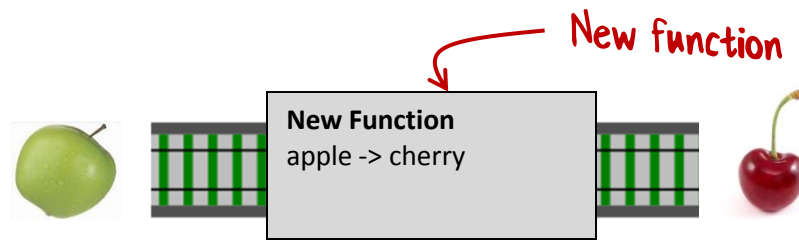
Function composition



Function composition



Function composition

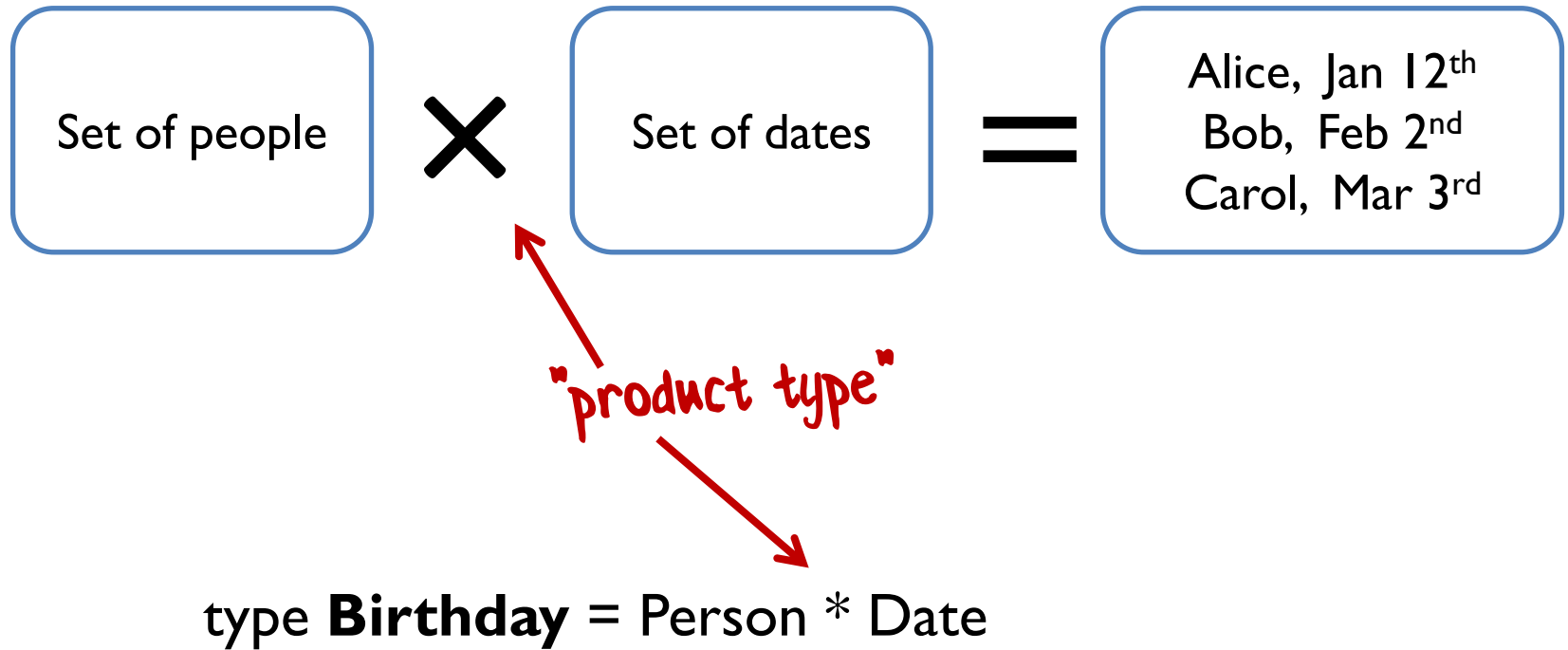


Can't tell it was built from
smaller functions!

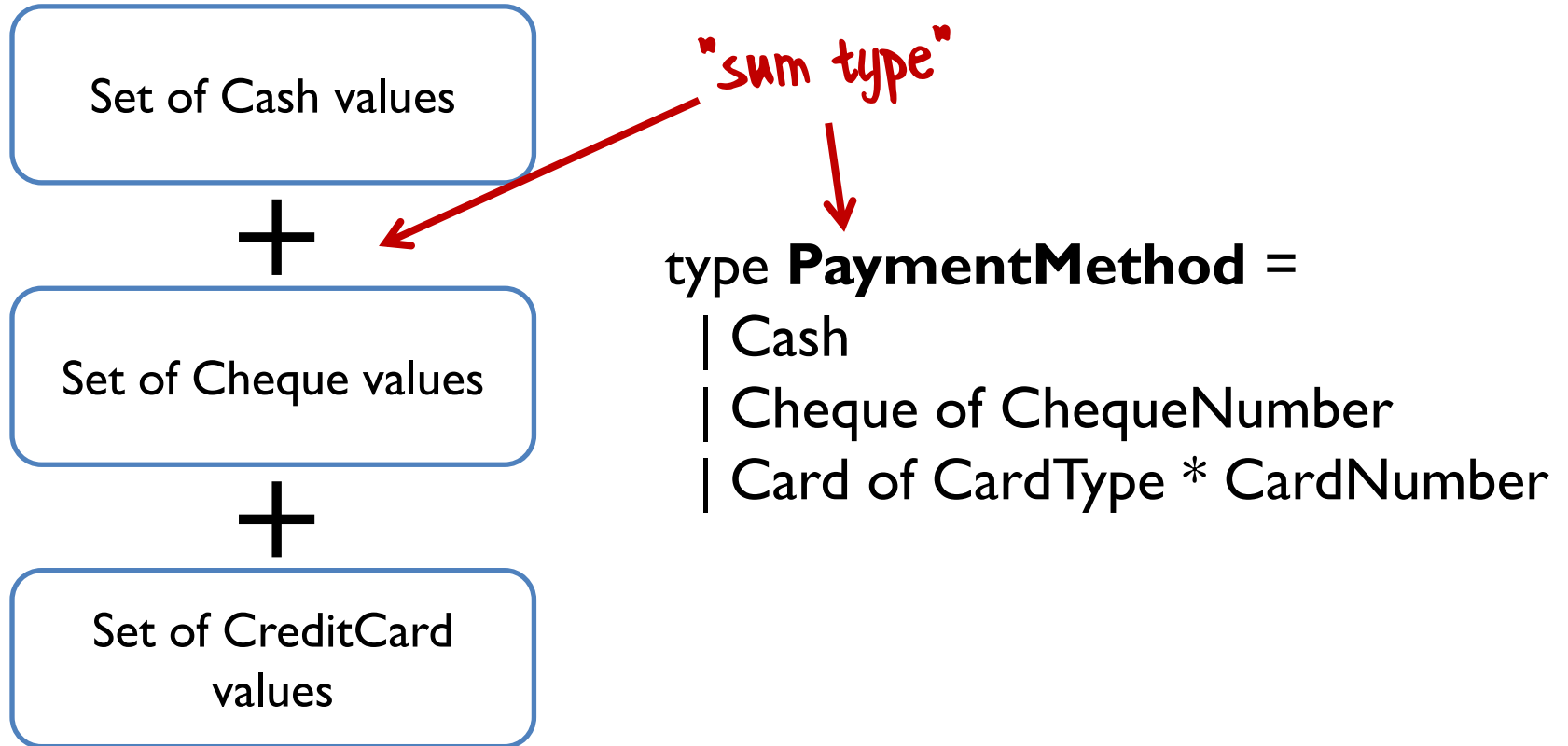
Types can be composed too

“algebraic types”

Product types



Sum types



DDD & DOMAIN MODELLING

Domain modelling pattern:
Use types to represent constraints

Avoid “primitive obsession”

Types represent constraints on input and output

type **Suit** = Club | Diamond | Spade | Heart

type **String50** = // non-null, not more than 50 chars

type **EmailAddress** = // non-null, must contain '@'

type **StringTransformer** = string -> string



Instant mockability

type **GetCustomer** = CustomerId -> Customer option

Domain modelling pattern:
Types are cheap

“There’s no problem that can’t be solved by wrapping it in a type”

Types are cheap

```
type Suit = Club | Diamond | Spade | Heart
```

```
type Rank = Two | Three | Four | Five | Six | Seven | Eight  
          | Nine | Ten | Jack | Queen | King | Ace
```

```
type Card = Suit * Rank
```

```
type Hand = Card list
```

*New types composed from
existing types*

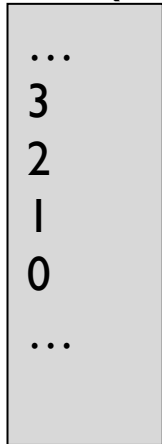


*Only one line of code to
create a type!*

Design principle:
Strive for totality

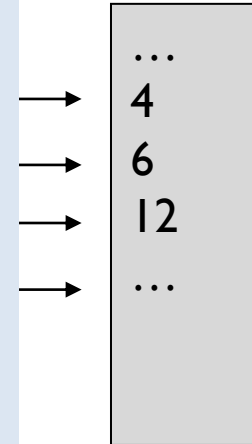
Totality

Domain (int)



```
int TwelveDividedBy(int input)
{
    switch (input)
    {
        case 3: return 4;
        case 2: return 6;
        case 1: return 12;
        case 0: return ??;
    }
}
```

Codomain (int)



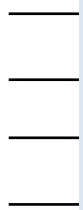
What happens here?

Totality

Constrain the input

NonZeroInteger

...
3
2
1
-1
...



```
int TwelveDividedBy(int input)
{
    switch (input)
    {
        case 3: return 4;
        case 2: return 6;
        case 1: return 12;
        case -1: return -12;
    }
}
```



int

...
4
6
12
...

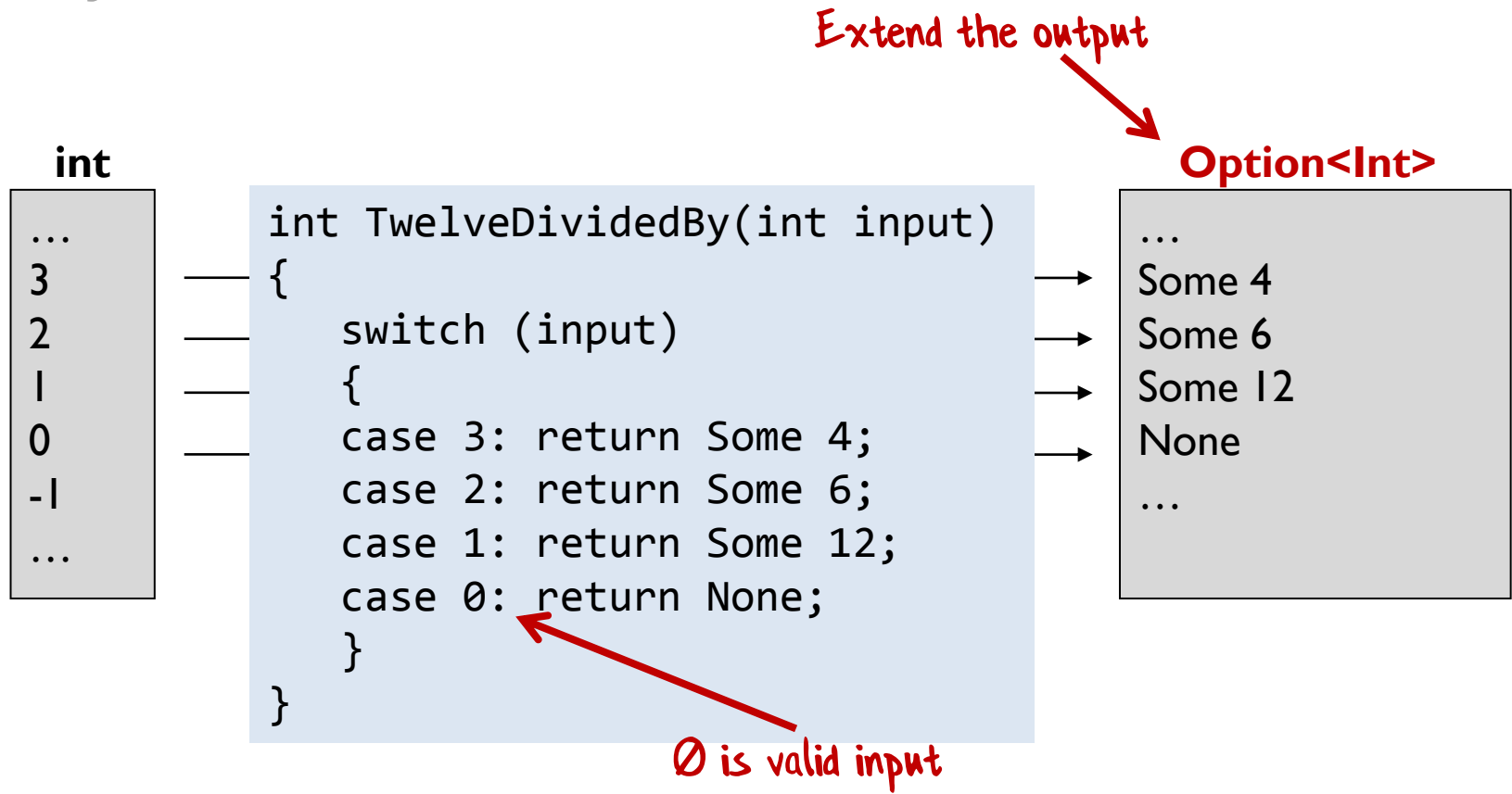
0 is missing

0 is doesn't have
to be handled

NonZeroInteger -> int

Types are documentation

Totality



int -> int option

Types are documentation

Design principle:
Use types to indicate errors

Output types as error codes

ParseInt: string -> int

ParseInt: string -> int option

No nulls
No exceptions

FetchPage: Uri -> String

FetchPage: Uri -> SuccessOrFailure<String>

LoadCustomer: CustomerId -> Customer

LoadCustomer: CustomerId -> SuccessOrFailure<Customer>

Use the signature, Luke!



Domain modelling principle:
“Make illegal states unrepresentable”

Types can represent business rules

```
type EmailContactInfo =  
  | Unverified of EmailAddress  
  | Verified of VerifiedEmailAddress
```

```
type ContactInfo =  
  | EmailOnly of EmailContactInfo  
  | AddrOnly of PostalContactInfo  
  | EmailAndAddr of EmailContactInfo * PostalContactInfo
```

Domain modelling principle:
Use sum-types instead of inheritance

Using sum vs. inheritance

```
type PaymentMethod =  
  | Cash  
  | Cheque of ChequeNumber  
  | Card of CardType * CardNumber
```

“closed” set of options

extra data is obvious

OO version:

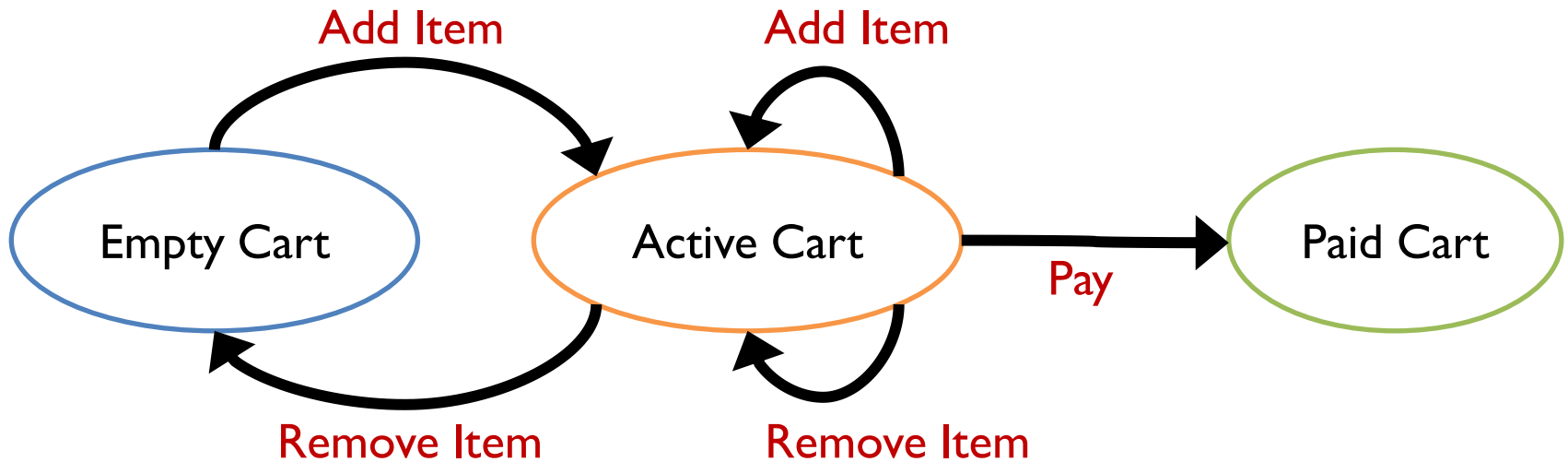
```
interface IPaymentMethod {..  
class Cash : IPaymentMethod {..  
class Cheque : IPaymentMethod {..  
class Card : IPaymentMethod {..  
class Evil : IPaymentMethod {..}
```

What goes in here? What is the common behaviour?

Definition is scattered around many locations

“open” set of options – unpleasant surprises?

Domain modelling principle:
Use sum-types for state machines



```
type ShoppingCart =  
  | EmptyCartState  
  | ActiveCartState of ActiveCartData  
  | PaidCartState of PaidCartData
```

Domain modelling principle:
It's ok to expose public data

It's ok to expose public data

Immutable



```
type PersonalName = {  
  FirstName: String50  
  MiddleInitial: String1 option  
  LastName: String50 }
```



*Can't create
invalid values*

Domain modelling principle:

Types are executable documentation

Types are executable documentation

type **Suit** = Club | Diamond | Spade | Heart

type **Rank** = Two | Three | Four | Five | Six | Seven | Eight
| Nine | Ten | Jack | Queen | King | Ace

type **Card** = Suit * Rank

← Types can be nouns

type **Hand** = Card list

type **Deck** = Card list

type **Player** = {Name:string; Hand:Hand}

type **Game** = {Deck:Deck; Players: Player list}

type **Deal** = Deck → (Deck * Card)

← Types can be verbs

type **PickupCard** = (Hand * Card) → Hand

Types are executable documentation

type **CardType** = Visa | Mastercard

type **CardNumber** = CardNumber of string

type **ChequeNumber** = ChequeNumber of int

type **PaymentMethod** =

| Cash

| Cheque of ChequeNumber

| Card of CardType * CardNumber

*Can you guess what
payment methods are
accepted?*



More on DDD and designing with types at
fsharpforfunandprofit.com/ddd

Static types only!
Sorry Clojure and JS
developers ☹

HIGH-LEVEL DESIGN

Design paradigm:
Functions all the way down





“Functions in the small,
objects in the large”

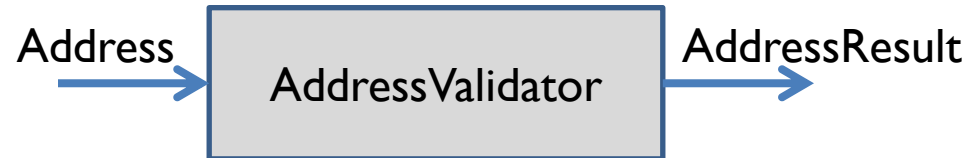
“Functions in the small,
functions in the large”

Low-level operation

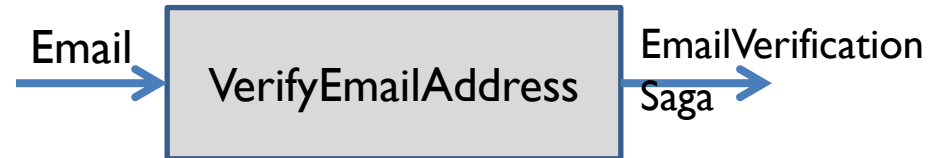


Service

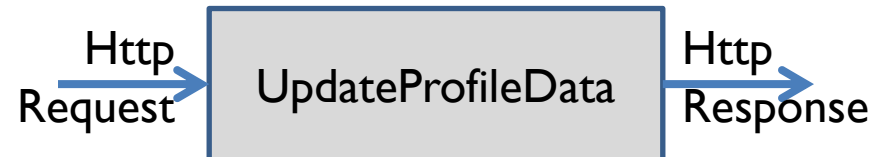
"Service" is the new "microservice"



Domain logic



High-level use-case



"Composition is fractal"

Design paradigm:
Transformation-oriented
programming



Interacting with the outside world

```
type ContactDTO = {  
    External model  
    FirstName: string  
    MiddleInitial: string  
    LastName: string  
  
    EmailAddress: string  
    IsEmailVerified: bool  
}
```


*Transformation to clean
internal model*

```
type EmailAddress = ...  
    Internal model
```

```
type VerifiedEmail =  
    VerifiedEmail of EmailAddress
```

```
type EmailContactInfo =  
    | Unverified of EmailAddress  
    | Verified of VerifiedEmail
```

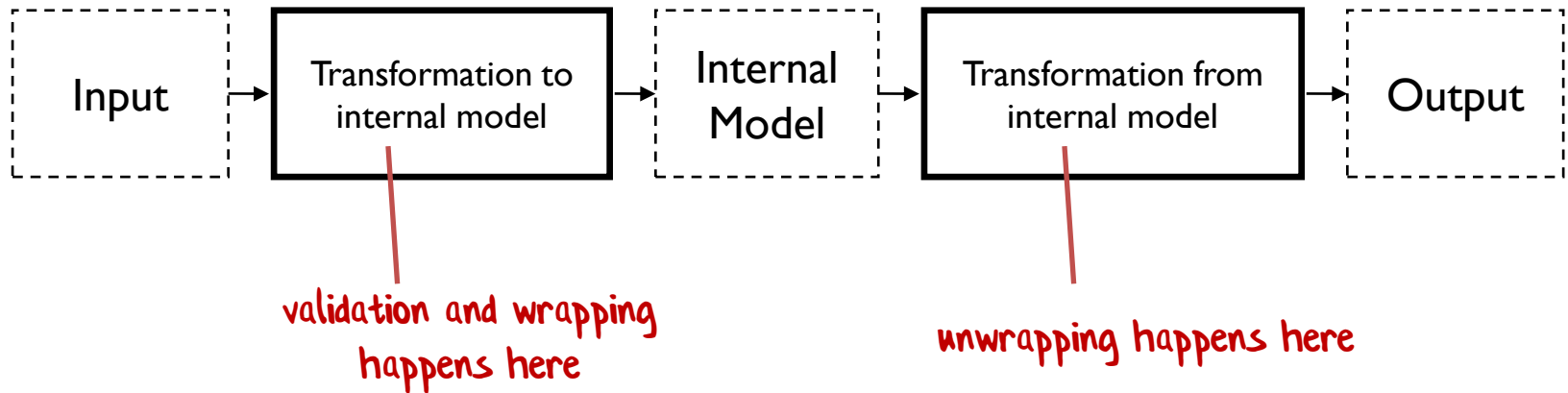
```
type PersonalName = {  
    FirstName: String50  
    MiddleInitial: String1 option  
    LastName: String50 }
```

```
type Contact = {  
    Name: PersonalName  
    Email: EmailContactInfo }
```

Transformation oriented programming

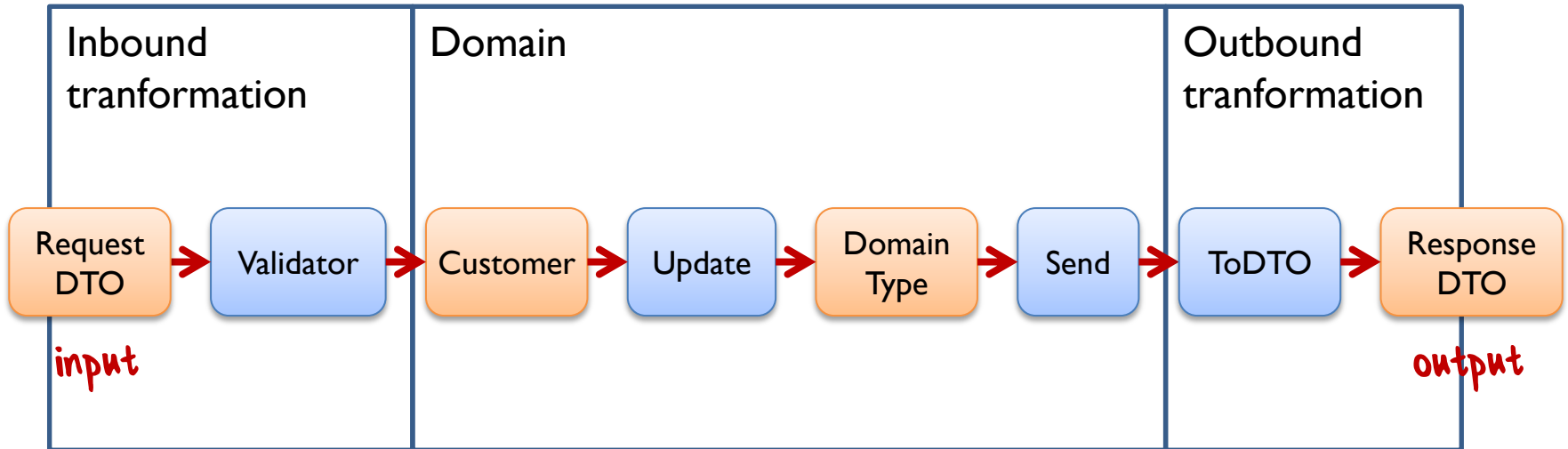


Transformation oriented programming



“transformation-oriented programming”

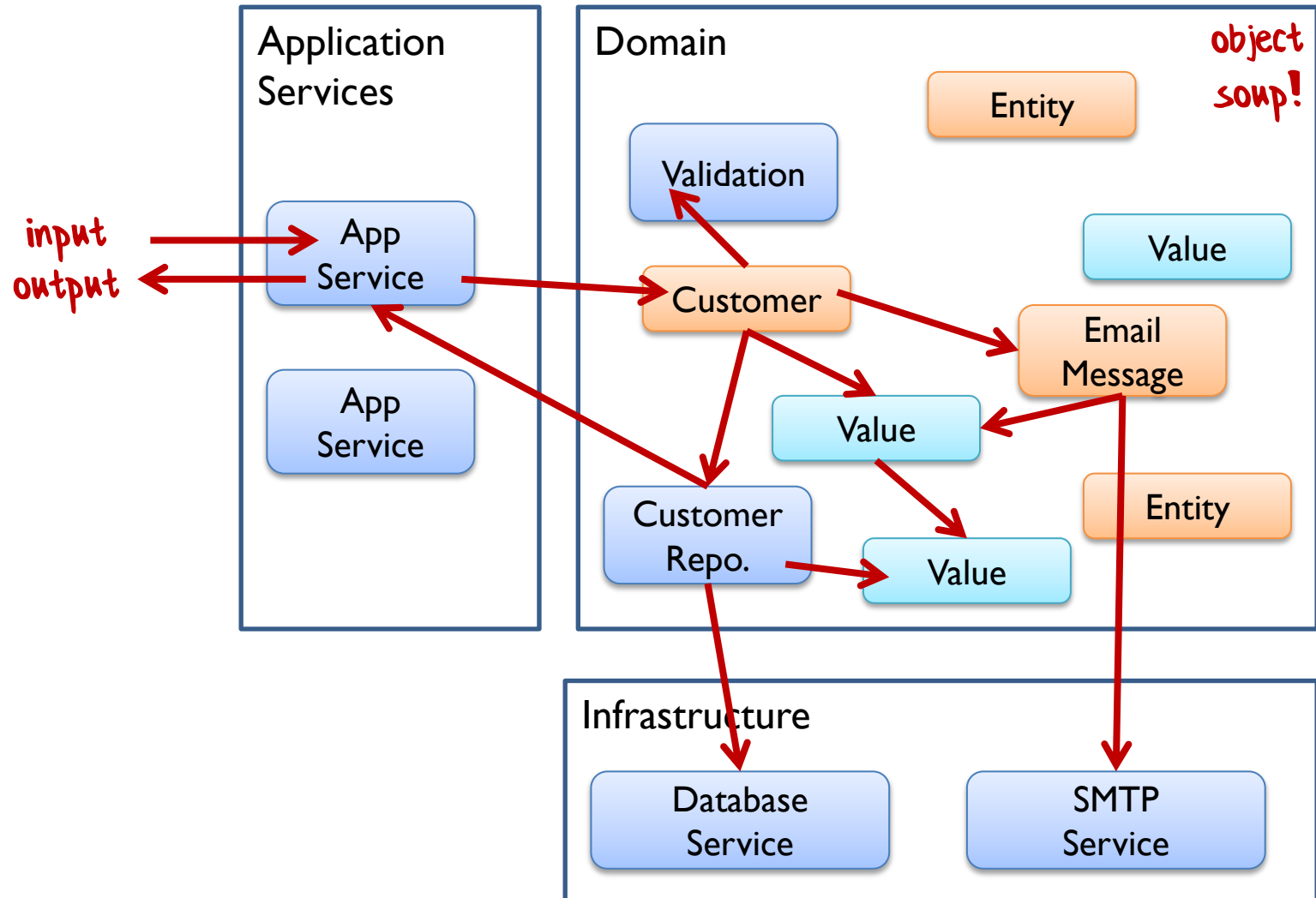
Flow of control in a FP use case



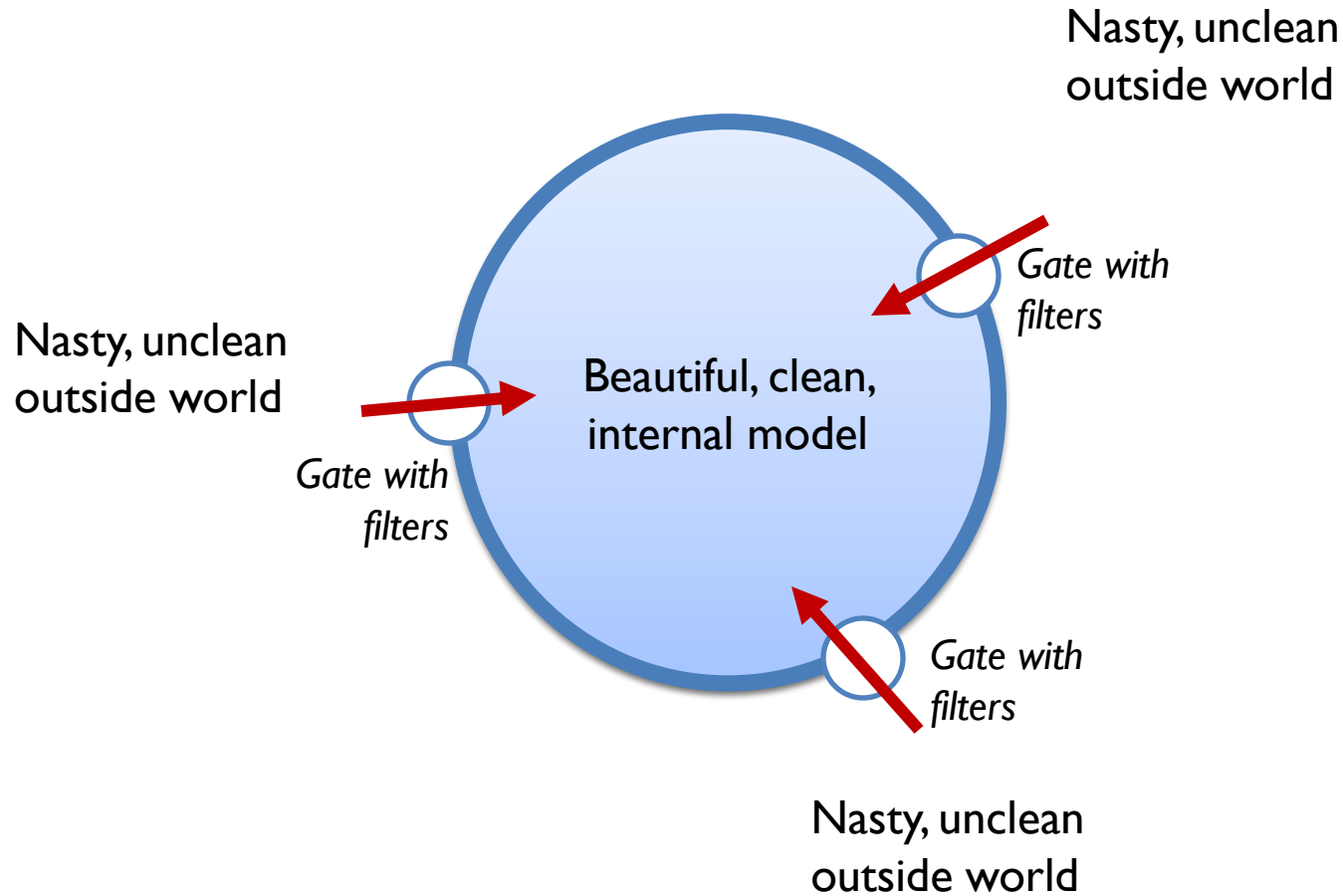
Linear!

Works well with domain events, FRP, etc

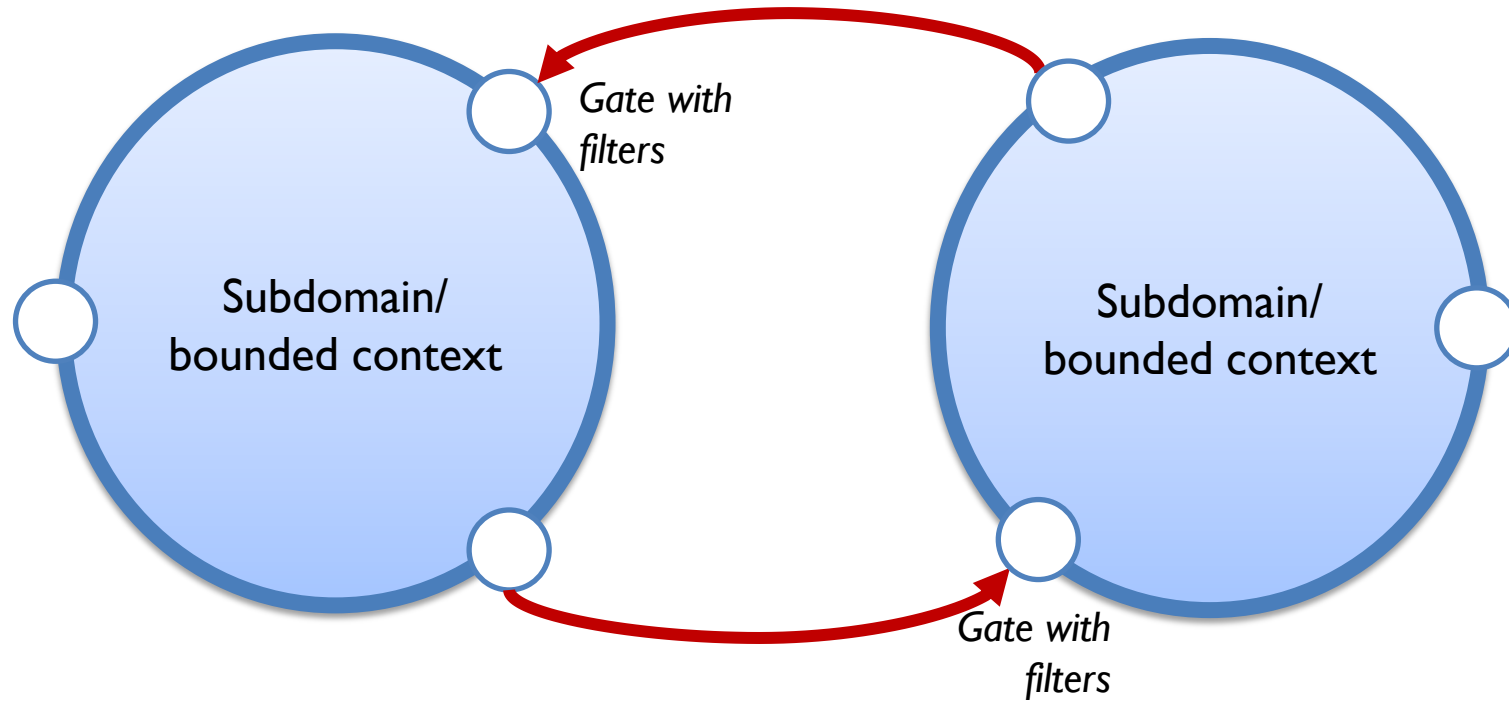
Flow of control in a OO use case



Interacting with the outside world

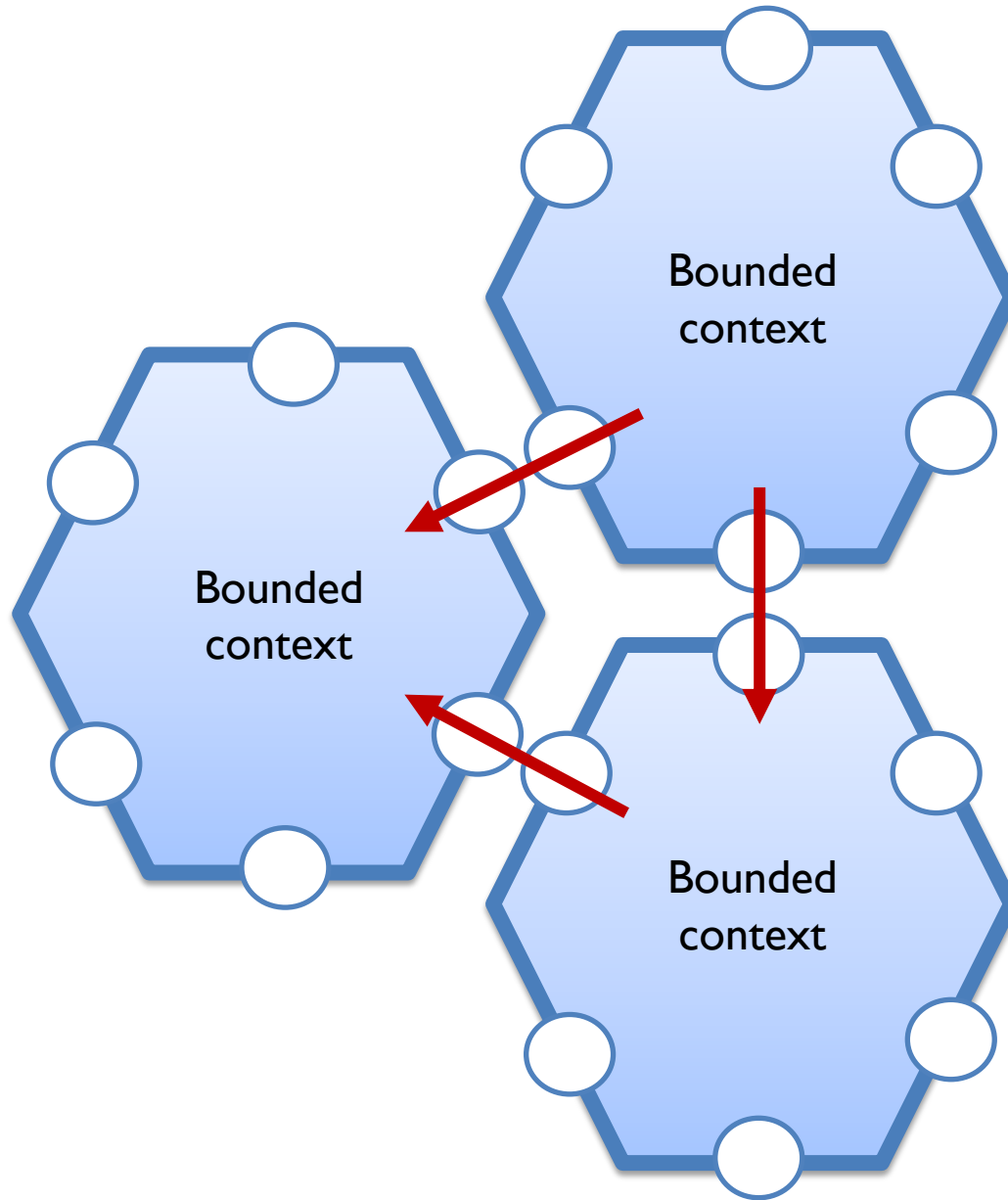


Interacting with the other domains



Transformation from one
domain to another

Interacting with the other domains



*Hexagonal
architecture!*

FUNCTIONS AS PARAMETERS

Guideline:

Parameterize all the things

Parameterize all the things

```
let printList() =  
  for i in [1..10] do  
    printfn "the number is %i" i
```


Parameterize all the things

It's second nature to parameterize the data input:

```
let printList aList =  
  for i in aList do  
    printfn "the number is %i" i
```

Parameterize all the things

FPers would parameterize the action as well:

```
let printList anAction aList =  
  for i in aList do  
    anAction i
```

↖
We've decoupled the
behavior from the data

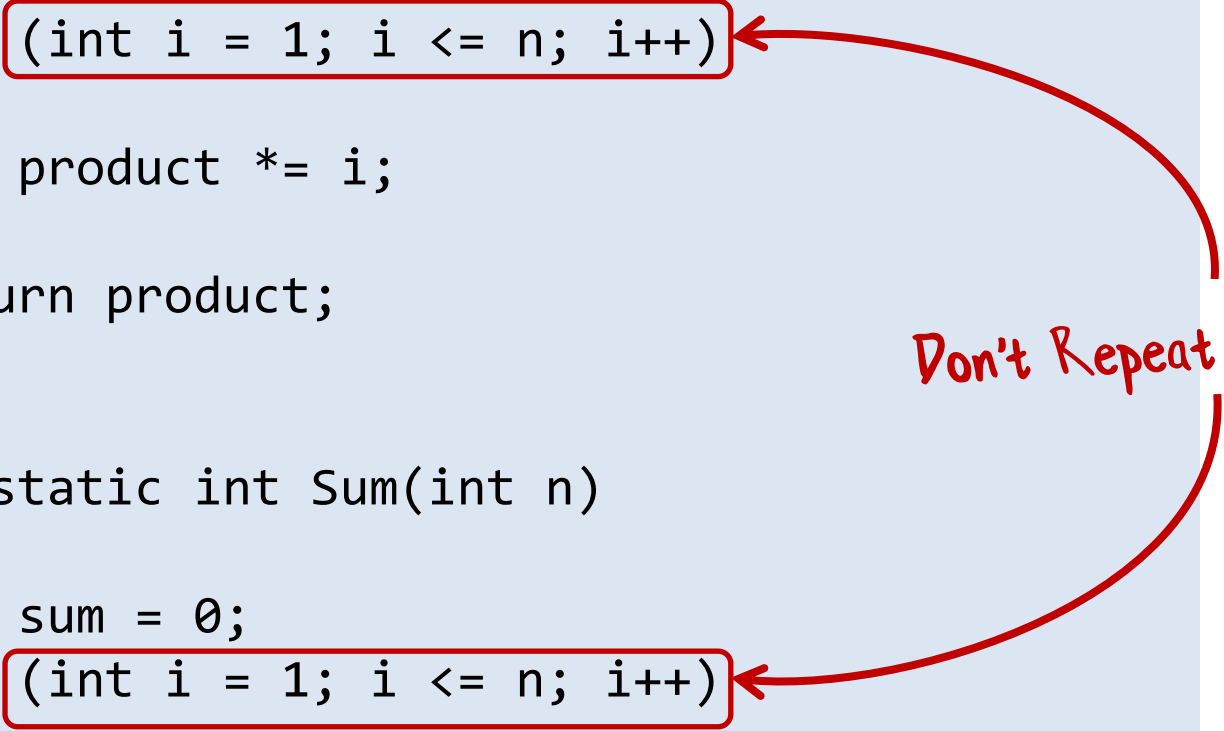
↖
A good language makes
this trivial to do!

Parameterize all the things

```
public static int Product(int n)
{
    int product = 1;
    for (int i = 1; i <= n; i++)
    {
        product *= i;
    }
    return product;
}
```

```
public static int Sum(int n)
{
    int sum = 0;
    for (int i = 1; i <= n; i++)
    {
        sum += i;
    }
    return sum;
}
```

Don't Repeat Yourself



Parameterize all the things

```
public static int Product(int n)
{
```

```
    int product = 1;
```

```
    for (int i = 1; i <= n; i++)
```

```
    {
```

```
        product *= i;
```

```
    }
```

```
    return product;
```

```
}
```

```
public static int Sum(int n)
```

```
{
```

```
    int sum = 0;
```

```
    for (int i = 1; i <= n; i++)
```

```
    {
```

```
        sum += i;
```

```
    }
```

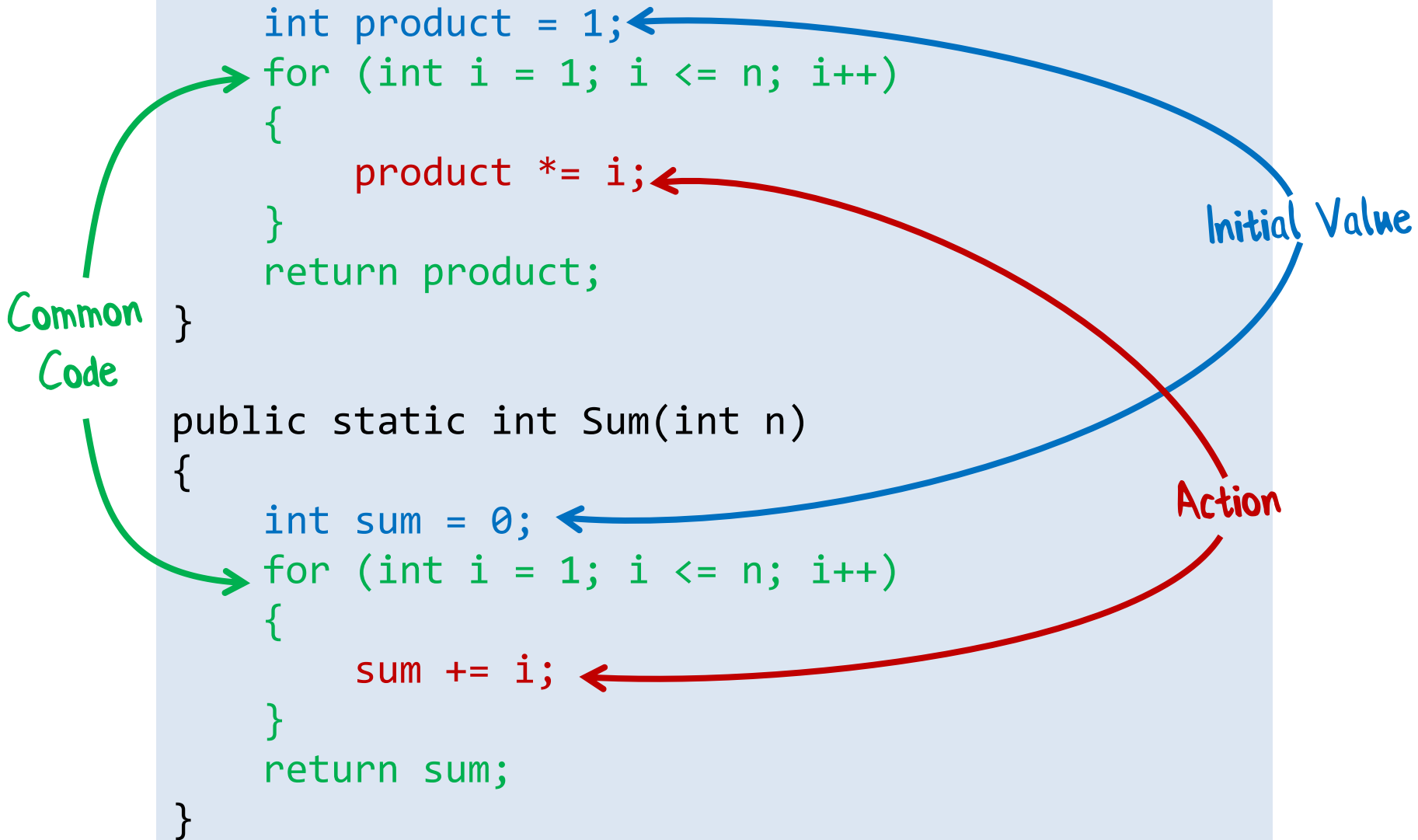
```
    return sum;
```

```
}
```

Initial Value

Action

Common
Code



Parameterize all the things

```
let product n =  
  let initialValue = 1  
  let action productSoFar x = productSoFar * x  
  [1..n] |> List.fold action initialValue
```

```
let sum n =  
  let initialValue = 0  
  let action sumSoFar x = sumSoFar+x  
  [1..n] |> List.fold action initialValue
```

Parameterized
action

Common code extracted

Initial Value

Lots of collection functions like this:
"fold", "map", "reduce", "collect", etc.

Guideline:

Be as generic as possible

Generic code

```
let printList anAction aList =  
    for i in aList do  
        anAction i  
  
// val printList :  
//    ('a -> unit) -> seq<'a> -> unit
```

Any kind of collection,
any kind of action!

F# and other functional languages
make code generic automatically

Generic code

```
int -> int
```

How many ways are there to
implement this function?

```
'a -> 'a
```

How many ways are there to
this function?

Generic code

```
int list -> int list
```

How many ways are there to
implement this function?

```
'a list -> 'a list
```

How many ways are there to
this function?

Generic code

```
('a -> 'b) -> 'a list -> 'b list
```

How many ways are there to
implement this function?

Tip:

Function types are "interfaces"

Function types provide instant
abstraction!

Function types are interfaces

```
interface IBunchOfStuff
{
    int DoSomething(int x);
    string DoSomethingElse(int x);
    void DoAThirdThing(string x);
}
```

Let's take the
Single Responsibility Principle and the
Interface Segregation Principle
to the extreme...

Every interface should have
only one method!

Function types are interfaces

```
interface IBunchOfStuff
{
    int DoSomething(int x);
}
```

An interface with one method is a just a function type

```
type IBunchOfStuff: int -> int
```

Any function with that type is compatible with it

```
let add2 x = x + 2           // int -> int
let times3 x = x * 2         // int -> int
```

Strategy pattern is trivial in FP

Object-oriented strategy pattern:

```
class MyClassinterface IBunchOfStuff
{
    public MyClass(IBunchOfStuff strategy) {...}

    int DoSomethingWithStuff(int x)
    {
        return _strategy.DoSomething(x)
    }
}
```

Functional equivalent:

```
let DoSomethingWithStuff strategy x =
    strategy x
```

+ with FP approach => you don't need to create an interface in advance.
& you can substitute ANY function in later

Decorator pattern in FP

Functional equivalent of decorator pattern

```
let add1 x = x + 1    // int -> int
```

Decorator pattern in FP

Functional equivalent of decorator pattern

```
let add1 x = x + 1    // int -> int
```

```
let logged f x =  
  printfn "input is %A" x  
  let result = f x  
  printfn "output is %A" result  
  result
```


Decorator pattern in FP

Functional equivalent of decorator pattern

```
let add1 x = x + 1    // int -> int
```

```
let logged f x =  
  printfn "input is %A" x  
  let result = f x  
  printfn "output is %A" result  
  result
```

```
let add1Decorated =    // int -> int  
  logged add1
```

```
[1..5] |> List.map add1
```

```
[1..5] |> List.map add1Decorated
```

Tip

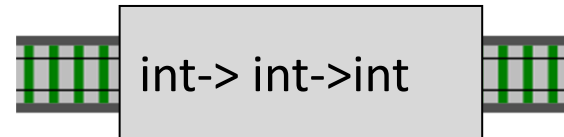
Every function is a
one parameter function

Writing functions in different ways

Two parameters



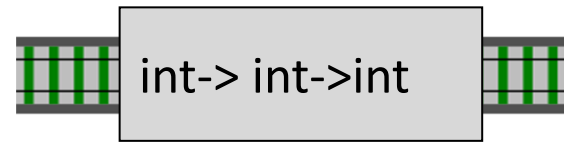
```
let add x y = x + y
```



No parameters



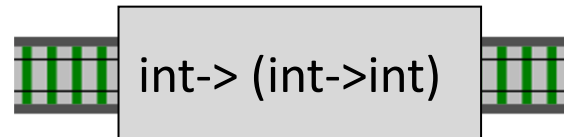
```
let add = (fun x y -> x + y)
```



One parameter



```
let add x = (fun y -> x + y)
```



```
let three = 1 + 2
```

```
let three = (+) 1 2
```

```
let add1 = (+) 1
```

← Missing a parameter?

```
let add1ToEach = List.map add1
```

Pattern:
Partial application

```
let name = "Scott"
printfn "Hello, my name is %s" name
```

Two parameters

```
let name = "Scott"
let hello = (printfn "Hello, my name is %s")
```

```
let name = "Scott"
let hello = (printfn "Hello, my name is %s")
hello name
```

```
let names = ["Alice"; "Bob"; "Scott"]
Names |> List.iter hello
```

One parameter

Pattern:

Use partial application to do
dependency injection

 Persistence agnostic

```
type GetCustomer = CustomerId -> Customer
```

```
let getCustomerFromDatabase connection  
    (customerId:CustomerId) =  
    // from connection  
    // select customer  
    // where customerId = customerId
```

```
type of getCustomerFromDatabase =  
    DbConnection -> CustomerId -> Customer
```

```
let getCustomer1 = getCustomerFromDatabase myConnection  
  
// getCustomer1 : CustomerId -> Customer
```



```
type GetCustomer = CustomerId -> Customer
```

```
let getCustomerFromMemory map (customerId:CustomerId) =  
    map |> Map.find customerId
```

```
type of getCustomerFromMemory =  
    Map<Id, Customer> -> CustomerId -> Customer
```

```
let getCustomer2 = getCustomerFromMemory inMemoryMap  
  
// getCustomer2 : CustomerId -> Customer
```

Pattern:

The Hollywood principle:
continuations

Continuations

```
int Divide(int top, int bottom)
{
    if (bottom == 0)
    {
        throw new InvalidOperationException("div by 0");
    }
    else
    {
        return top/bottom;
    }
}
```

Method has decided to throw
an exception



Continuations

Let the caller decide what happens

```
void Divide(int top, int bottom,  
            Action ifZero, Action<int> ifSuccess)  
{  
    if (bottom == 0)  
    {  
        ifZero();  
    }  
    else  
    {  
        ifSuccess( top/bottom );  
    }  
}
```

what happens next?

Continuations

F# version

```
let divide ifZero ifSuccess top bottom =  
    if (bottom=0)  
    then ifZero()  
    else ifSuccess (top/bottom)
```

Four parameters is a lot
though!



Continuations

```
let divide ifZero ifSuccess top bottom =  
  if (bottom=0)  
  then ifZero()  
  else ifSuccess (top/bottom)
```

```
let ifZero1 () = printfn "bad"  
let ifSuccess1 x = printfn "good %i" x
```

setup the functions to
print a message

```
let divide1 = divide ifZero1 ifSuccess1
```

```
//test
```

```
let good1 = divide1 6 3
```

```
let bad1 = divide1 6 0
```

Partially apply the
continuations

Use it like a normal function —
only two parameters

Continuations

```
let divide ifZero ifSuccess top bottom =  
  if (bottom=0)  
  then ifZero()  
  else ifSuccess (top/bottom)
```

← setup the functions to
return an Option

```
let ifZero2() = None  
let ifSuccess2 x = Some x
```

```
let divide2 = divide ifZero2 ifSuccess2
```

← Partially apply the
continuations

```
//test  
let good2 = divide2 6 3  
let bad2 = divide2 6 0
```

← Use it like a normal function —
only two parameters

Continuations

```
let divide ifZero ifSuccess top bottom =  
  if (bottom=0)  
  then ifZero()  
  else ifSuccess (top/bottom)
```

← setup the functions to
throw an exception

```
let ifZero3() = failwith "div by 0"  
let ifSuccess3 x = x
```

```
let divide3 = divide ifZero3 ifSuccess3
```

```
//test
```

```
let good3 = divide3 6 3
```

```
let bad3 = divide3 6 0
```

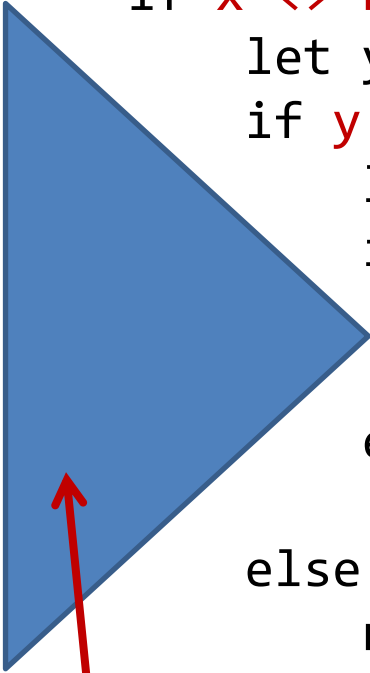
← Partially apply the
continuations

← Use it like a normal function —
only two parameters

MONADS

Pyramid of doom: null testing example

```
let example input =  
  let x = doSomething input  
  if x <> null then  
    let y = doSomethingElse x  
    if y <> null then  
      let z = doAThirdThing y  
      if z <> null then  
        let result = z  
        result  
      else  
        null  
    else  
      null  
  else  
    null
```



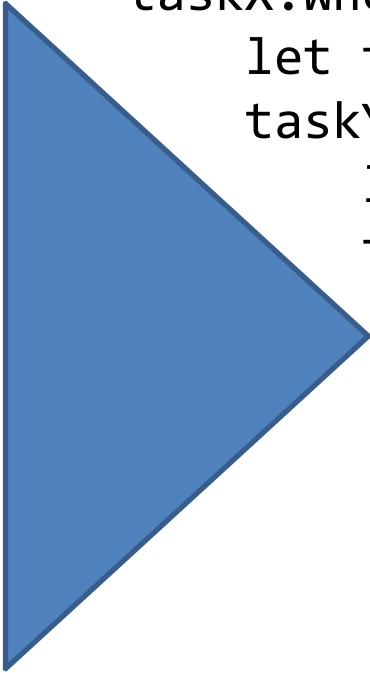
The diagram shows a blue triangle pointing to the right, representing the 'pyramid of doom'. Red arrows point from the text 'Nested null checks' to the three 'if' statements in the code. Another red arrow points from the text 'The pyramid of doom' to the blue triangle.

Nested null
checks

The pyramid
of doom

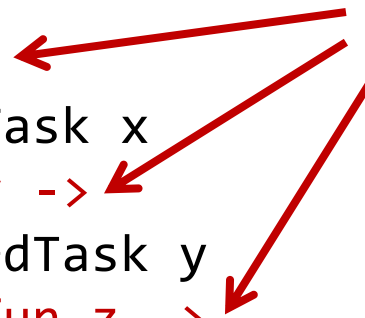
I know you could do early
returns, but bear with me...

Pyramid of doom: async example



```
let taskExample input =  
  let taskX = startTask input  
  taskX.WhenFinished (fun x ->  
    let taskY = startAnotherTask x  
    taskY.WhenFinished (fun y ->  
      let taskZ = startThirdTask y  
      taskZ.WhenFinished (fun z ->  
        z // final result
```

Nested
callbacks



Pyramid of doom: null example

```
let example input =  
  let x = doSomething input  
  if x <> null then  
    let y = doSomethingElse x  
    if y <> null then  
      let z = doAThirdThing y  
      if z <> null then  
        let result = z  
        result  
      else  
        null  
    else  
      null  
  else  
    null
```

Nulls are a code smell:
replace with Option!

Pyramid of doom: option example

```
let example input =  
  let x = doSomething input  
  if x.IsSome then  
    let y = doSomethingElse (x.Value)  
    if y.IsSome then  
      let z = doAThirdThing (y.Value)  
      if z.IsSome then  
        let result = z.Value  
        Some result  
      else  
        None  
    else  
      None  
  else  
    None
```

Much more elegant, yes?

No! This is fugly!
Let's do a cut & paste refactoring

Pyramid of doom: option example

```
let example input =  
  let x = doSomething input  
  if x.IsSome then  
    let y = doSomethingElse (x.Value)  
    if y.IsSome then  
      let z = doAThirdThing (y.Value)  
      if z.IsSome then  
        let result = z.Value  
        Some result  
      else  
        None  
    else  
      None  
  else  
    None
```

Pyramid of doom: option example

```
let doWithX x =  
  let y = doSomethingElse x  
  if y.IsSome then  
    let z = doAThirdThing (y.Value)  
    if z.IsSome then  
      let result = z.Value  
      Some result  
    else  
      None  
  else  
    None
```

```
let example input =  
  let x = doSomething input  
  if x.IsSome then  
    doWithX x  
  else  
    None
```

Pyramid of doom: option example

```
let doWithX x =  
  let y = doSomethingElse x  
  if y.IsSome then  
    let z = doAThirdThing (y.Value)  
    if z.IsSome then  
      let result = z.Value  
      Some result  
    else  
      None  
  else  
    None
```

```
let example input =  
  let x = doSomething input  
  if x.IsSome then  
    doWithX x  
  else  
    None
```


Pyramid of doom: option example

```
let doWithY y =
```

```
  let z = doAThirdThing y
  if z.IsSome then
    let result = z.Value
    Some result
  else
    None
```

```
let doWithX x =
```

```
  let y = doSomethingElse x
  if y.IsSome then
    doWithY y
  else
    None
```

```
let example input =
```

```
  let x = doSomething input
  if x.IsSome then
    doWithX x
  else
    None
```

Pyramid of doom: option example refactored

```
let doWithZ z =  
  let result = z  
  Some result
```

```
let doWithY y =  
  let z = doAThirdThing y  
  if z.IsSome then  
    doWithZ z.Value  
  else  
    None
```

```
let doWithX x =  
  let y = doSomethingElse x  
  if y.IsSome then  
    doWithY y.Value  
  else  
    None
```

```
let optionExample input =  
  let x = doSomething input  
  if x.IsSome then  
    doWithX x.Value  
  else  
    None
```

Three small pyramids instead
of one big one!

This is still ugly!

But the code has a pattern...

Pyramid of doom: option example refactored

```
let doWithZ z =  
  let result = z  
  Some result
```

```
let doWithY y =  
  let z = doAThirdThing y  
  if z.IsSome then  
    doWithZ z.Value  
  else  
    None
```

```
let doWithX x =  
  let y = doSomethingElse x  
  if y.IsSome then  
    doWithY y.Value  
  else  
    None
```

```
let optionExample input =  
  let x = doSomething input  
  if x.IsSome then  
    doWithX x.Value  
  else  
    None
```

But the code has a pattern...

```
let doWithY y =  
  let z = doAThirdThing y  
  if z.IsSome then  
    doWithZ z.Value  
  else  
    None
```



*Crying out to be
parameterized!*

```
let ifSomeDo f x =  
    if x.IsSome then  
        f x.Value  
    else  
        None
```

```
let doWithY y =  
    let z = doAThirdThing y  
    z |> ifSomeDo doWithZ
```

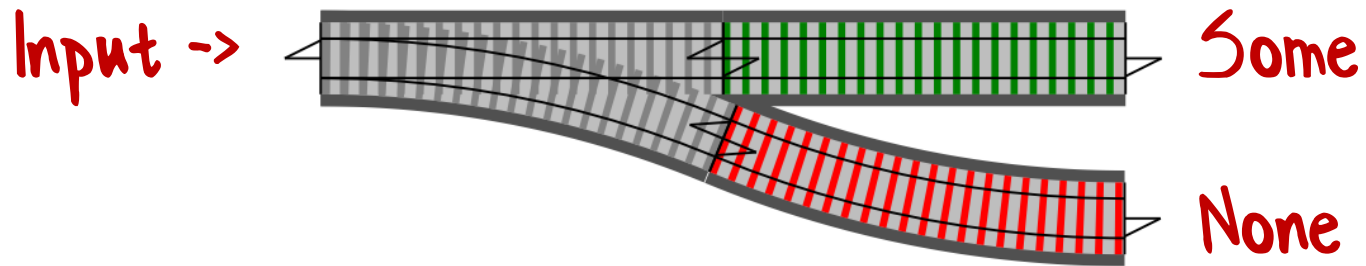
```
let ifSomeDo f x =  
    if x.IsSome then  
        f x.Value  
    else  
        None
```

```
let doWithY y =  
    y  
    |> doAThirdThing  
    |> ifSomeDo doWithZ
```

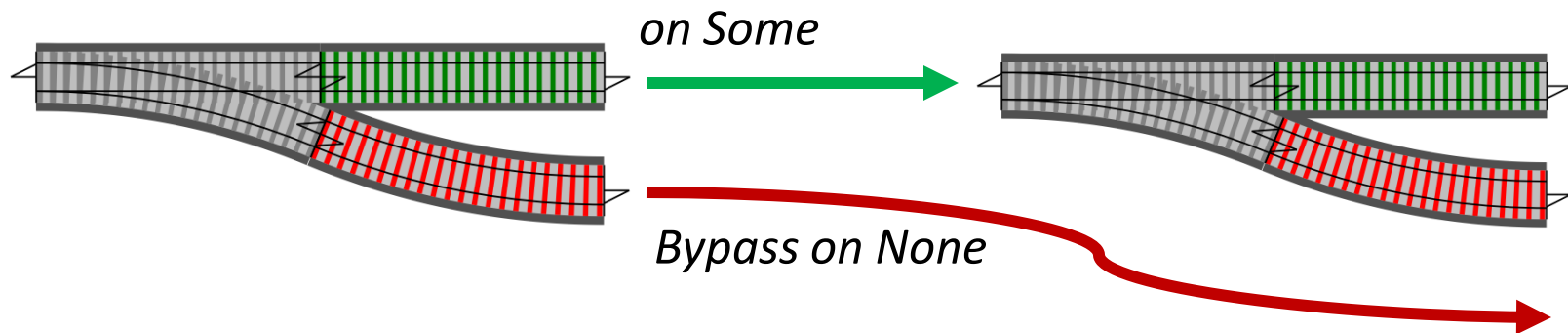
```
let ifSomeDo f x =  
    if x.IsSome then  
        f x.Value  
    else  
        None
```

```
let example input =  
    doSomething input  
    |> ifSomeDo doSomethingElse  
    |> ifSomeDo doAThirdThing  
    |> ifSomeDo (fun z -> Some z)
```

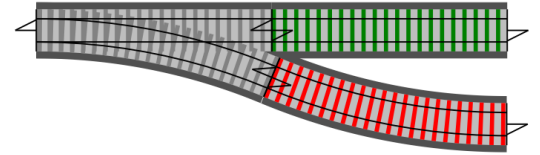
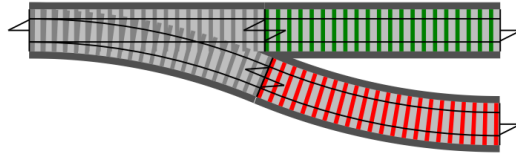
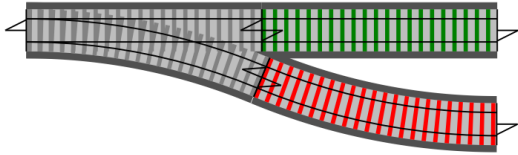
A switch analogy



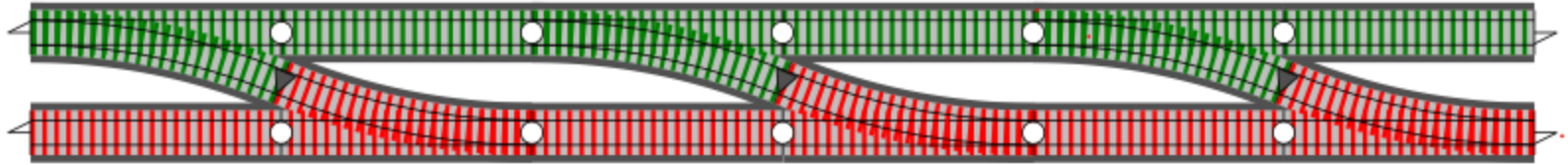
Connecting switches



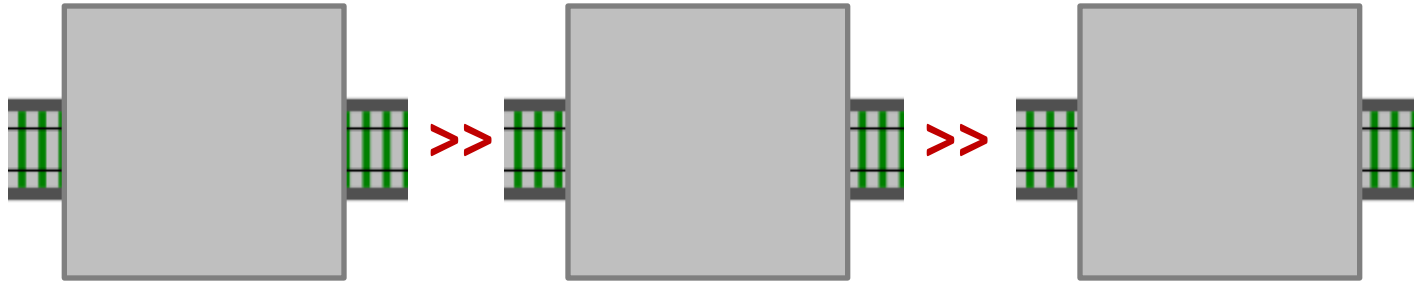
Connecting switches



Connecting switches

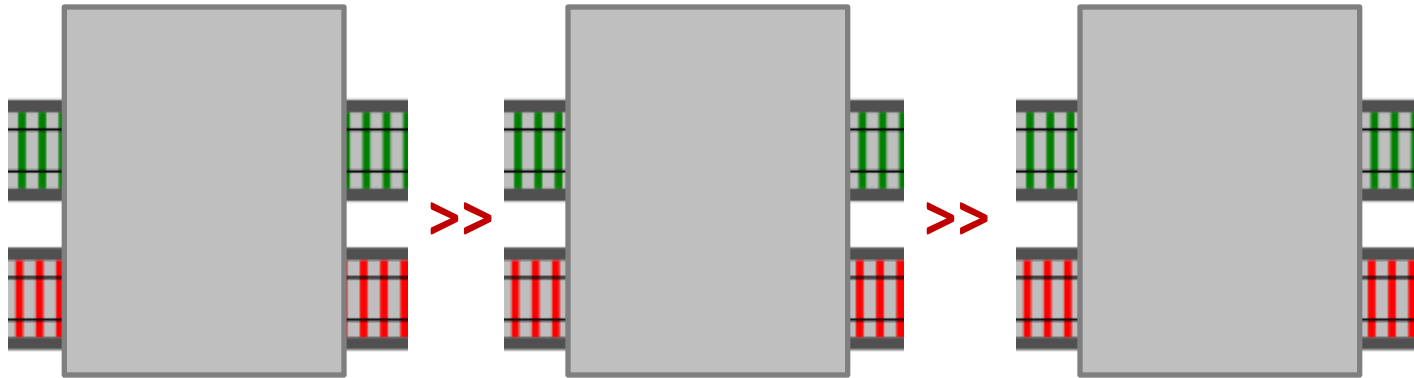


Composing switches



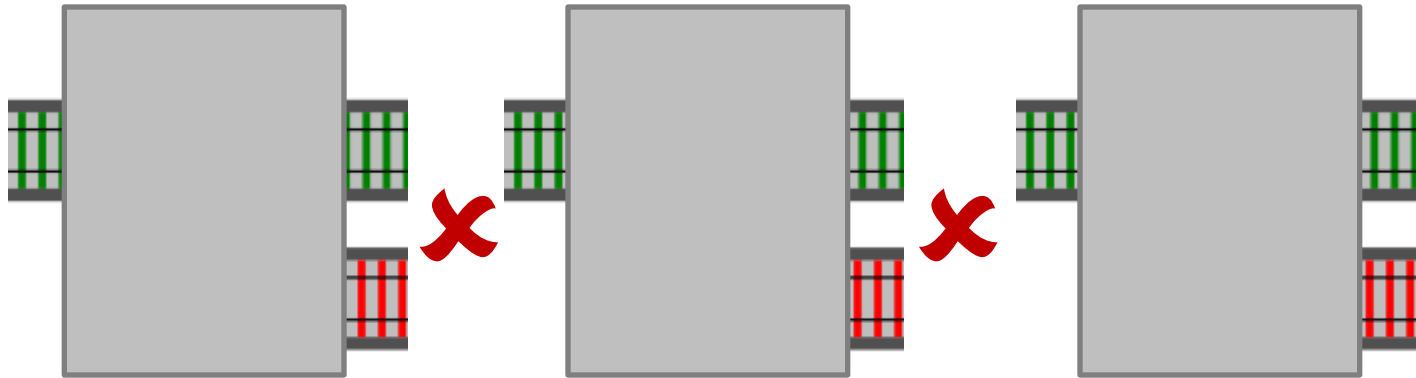
Composing one-track functions is fine...

Composing switches



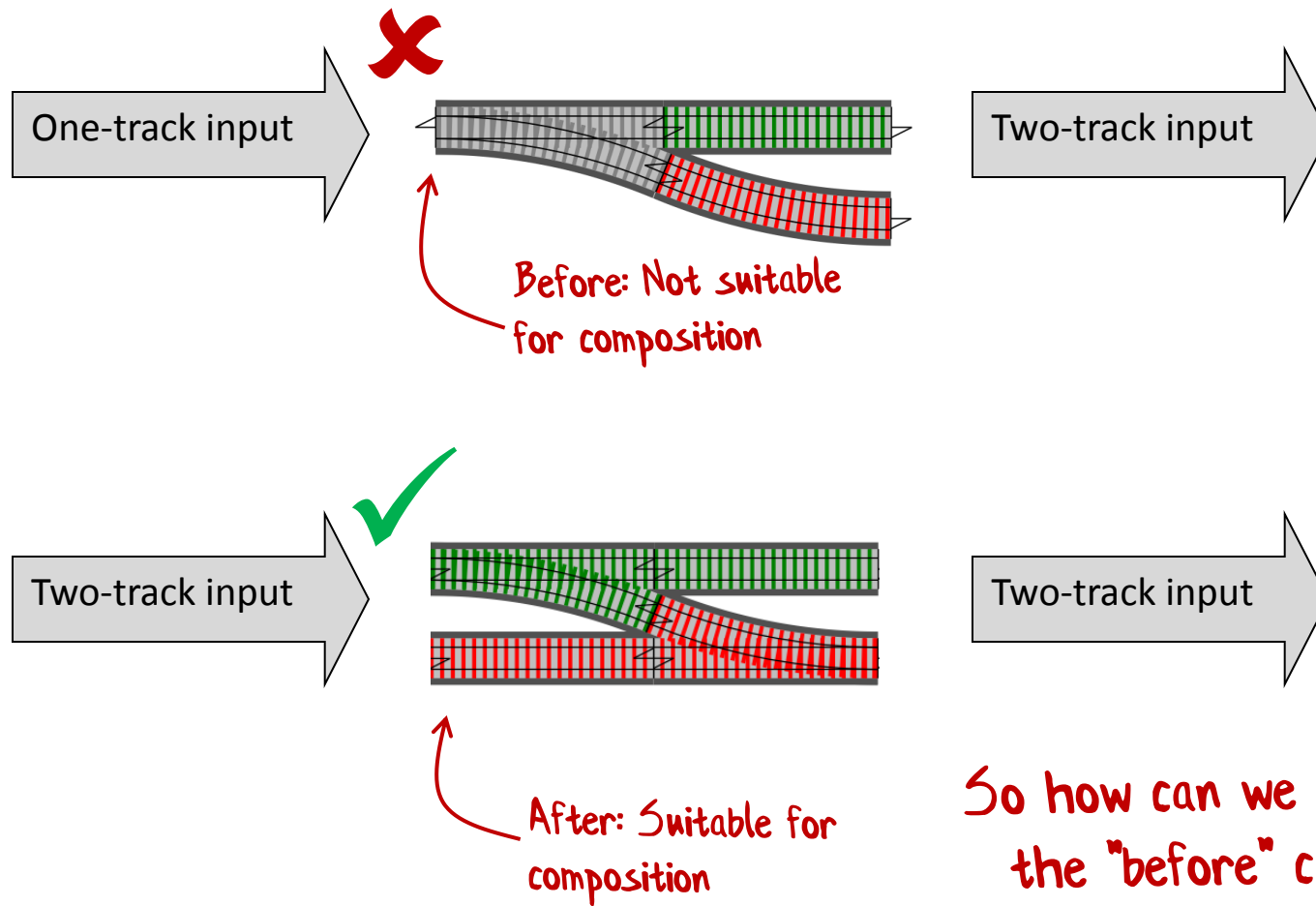
... and composing two-track functions is fine...

Composing switches



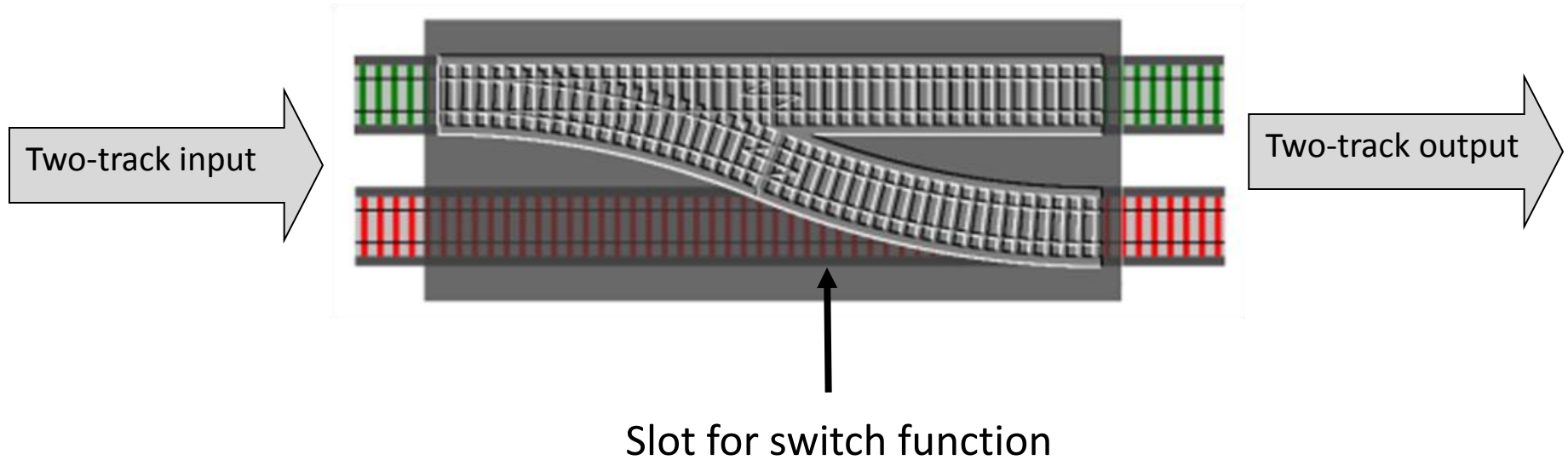
... but composing switches is not allowed!

Composing switches

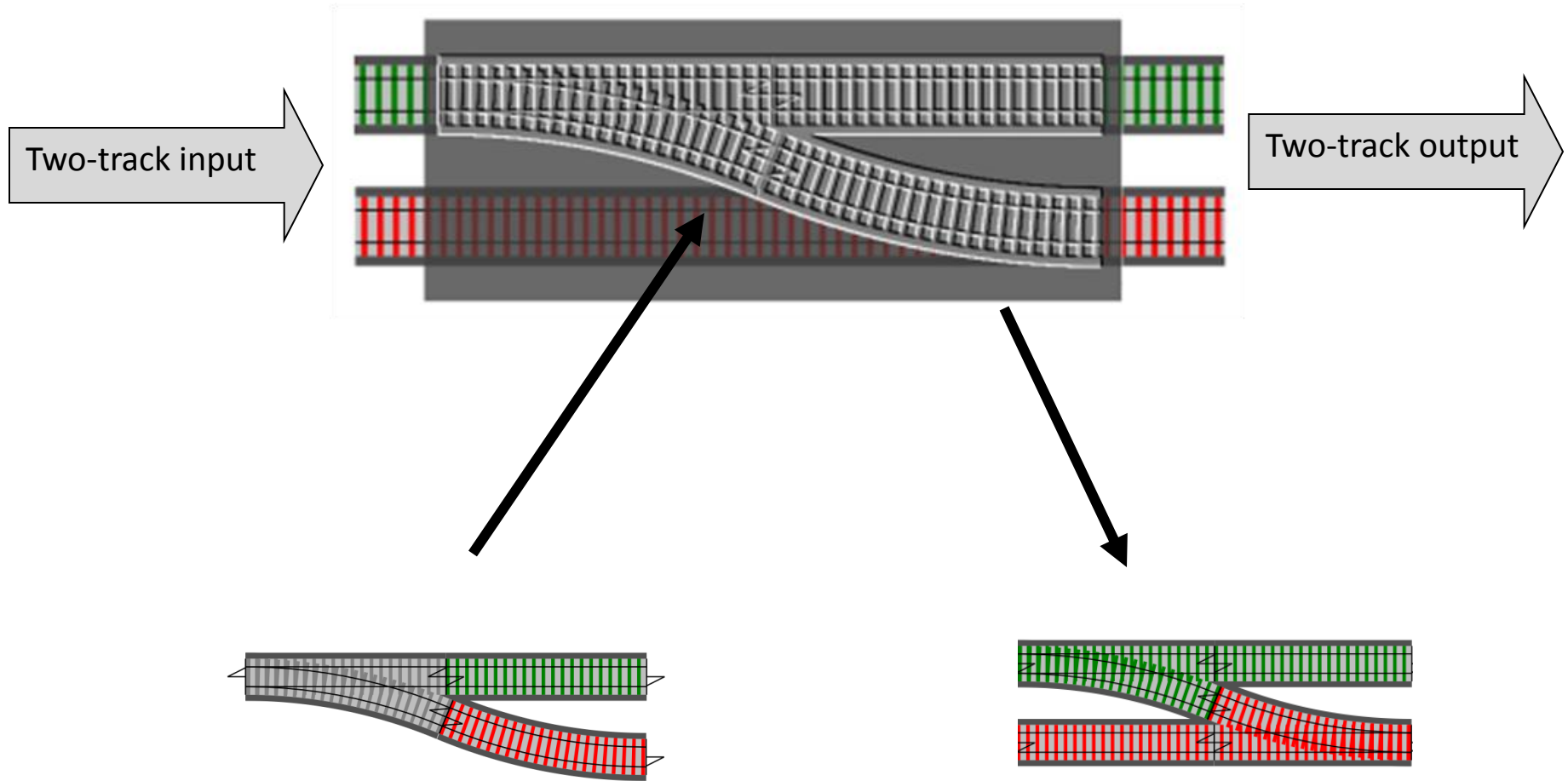


So how can we convert from the "before" case to the "after" case?

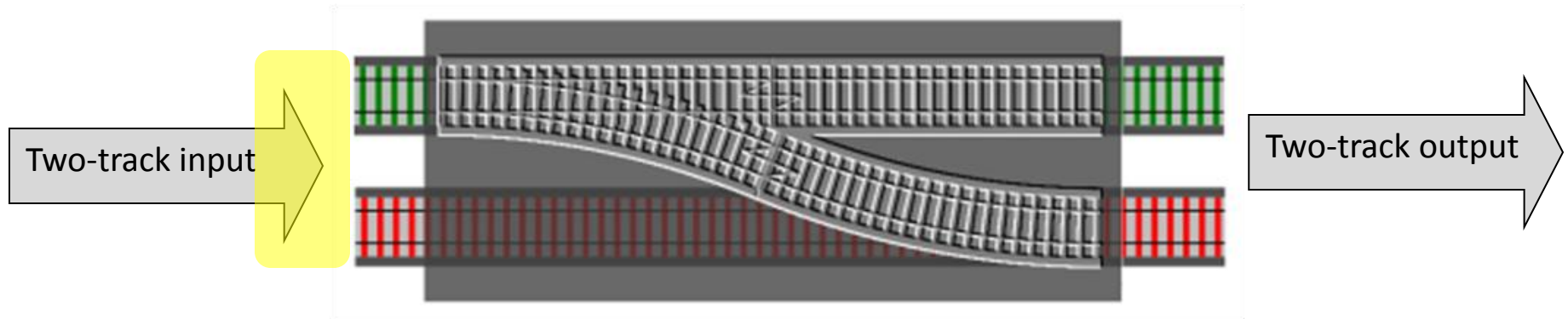
Building an adapter block



Building an adapter block

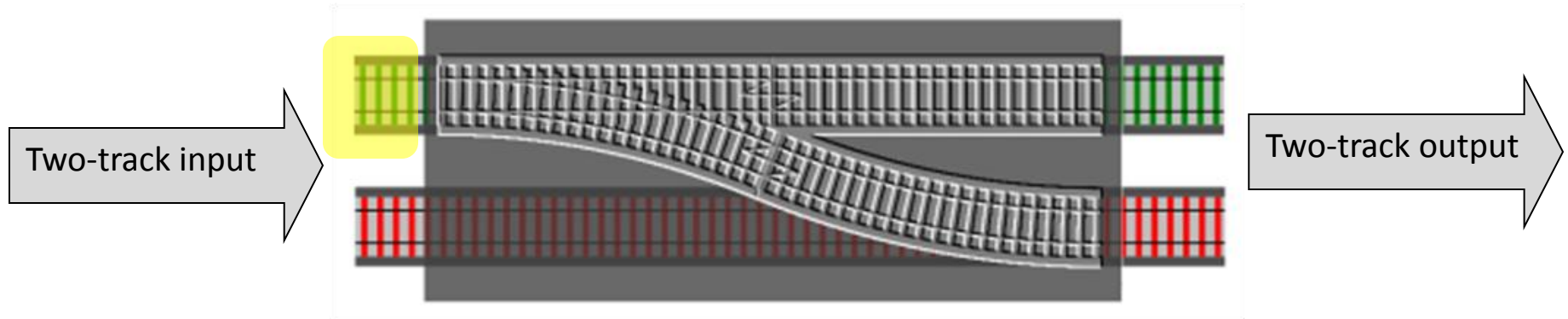


Building an adapter block



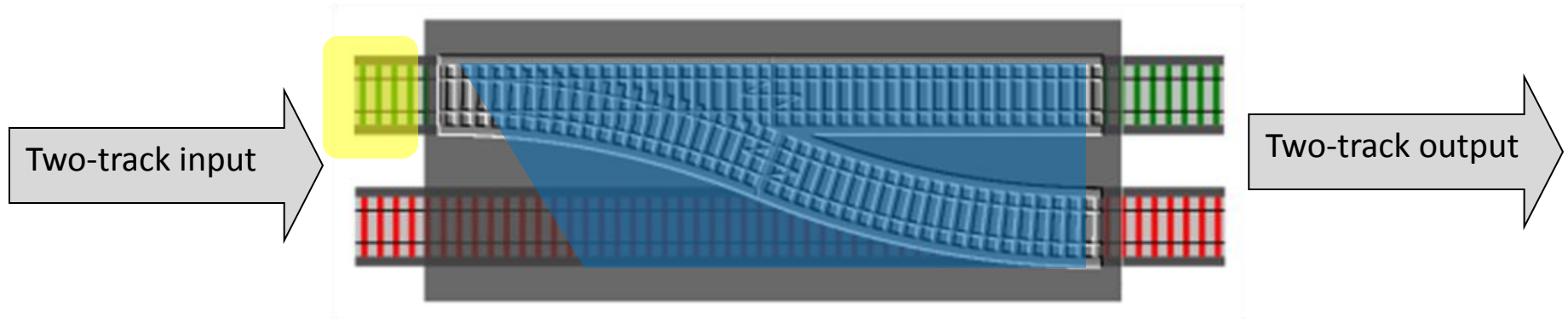
```
let bind nextFunction optionInput =  
  match optionInput with  
  | Some s -> nextFunction s  
  | None -> None
```

Building an adapter block



```
let bind nextFunction optionInput =  
  match optionInput with  
  | Some s -> nextFunction s  
  | None -> None
```

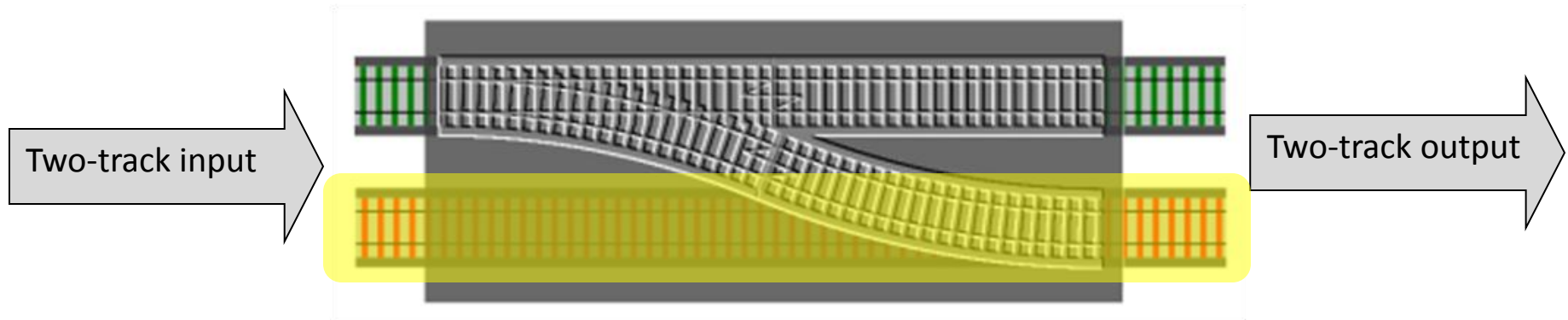
Building an adapter block



```
let bind nextFunction optionInput =  
  match optionInput with  
  | Some s -> nextFunction s  
  | None -> None
```

*This is a
continuation*

Building an adapter block



```
let bind nextFunction optionInput =  
  match optionInput with  
  | Some s -> nextFunction s  
  | None -> None
```

Pattern:

Use bind to chain options

Pyramid of doom: using bind

```
let bind f opt =  
  match opt with  
  | Some v -> f v  
  | None -> None  
  
let example input =  
  let x = doSomething input  
  if x.IsSome then  
    let y = doSomethingElse (x.Value)  
    if y.IsSome then  
      let z = doAThirdThing (y.Value)  
      if z.IsSome then  
        let result = z.Value  
        Some result  
      else  
        None  
    else  
      None  
  else  
    None
```

Pyramid of doom: using bind

```
let bind f opt =  
  match opt with  
  | Some v -> f v  
  | None -> None  
  
let example input =  
  doSomething input  
  |> bind doSomethingElse  
  |> bind doAThirdThing  
  |> bind (fun z -> Some z)
```

No pyramids!

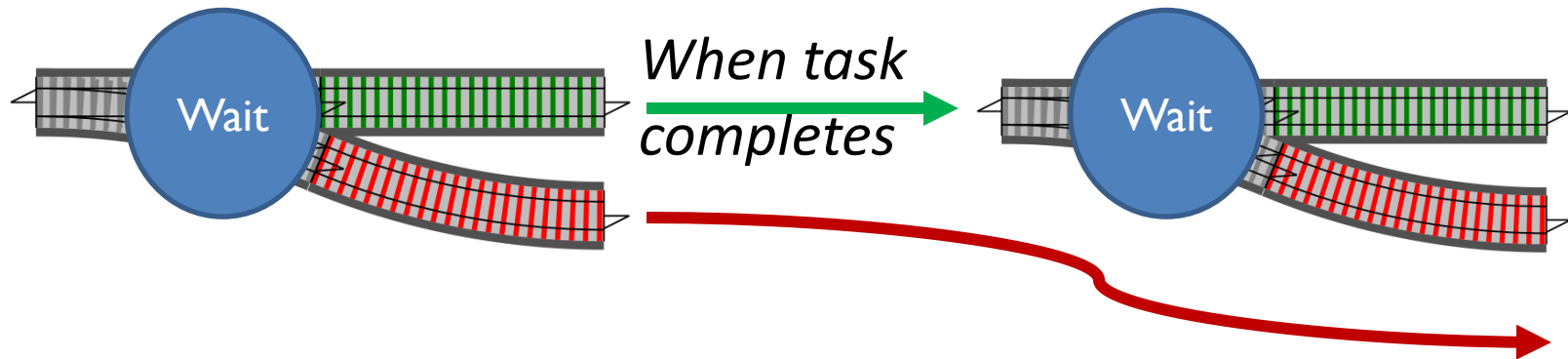
Code is linear and clear.

This pattern is called “monadic bind”

Pattern:

Use bind to chain tasks

Connecting tasks



Pyramid of doom: using bind for tasks

```
let taskBind f task =  
    task.WhenFinished (fun taskResult ->  
        f taskResult)
```

a.k.a “promise” “future”

```
let taskExample input =  
    startTask input  
    |> taskBind startAnotherTask  
    |> taskBind startThirdTask  
    |> taskBind (fun z -> z)
```

This pattern is also a “monadic bind”

Computation expressions

```
let example input =  
  maybe {  
    let! x = doSomething input  
    let! y = doSomethingElse x  
    let! z = doAThirdThing y  
    return z  
  }
```

← Computation expression

```
let taskExample input =  
  task {  
    let! x = startTask input  
    let! y = startAnotherTask x  
    let! z = startThirdTask z  
    return z  
  }
```

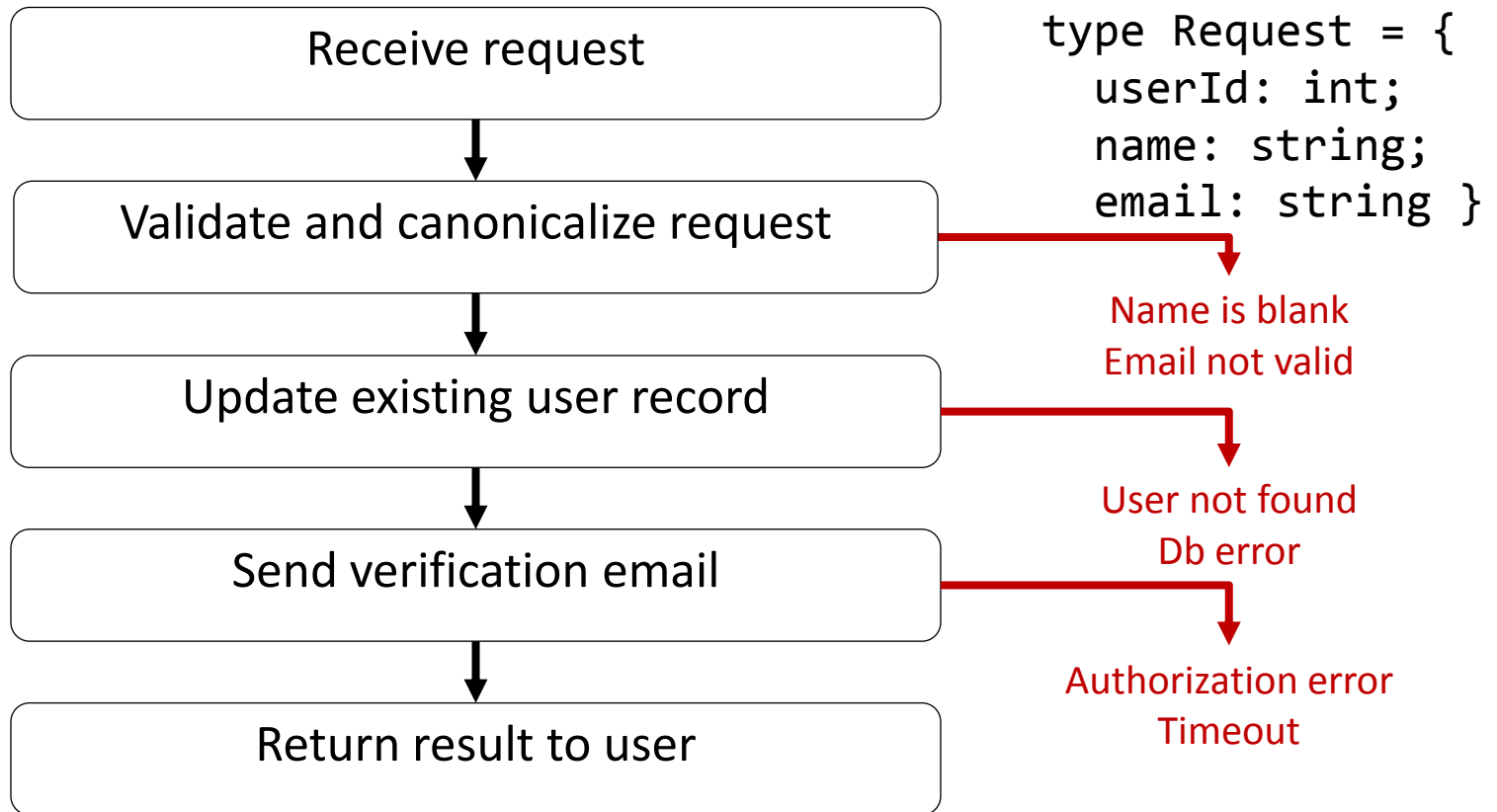
← Computation expression

Pattern:

Use bind to chain error handlers

Example use case

"As a user I want to update my name and email address"
- and see sensible error messages when something goes wrong!



Use case without error handling

```
string UpdateCustomerWithErrorHandling()  
{  
    var request = receiveRequest();  
    validateRequest(request);  
    canonicalizeEmail(request);  
    db.updateDbFromRequest(request);  
    smtpServer.sendEmail(request.Email)  
  
    return "OK";  
}
```

Use case with error handling

```
string UpdateCustomerWithErrorHandling()
{
    var request = receiveRequest();
    var isValidated = validateRequest(request);
    if (!isValidated) {
        return "Request is not valid"
    }
    canonicalizeEmail(request);
    db.updateDbFromRequest(request);
    smtpServer.sendEmail(request.Email)

    return "OK";
}
```


Use case with error handling

```
string UpdateCustomerWithErrorHandling()
{
    var request = receiveRequest();
    var isValidated = validateRequest(request);
    if (!isValidated) {
        return "Request is not valid"
    }
    canonicalizeEmail(request);
    var result = db.updateDbFromRequest(request);
    if (!result) {
        return "Customer record not found"
    }

    smtpServer.sendEmail(request.Email)

    return "OK";
}
```

Use case with error handling

```
string UpdateCustomerWithErrorHandling()
{
    var request = receiveRequest();
    var isValidated = validateRequest(request);
    if (!isValidated) {
        return "Request is not valid"
    }
    canonicalizeEmail(request);
    try {
        var result = db.updateDbFromRequest(request);
        if (!result) {
            return "Customer record not found"
        }
    } catch {
        return "DB error: Customer record not updated"
    }

    smtpServer.sendEmail(request.Email)

    return "OK";
}
```

Use case with error handling

```
string UpdateCustomerWithErrorHandling()
{
    var request = receiveRequest();
    var isValidated = validateRequest(request);
    if (!isValidated) {
        return "Request is not valid"
    }
    canonicalizeEmail(request);
    try {
        var result = db.updateDbFromRequest(request);
        if (!result) {
            return "Customer record not found"
        }
    } catch {
        return "DB error: Customer record not updated"
    }

    if (!smtpServer.sendEmail(request.Email)) {
        log.Error "Customer email not sent"
    }

    return "OK";
}
```

Use case with error handling

```
string UpdateCustomerWithErrorHandling()
{
    var request = receiveRequest();
    var isValidated = validateRequest(request);
    if (!isValidated) {
        return "Request is not valid"
    }
    canonicalizeEmail(request);
    try {
        var result = db.updateDbFromRequest(request);
        if (!result) {
            return "Customer record not found"
        }
    } catch {
        return "DB error: Customer record not updated"
    }

    if (!smtpServer.sendEmail(request.Email)) {
        log.Error "Customer email not sent"
    }

    return "OK";
}
```

↳ clean lines -> 18 ugly lines. 200% extra!
Sadly this is typical of error handling code.

A structure for managing errors

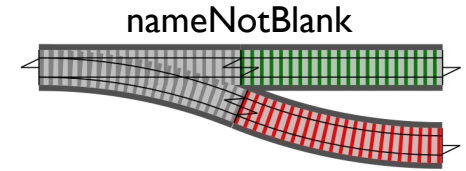
```
type TwoTrack<'TEntity> =  
  | Success of 'TEntity  
  | Failure of string
```



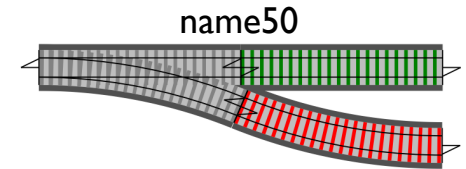
```
let validateInput input =  
  if input.name = "" then  
    Failure "Name must not be blank"  
  else if input.email = "" then  
    Failure "Email must not be blank"  
  else  
    Success input // happy path
```

Bind example

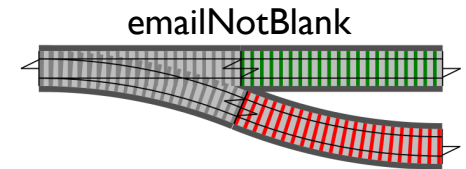
```
let nameNotBlank input =  
  if input.name = "" then  
    Failure "Name must not be blank"  
  else Success input
```



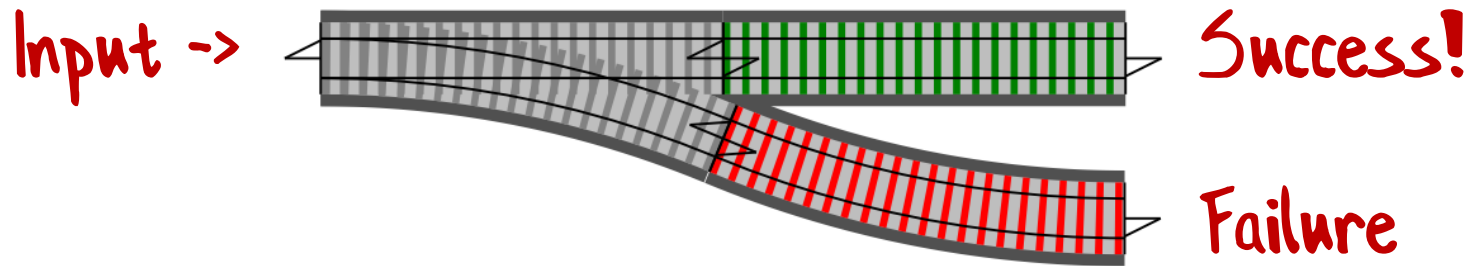
```
let name50 input =  
  if input.name.Length > 50 then  
    Failure "Name must not be longer than 50 chars"  
  else Success input
```



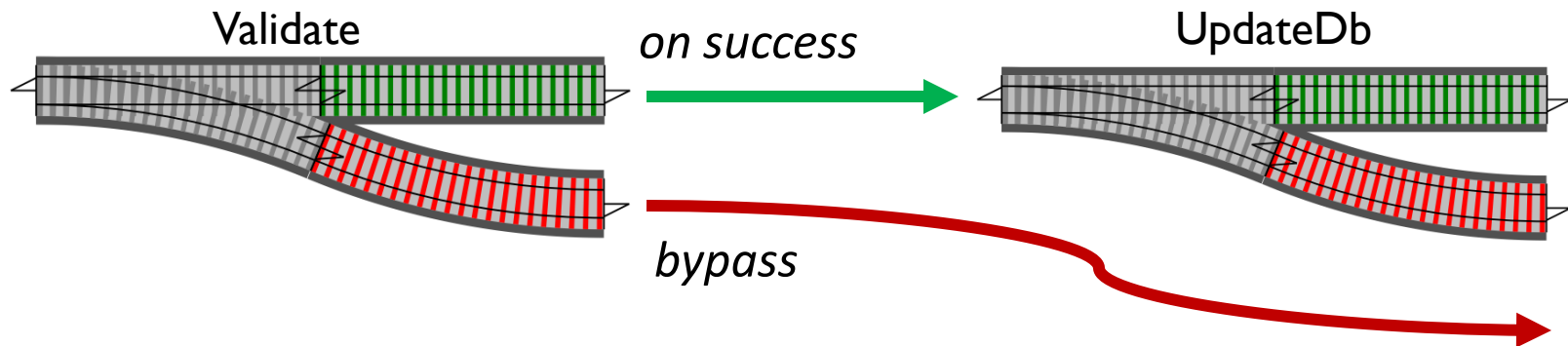
```
let emailNotBlank input =  
  if input.email = "" then  
    Failure "Email must not be blank"  
  else Success input
```



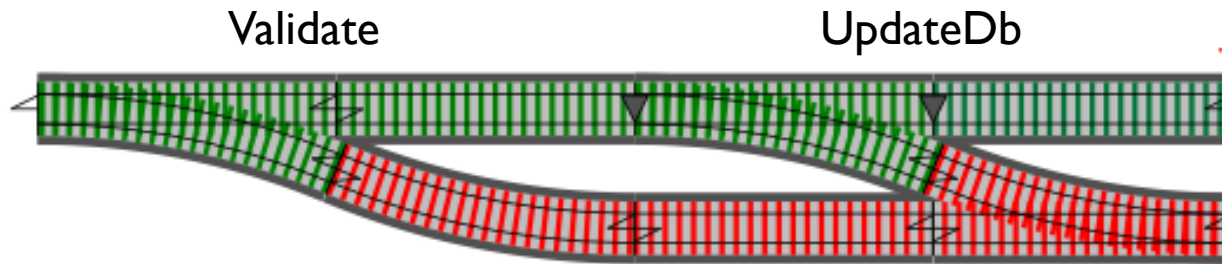
Switches again



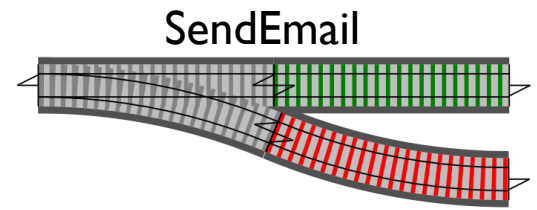
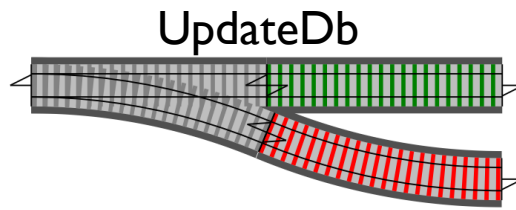
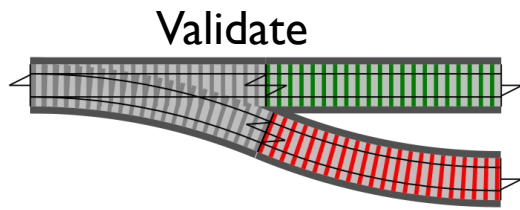
Connecting switches



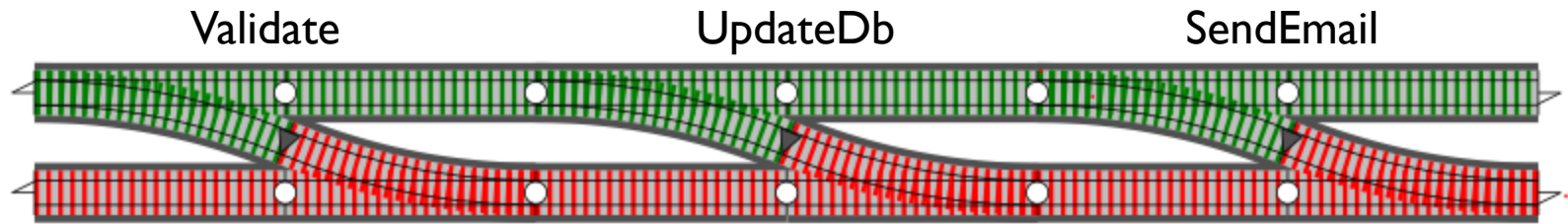
Connecting switches



Connecting switches



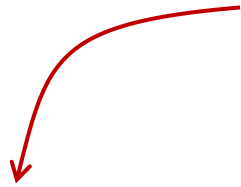
Connecting switches



This is the "two track" model –
the basis for the "Railway Oriented Programming"
approach to error handling.

Functional flow without error handling

Before



```
let updateCustomer =  
  receiveRequest  
  |> validateRequest  
  |> canonicalizeEmail  
  |> updateDbFromRequest  
  |> sendEmail  
  |> returnMessage
```

One track



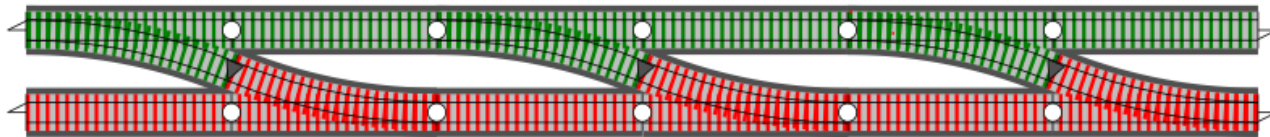
Functional flow with error handling

After



```
let updateCustomerWithErrorHandling =  
  receiveRequest  
  |> validateRequest  
  |> canonicalizeEmail  
  |> updateDbFromRequest  
  |> sendEmail  
  |> returnMessage
```

Two track



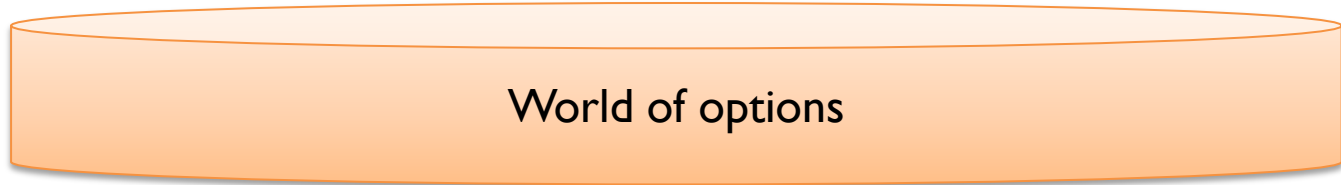
See fsharpforfunandprofit.com/rop

MAPS AND APPLICATIVES

`int option`

`string option`

`bool option`

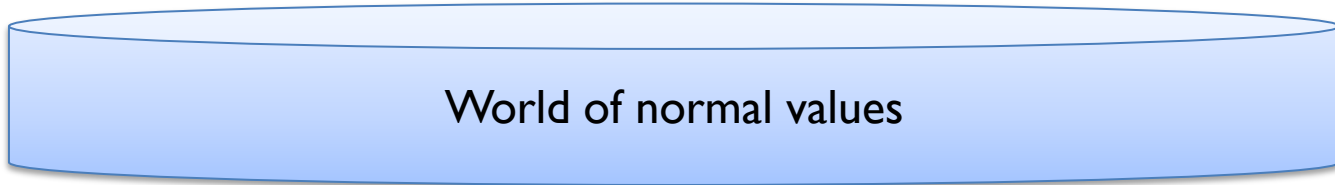


World of options

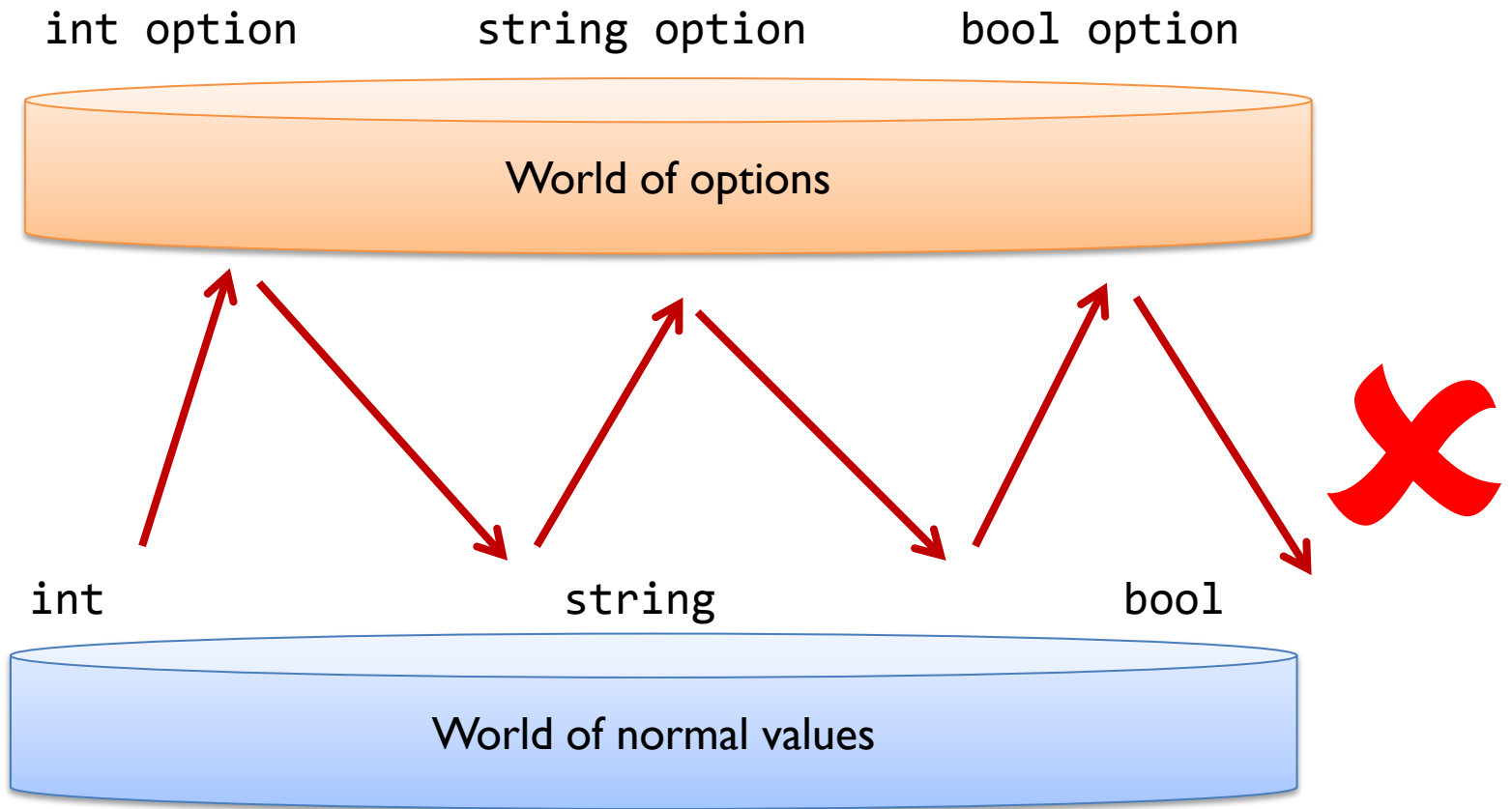
`int`

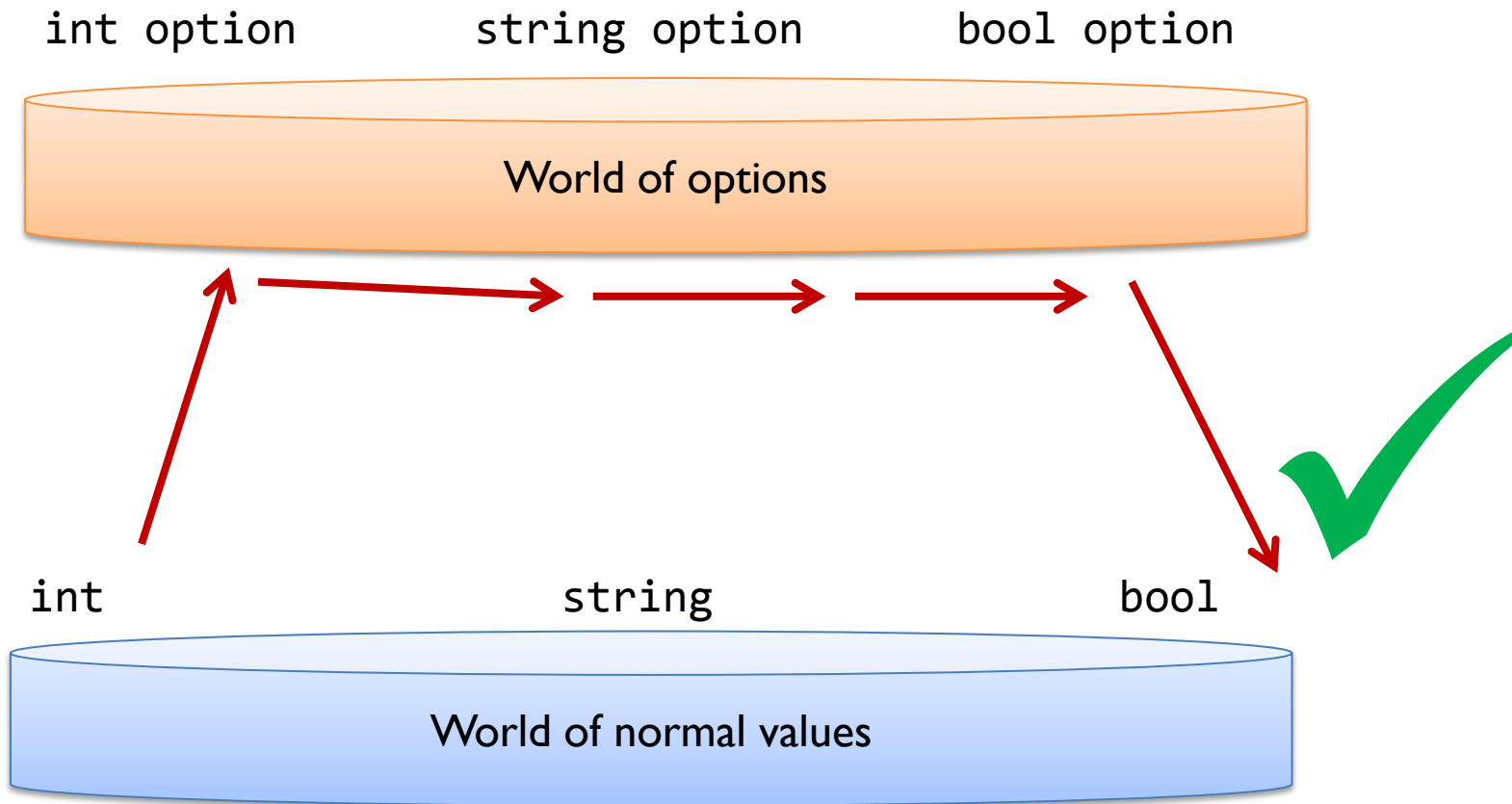
`string`

`bool`



World of normal values





How not to code with options

Let's say you have an int wrapped in an Option, and you want to add 42 to it:

```
let add42 x = x + 42
```

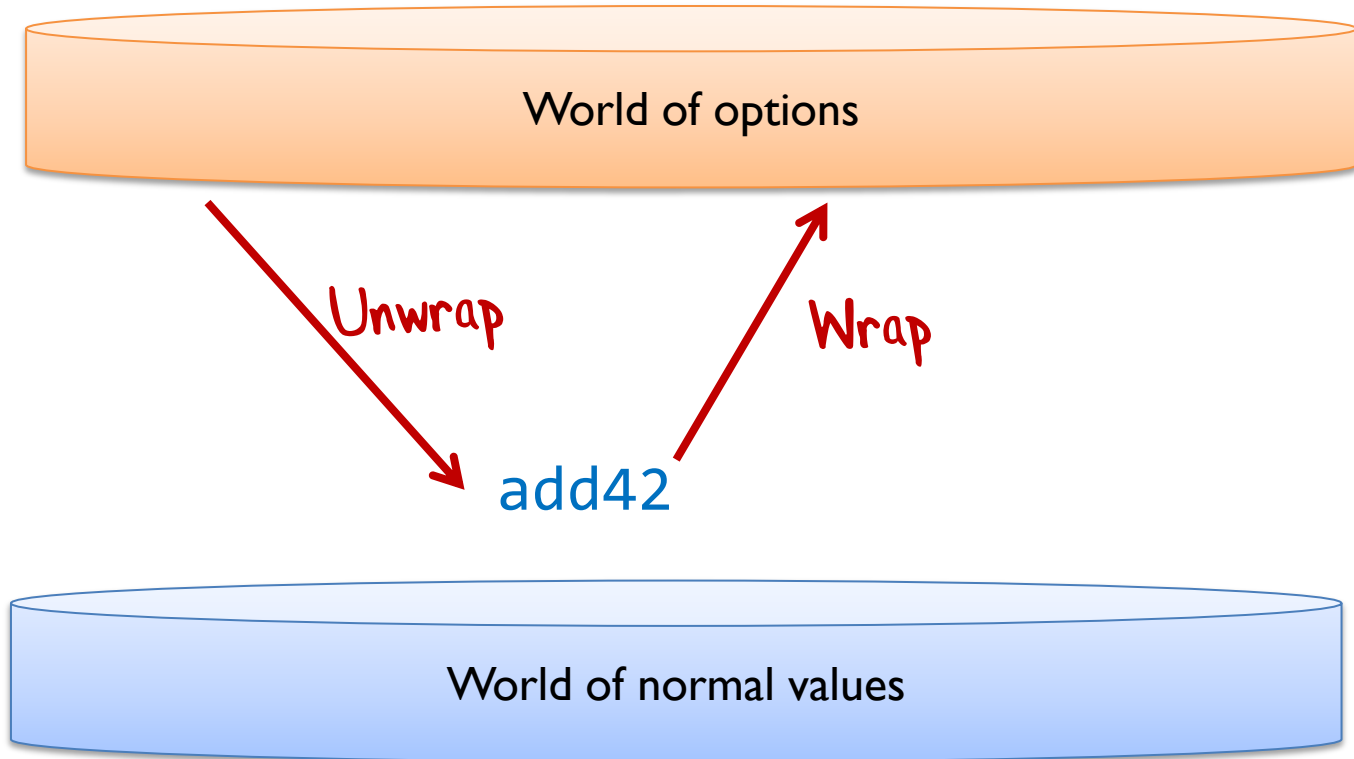
← Works on normal values

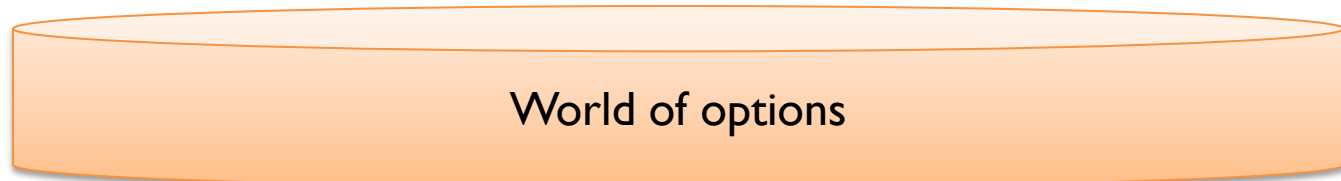
```
let add42ToOption opt =  
  if opt.IsSome then  
    let newVal = add42 opt.Value  
    Some newVal  
  else  
    None
```

← Unwrap

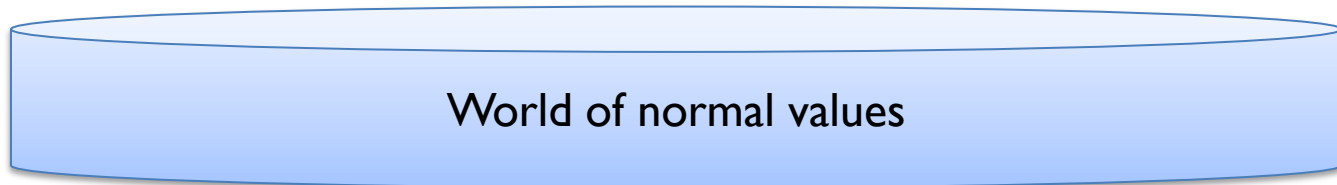
← Wrap again



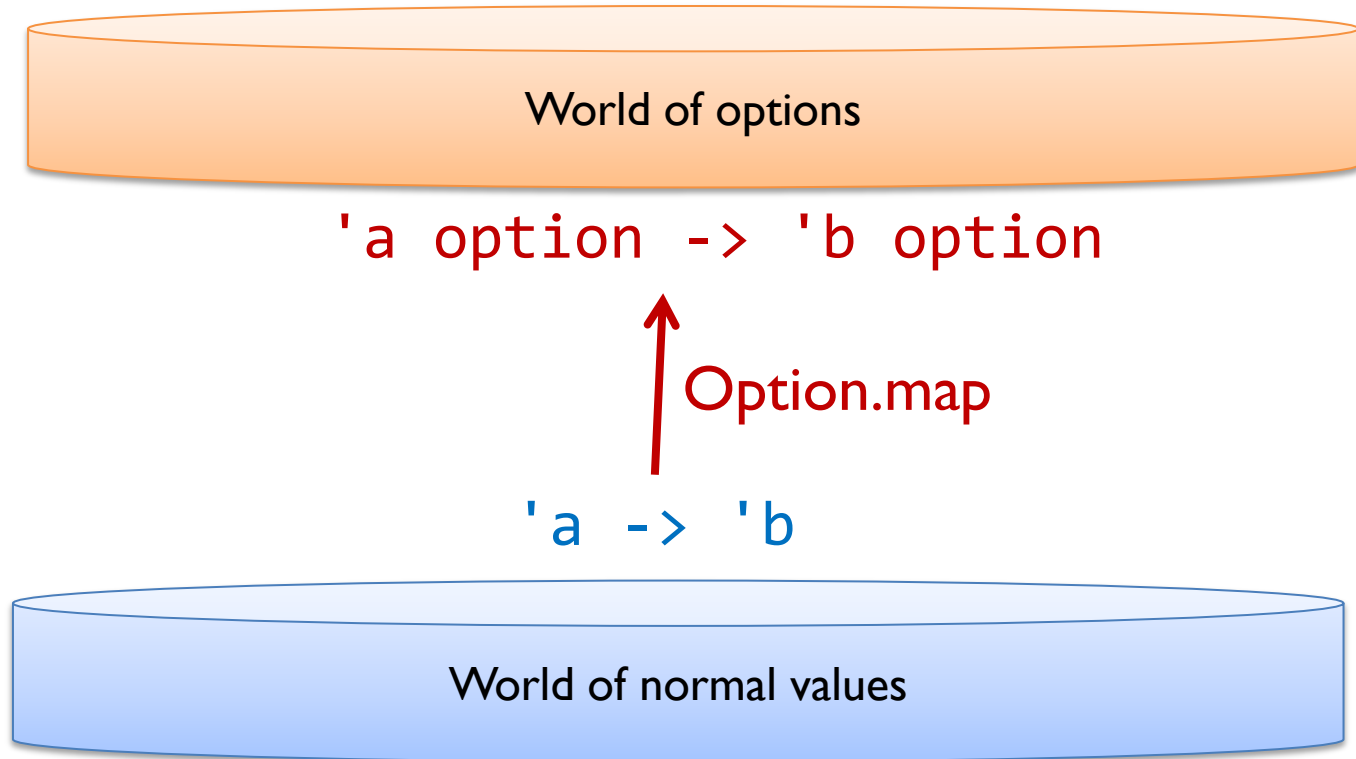




But how?



Lifting



The right way to code with options

Let's say you have an int wrapped in an Option, and you want to add 42 to it:

```
let add42 x = x + 42
```

```
let add42ToOption = Option.map add42  
Some 1 |> add42ToOption
```



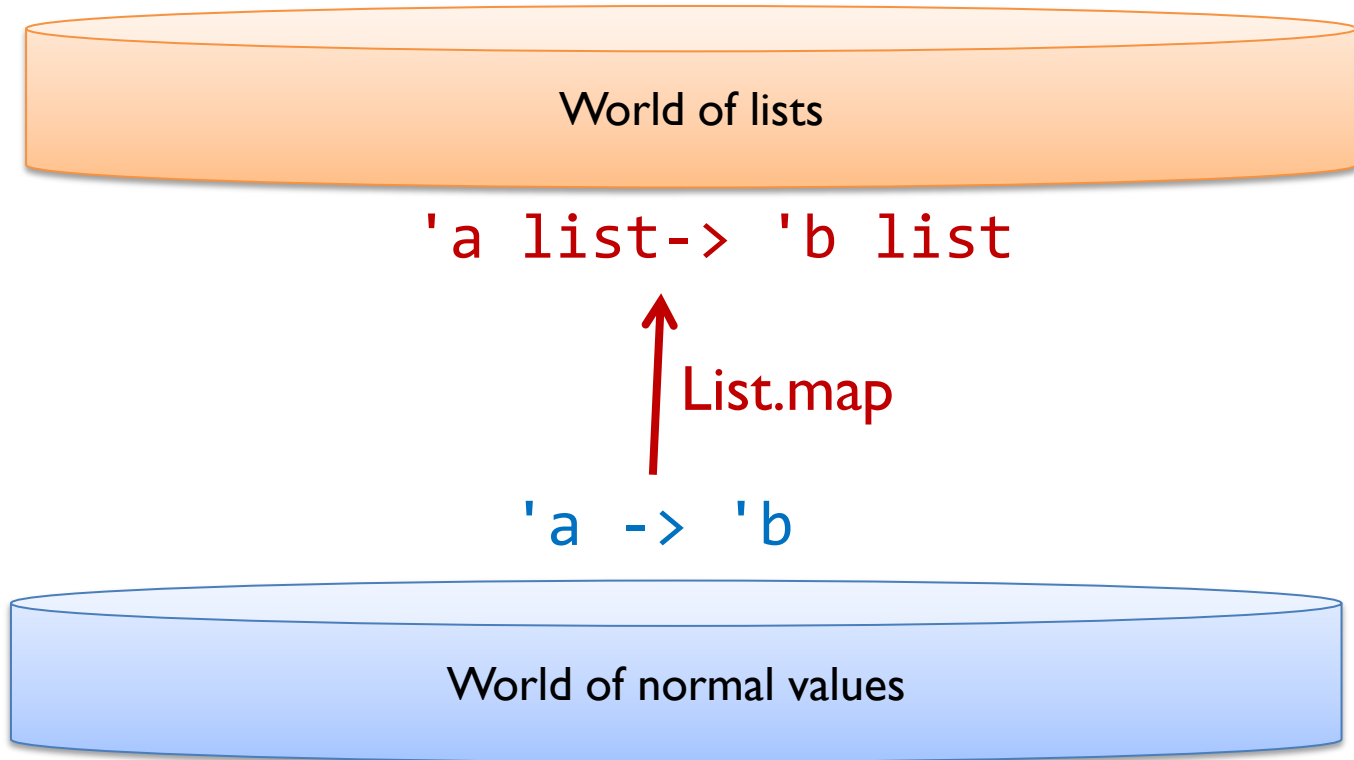
```
Some 1 |> Option.map add42
```

*Often no need to bother
creating a temp function*

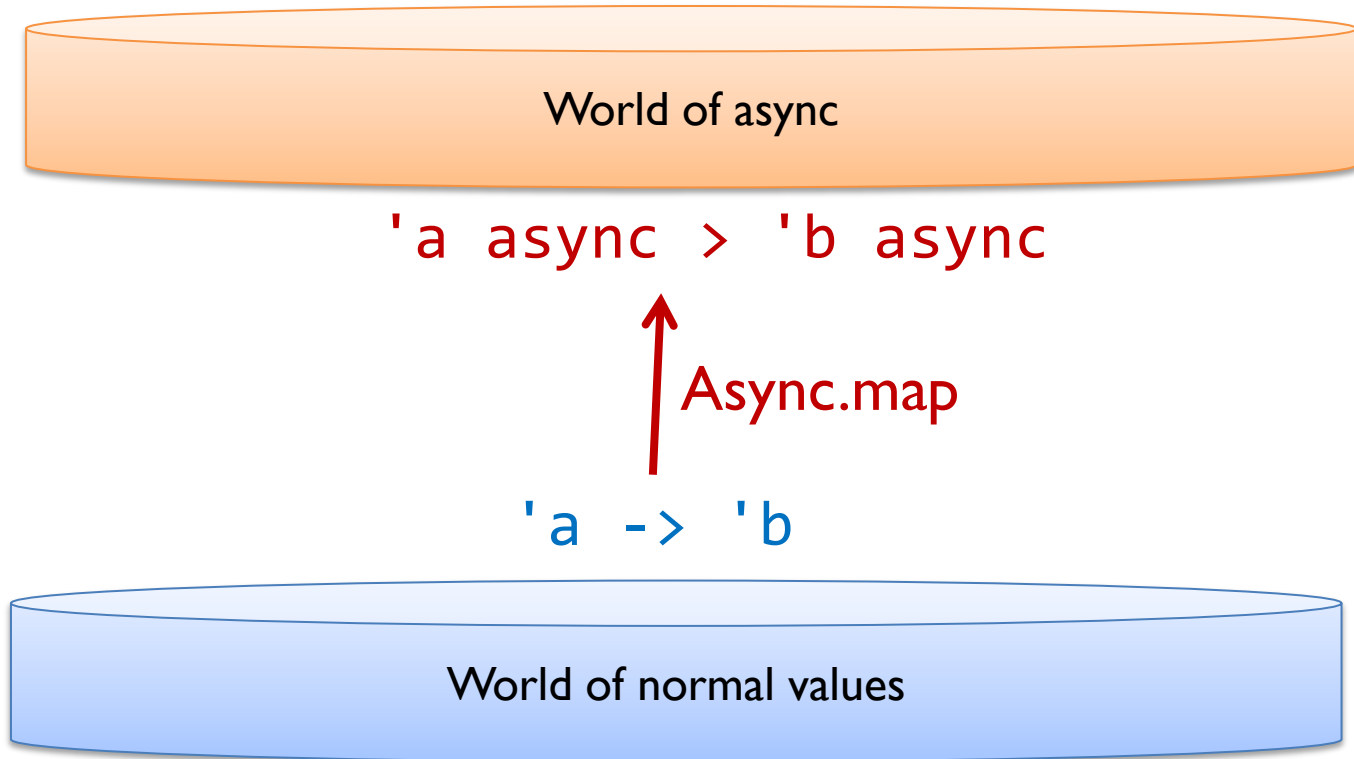
Pattern:

Use “map” to lift functions

Lifting to lists



Lifting to async



The right way to code with wrapped types

Most wrapped types provide a “map”

```
let add42 x = x + 42
```

```
Some 1 |> Option.map add42
```

```
[1;2;3] |> List.map add42
```

Guideline:

If you create a wrapped generic type, create a “map” for it.

Terminology alert:
Mappable types are “functors”

Maps

```
type TwoTrack<'TEntity> =  
  | Success of 'TEntity  
  | Failure of string
```

My Map!

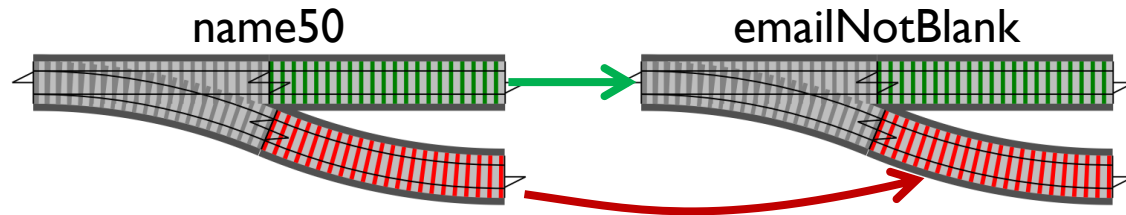


```
let mapTT f x =  
  match x with  
  | Success entity -> Success (f entity)  
  | Failure s -> Failure s
```

Tip:
Use applicatives for validation

What's an applicative?

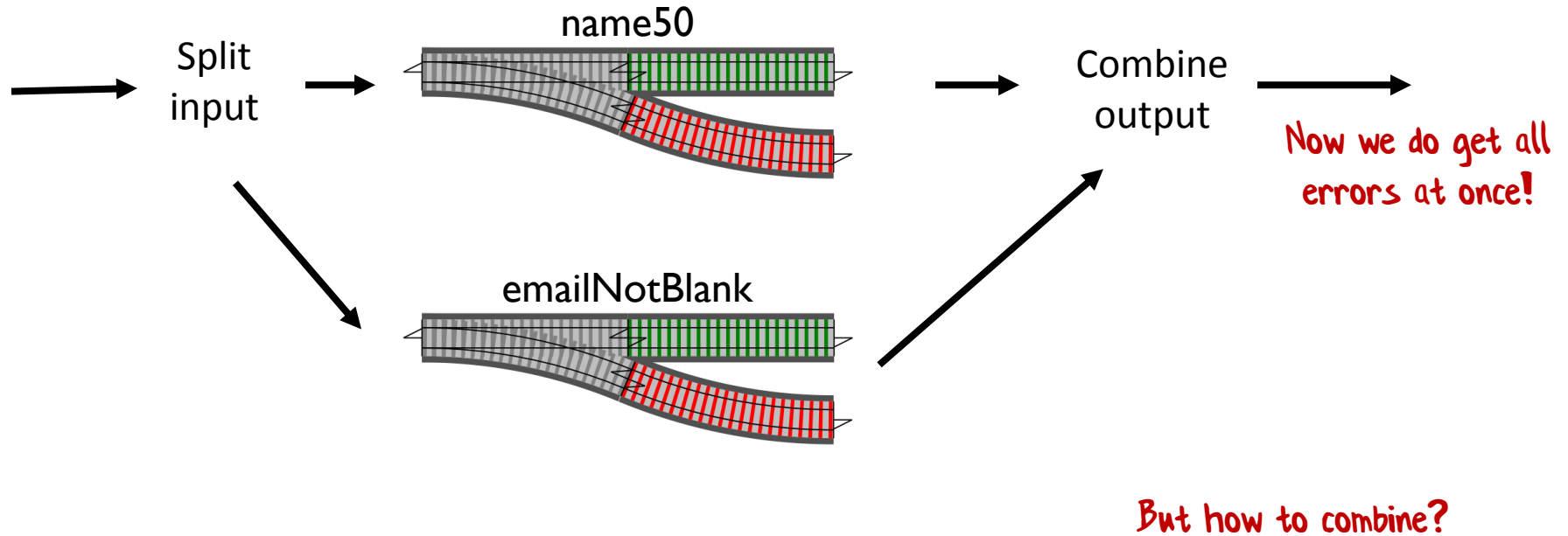
Series validation



Problem: Validation done in series.
So only one error at a time is returned

It would be nice to return all
validation errors at once.

Parallel validation



Creating a valid data structure

Domain object

```
type Request= {  
    UserId: UserId;  
    Name: String50;  
    Email: EmailAddress}
```

These are "pure"

Object from the outside

```
type RequestDTO= {  
    UserId: int;  
    Name: string;  
    Email: string}
```

These need validation

How not to do validation

```
// do the validation of the DTO
let userIdOrError = validateUserId dto.userId
let nameOrError = validateName dto.name
let emailOrError = validateEmail dto.email
```

```
if userIdOrError.IsSuccess
  && nameOrError.IsSuccess
  && emailOrError.IsSuccess then
```

No no no this is horrible!

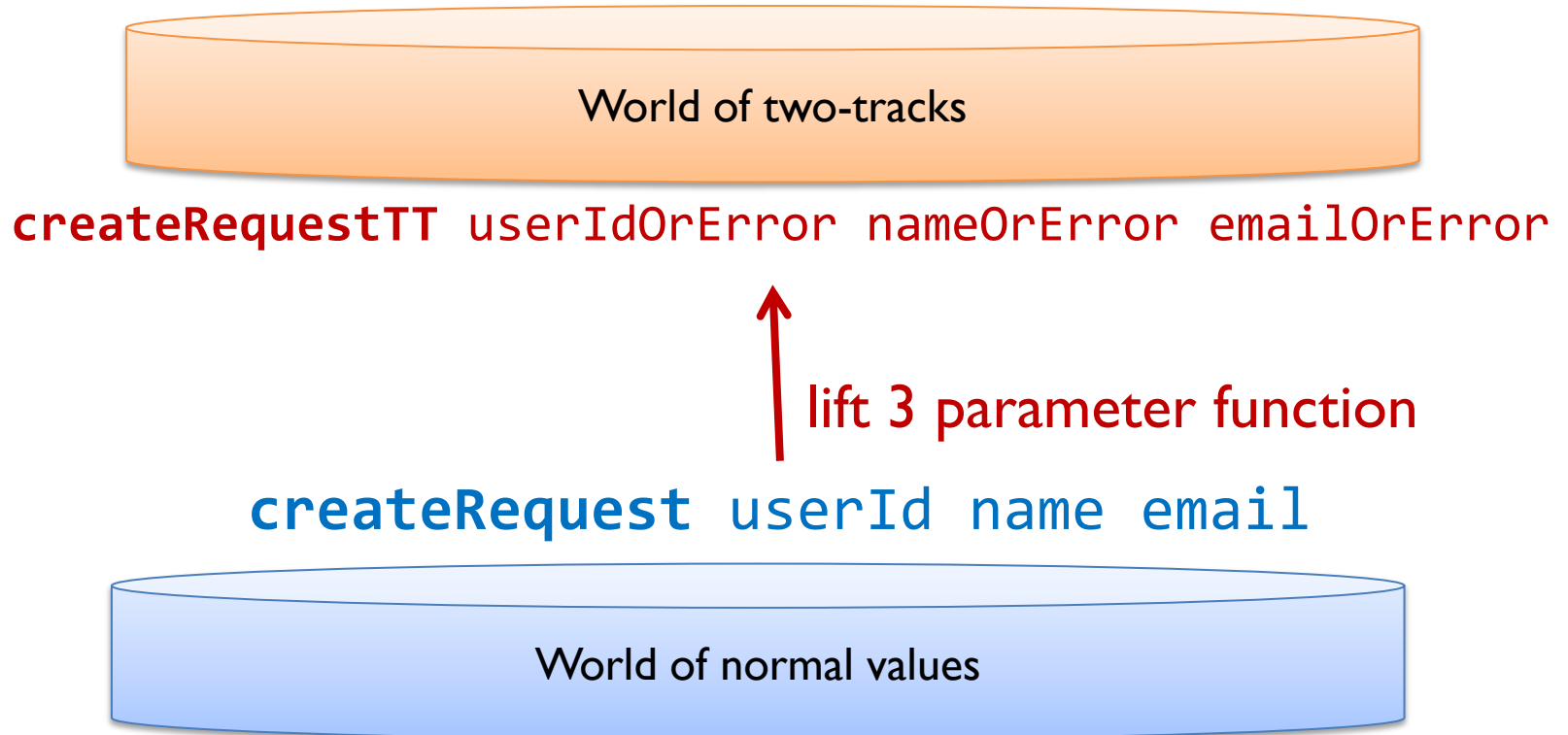
```
  {
    userId = userIdOrError.SuccessValue
    name = nameOrError.SuccessValue
    email = emailOrError.SuccessValue
  }
```



```
else if userIdOrError.IsFailure
  && nameOrError.IsSuccess
  && emailOrError.IsSuccess then
  userIdOrError.Errors
```

```
else ...
```

Lifting to TwoTracks



The right way

First create a function that creates a Request

```
let createRequest userId name email =  
  {  
    userId = userIdOnError.SuccessValue  
    name = nameOnError.SuccessValue  
    email = emailOnError.SuccessValue  
  }
```

then "lift" it to the world of two track errors

```
let createRequestTT = lift3 createRequest
```

There is a separate "lift" function for each number of parameters: "lift2" "lift3" etc.

"lift1" is just "map"

The right way

```
let createRequestTT = lift3 createRequest
```

Now you can pass in the errors safely

```
let userIdOnError = validateUserId dto.userId  
let nameOnError = validateName dto.name  
let emailOnError = validateEmail dto.email
```

```
let requestOnError =  
    createRequestTT userIdOnError nameOnError emailOnError
```



The result is also in the
world of two tracks

The right way

Alternative using `<!>` and `<*>`

```
let userIdOrError = validateUserId dto.userId
let nameOrError = validateName dto.name
let emailOrError = validateEmail dto.email
```

```
let requestOrError =
  createRequest
    <!> userIdOrError
    <*> nameOrError
    <*> emailOrError
```



Guideline:

If you use a wrapped generic type,
look for a set of “lifts” associated
with it

Terminology alert:

Liftable types are “applicative functors”

Guideline:

If you create a wrapped generic type, also create a set of “lifts” for clients to use with it

But I'm not going explain how right now!

MONOIDS



WARNING

**Mathematics
Ahead**

Thinking like a mathematician

$$1 + 2 = 3$$

$$1 + (2 + 3) = (1 + 2) + 3$$

$$1 + 0 = 1$$

$$0 + 1 = 1$$

A way of combining
them

$$1 + 2 = 3$$

Some things

Another one of
those things

A way of combining
them

$$1 \times 2 = 3$$

Some things

Another one of
those things

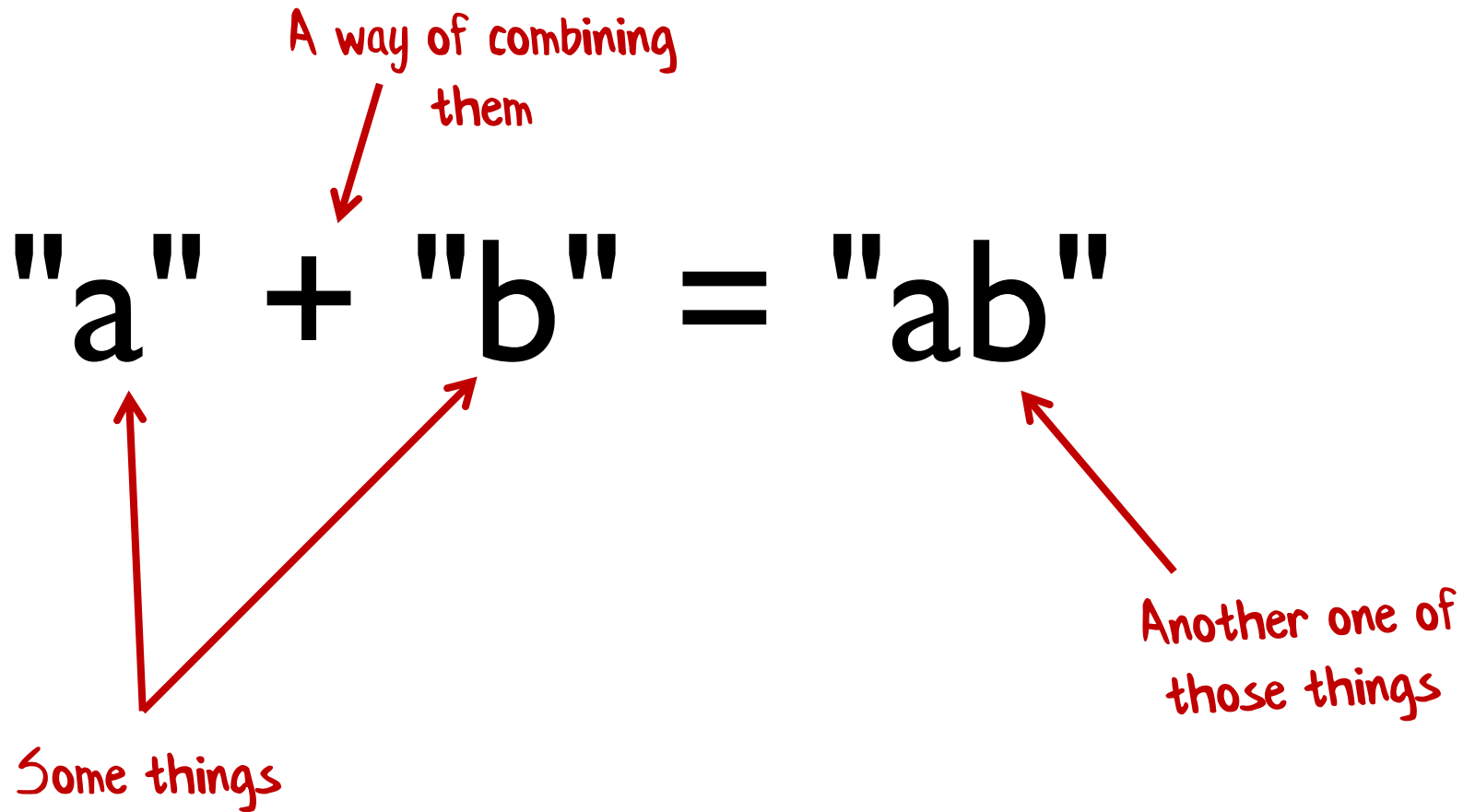
A way of combining
them

$$\max(1, 2) = 2$$

Some things

Another one of
those things

The diagram illustrates the function $\max(1, 2) = 2$. A red arrow points from the text 'A way of combining them' to the $\max$ function. Two red arrows point from the text 'Some things' to the arguments '1' and '2'. A red arrow points from the text 'Another one of those things' to the result '2'.



A way of combining
them

$$\text{concat}([a],[b]) = [a; b]$$

Some things

Another one of
those things

The diagram illustrates the `concat` function. The equation `concat([a],[b]) = [a; b]` is shown. A red arrow points from the text 'A way of combining them' to the `concat` function. Two red arrows point from the text 'Some things' to the arguments `[a]` and `[b]`. A red arrow points from the text 'Another one of those things' to the result `[a; b]`.

Is an integer

$$1 + 2$$

A pairwise operation has
become an operation that
works on lists!

Is an integer

$$1 + 2 + 3$$

$$1 + 2 + 3 + 4$$

Order of combining doesn't matter

$$1 + (2 + 3) = (1 + 2) + 3$$

$$1 + 2 + 3 + 4$$

$$(1 + 2) + (3 + 4)$$

$$((1 + 2) + 3) + 4$$

All the same

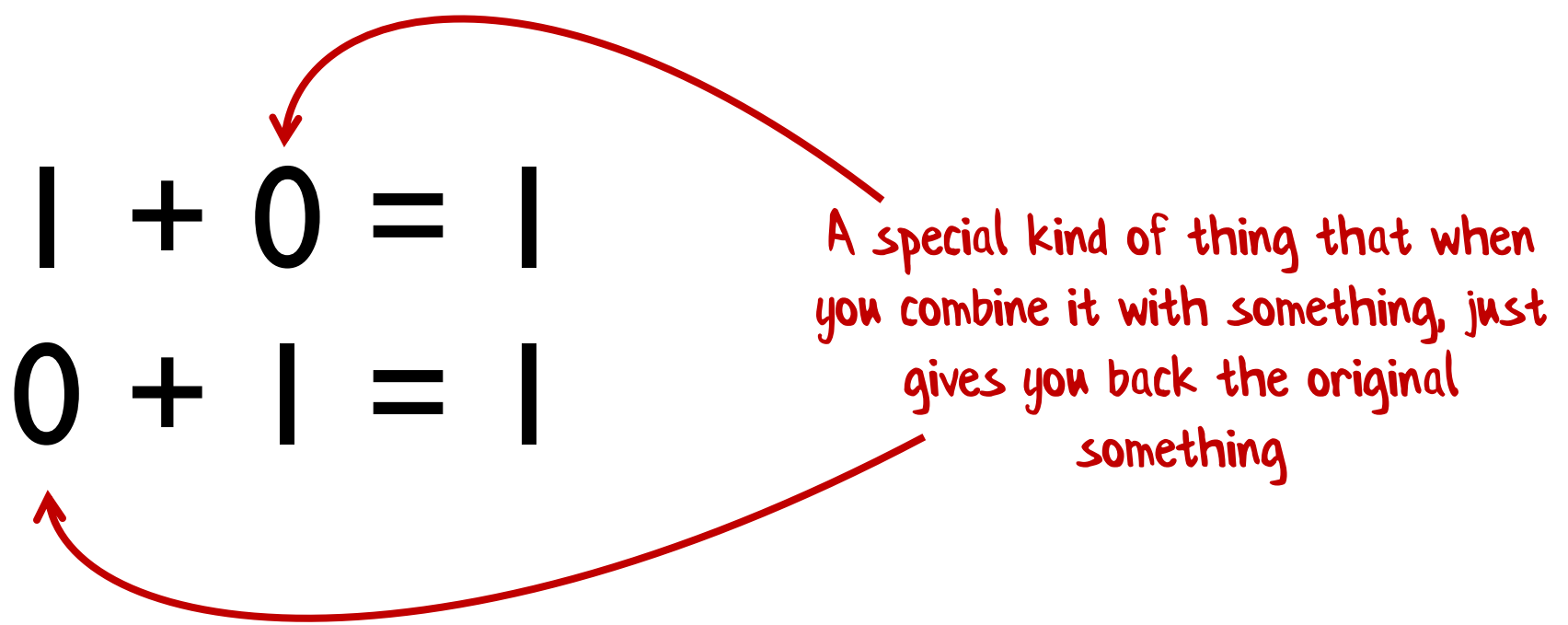
Order of combining does matter


$$1 - (2 - 3) = (1 - 2) - 3$$

$$1 + 0 = 1$$

$$0 + 1 = 1$$

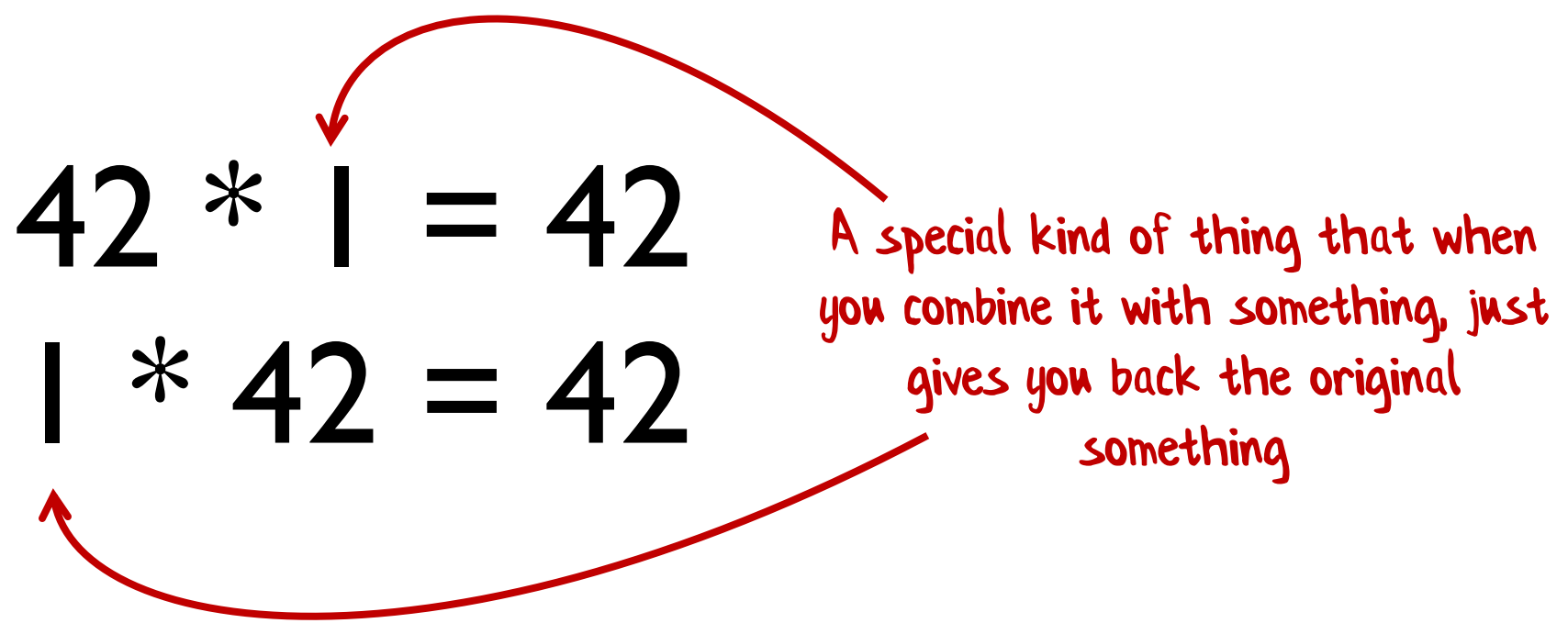
A special kind of thing that when you combine it with something, just gives you back the original something



$$42 * 1 = 42$$

$$1 * 42 = 42$$

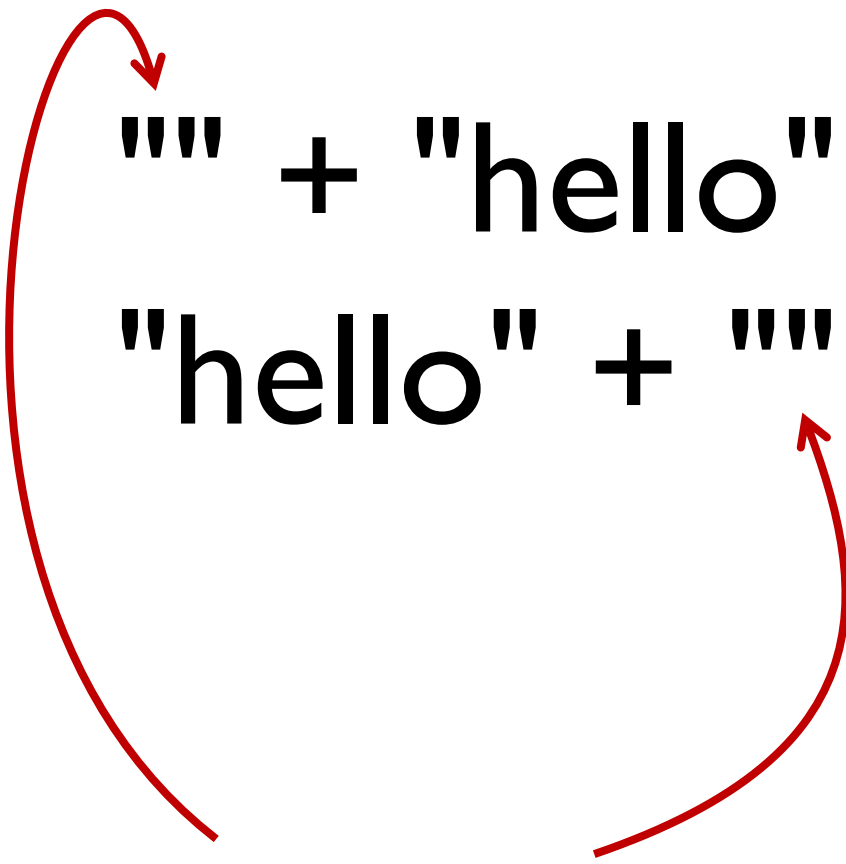
A special kind of thing that when you combine it with something, just gives you back the original something



"" + "hello" = "hello"

"hello" + "" = "hello"

"Zero" for strings



The generalization

- You start with a bunch of things, *and* some way of combining them two at a time.
- **Rule 1 (Closure):** The result of combining two things is always another one of the things.
- **Rule 2 (Associativity):** When combining more than two things, which pairwise combination you do first doesn't matter.
- **Rule 3 (Identity element):** There is a special thing called "zero" such that when you combine any thing with "zero" you get the original thing back.

A monoid!

- **Rule 1 (Closure):** The result of combining two things is always another one of the things.
- **Benefit:** converts pairwise operations into operations that work on lists.

$1 + 2 + 3 + 4$

$[1; 2; 3; 4] \rightarrow \text{List.reduce } (+)$

- **Rule 1 (Closure):** The result of combining two things is always another one of the things.
- **Benefit:** converts pairwise operations into operations that work on lists.

$1 * 2 * 3 * 4$

$[1; 2; 3; 4] \rightarrow \text{List.reduce} (*)$

- **Rule 1 (Closure):** The result of combining two things is always another one of the things.
- **Benefit:** converts pairwise operations into operations that work on lists.

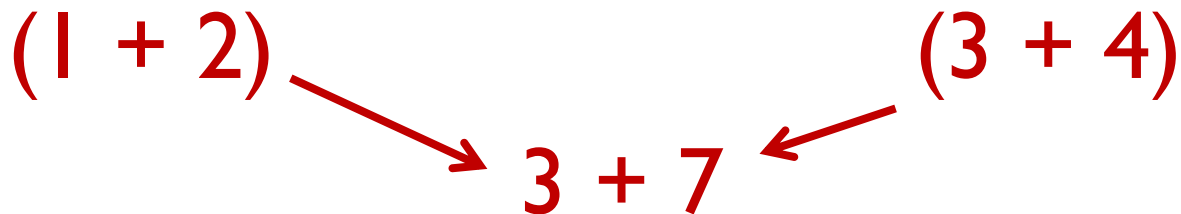
"a" + "b" + "c" + "d"

["a"; "b"; "c"; "d"] |> List.reduce (+)

- **Rule 2 (Associativity):** When combining more than two things, which pairwise combination you do first doesn't matter.
- **Benefit:** Divide and conquer, parallelization, and incremental accumulation.

$$1 + 2 + 3 + 4$$

- **Rule 2 (Associativity):** When combining more than two things, which pairwise combination you do first doesn't matter.
- **Benefit:** Divide and conquer, parallelization, and incremental accumulation.



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- **Benefit:** Divide and conquer, parallelization, and incremental accumulation.

$$(1 + 2 + 3)$$

- **Rule 2 (Associativity):** When combining more than two things, which pairwise combination you do first doesn't matter.
- **Benefit:** Divide and conquer, parallelization, and incremental accumulation.

$$(1 + 2 + 3) + 4$$

- **Rule 2 (Associativity):** When combining more than two things, which pairwise combination you do first doesn't matter.
- **Benefit:** Divide and conquer, parallelization, and incremental accumulation.

$$(6) + 4$$

Issues with reduce

- How can I use reduce on an empty list?
- In a divide and conquer algorithm, what should I do if one of the "divide" steps has nothing in it?
- When using an incremental algorithm, what value should I start with when I have no data?

- **Rule 3 (Identity element):** There is a special thing called "zero" such that when you combine any thing with "zero" you get the original thing back.
- **Benefit:** Initial value for empty or missing data



If missing, it
is called a
semigroup

Pattern:

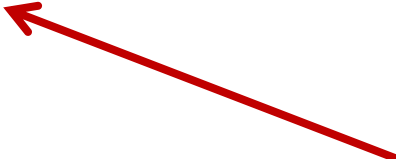
Simplifying aggregation code with monoids

```
type OrderLine = {Qty:int; Total:float}
```

```
let orderLines = [  
  {Qty=2; Total=19.98}  
  {Qty=1; Total= 1.99}  
  {Qty=3; Total= 3.99} ]
```

```
let addLine line1 line2 =  
  let newQty = line1.Qty + line2.Qty  
  let newTotal = line1.Total + line2.Total  
  {Qty=newQty; Total=newTotal}
```

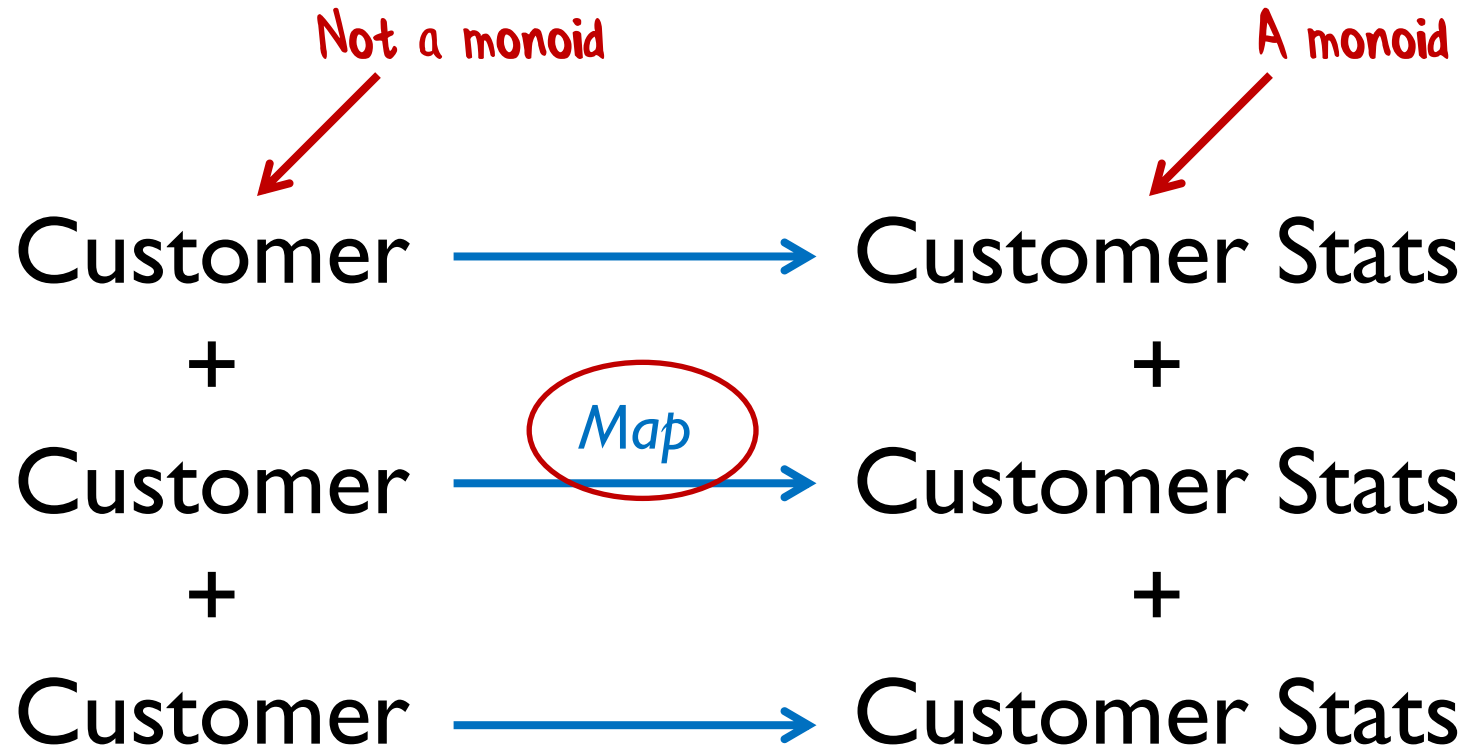
```
orderLines |> List.reduce addLine
```



Any combination
of monoids is
also a monoid

Pattern:

Convert non-monoids to monoids

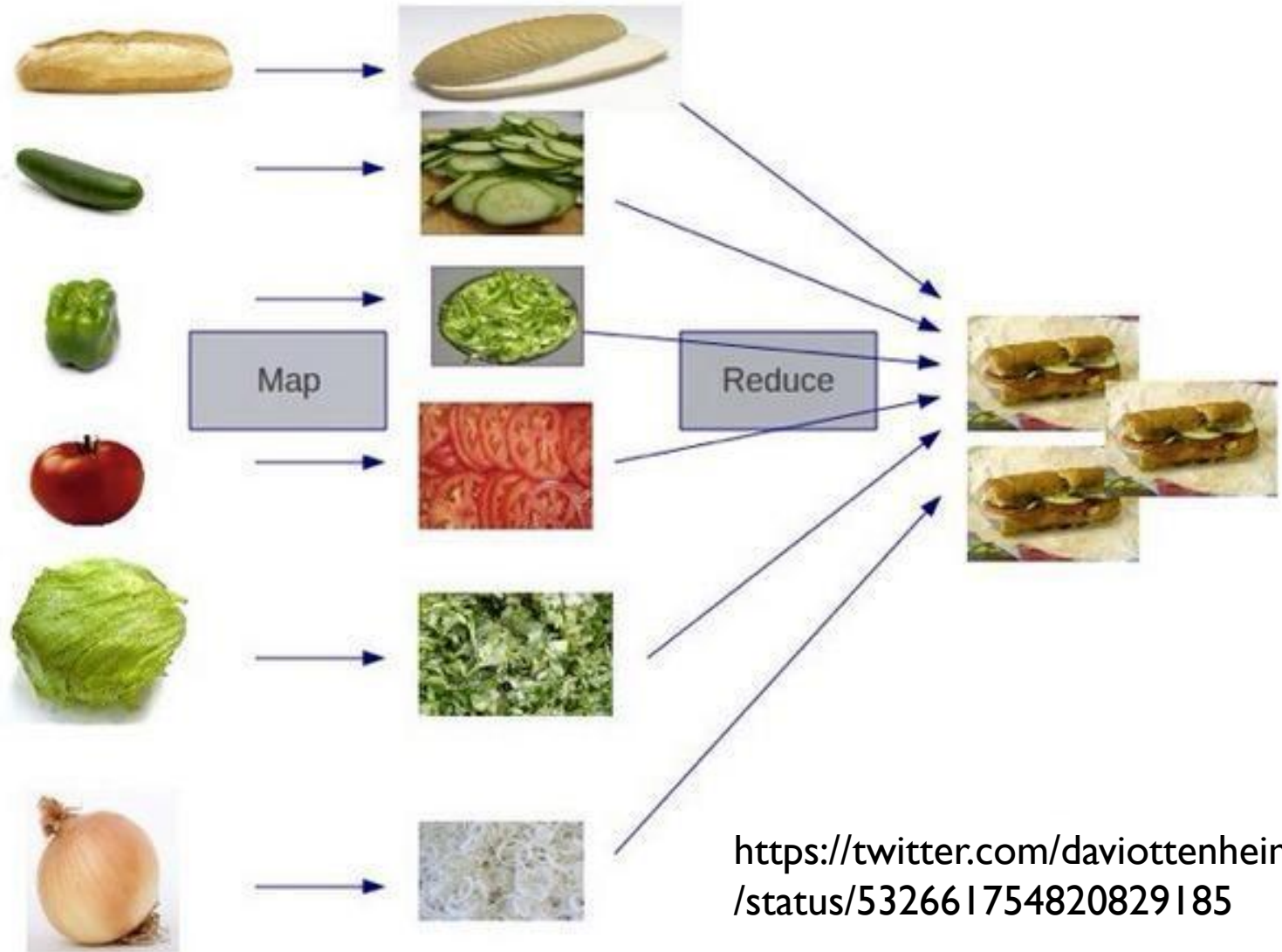


Map/Reduce!

Reduce

Summary Stats

Hadoop make me a sandwich



<https://twitter.com/daviottenheimer/status/532661754820829185>

Guideline:

Convert expensive monoids
to cheap monoids

Strings are monoids

A monoid

Log file (Mon) $\longrightarrow$ Summary (Mon)

+

+

Log File (Tue) $\xrightarrow{\text{Map}}$ Summary (Tue)

+

+

Log File (Wed) $\longrightarrow$ Summary (Wed)

=

Really big file

Much more efficient for
incremental updates

“Monoid homomorphism”

Pattern:

Seeing monoids everywhere

Monoids in the real world

Metrics guideline:

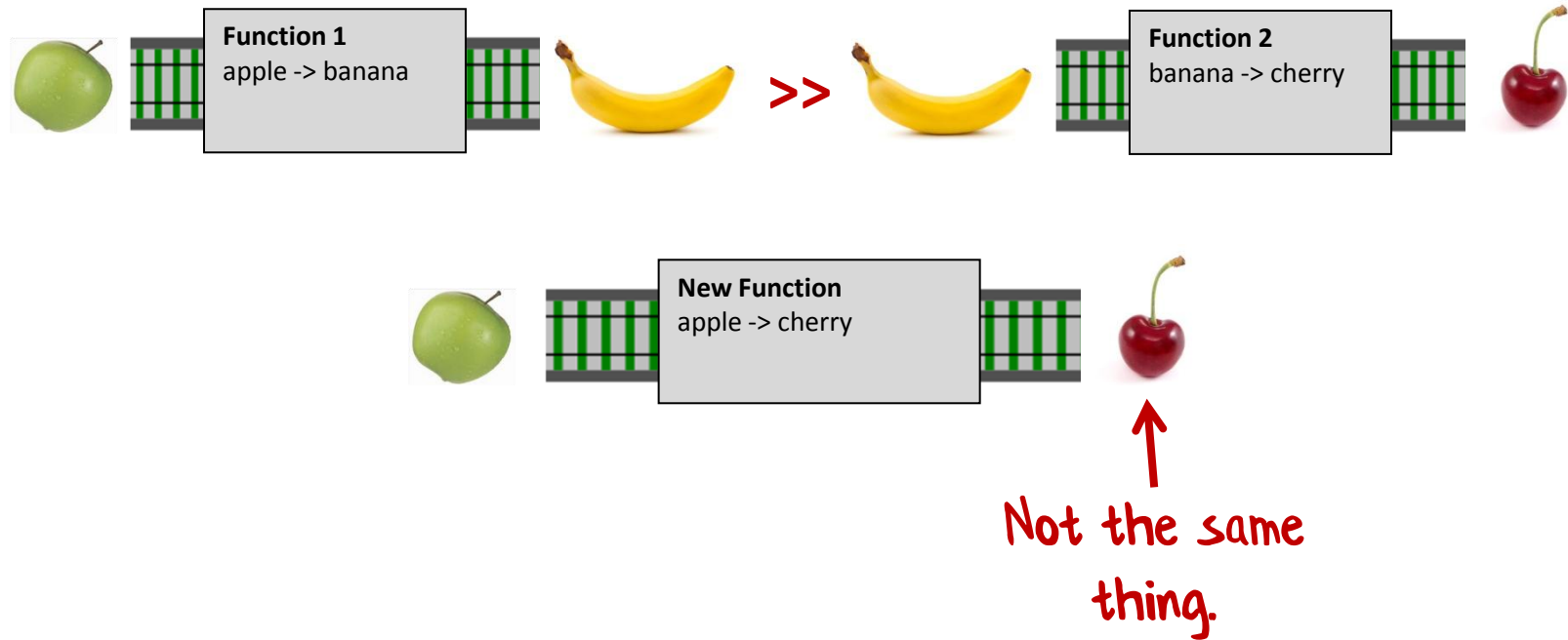
Use counters rather than rates

Alternative metrics guideline:

Make sure your metrics are monoids

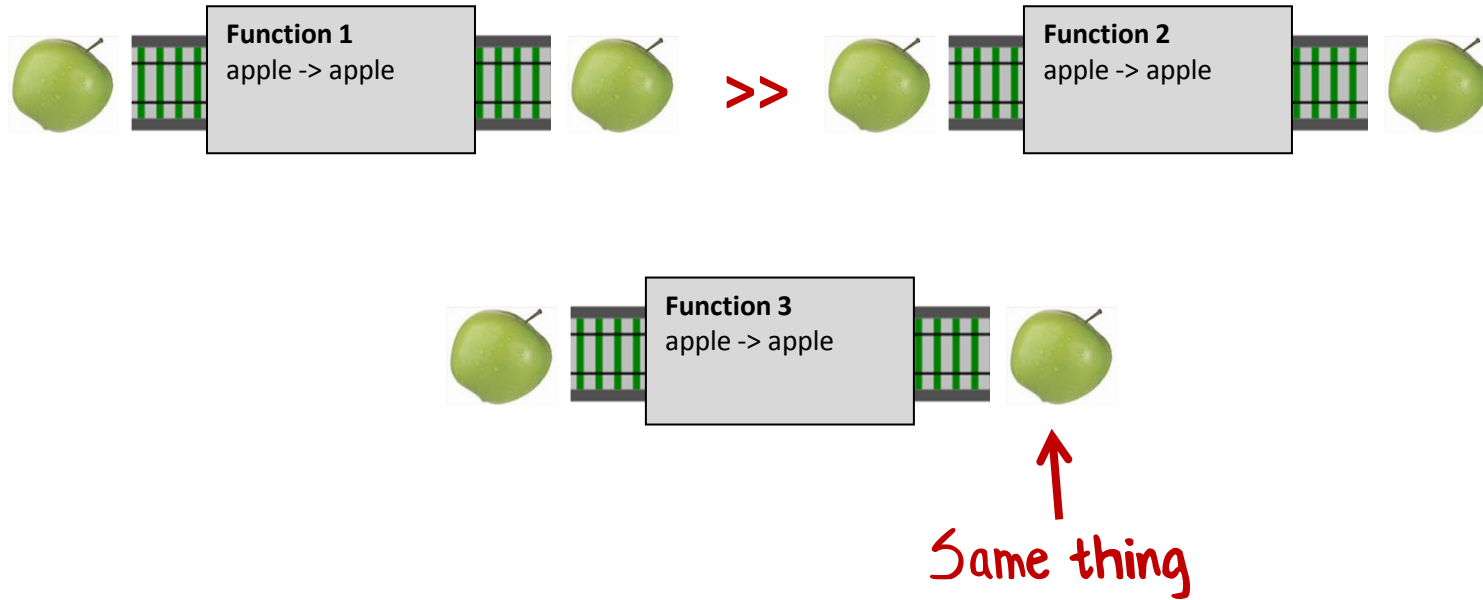
- incremental updates
- can handle missing data

Is function composition a monoid?



Not a monoid 😞

Is function composition a monoid?



A monoid! 😊

Is function composition a monoid?

Functions where the input and output are the *same* type are monoids! What shall we call these kinds of functions?

“Functions with same type of input and output”

Is function composition a monoid?

Functions where the input and output are the *same* type are monoids! What shall we call these kinds of functions?

~~“Functions with same type of input and output”~~

“Endomorphisms”

All endomorphisms are monoids

Endomorphism example

```
let plus1 x = x + 1           // int->int
let times2 x = x * 2          // int->int
let subtract42 x = x - 42      // int->int
```

Endomorphisms
↓

```
let functions = [
  plus1
  times2
  subtract42 ]
```

← Put them in a list

```
let newFunction =              // int->int
  functions |> List.reduce (>>)
```

↑
Reduce them

↑
Another
endomorphism

```
newFunction 20 // => 0
```

Event sourcing

Any function containing an endomorphism can be converted into a monoid.

For example: Event sourcing

Event $\rightarrow$ State $\rightarrow$ State

Is an endomorphism



Event sourcing example

Partial application of event

```
let applyFns = [  
  apply event1 // State -> State  
  apply event2 // State -> State  
  apply event3] // State -> State
```

```
let applyAll = // State -> State  
  applyFns |> List.reduce (>>)
```

```
let newState = applyAll oldState
```



A function that can apply all the events
in one step

- incremental updates
- can handle missing events

Bind

Any function containing an endomorphism can be converted into a monoid.

For example: Option.Bind

$(\text{fn param}) \rightarrow \text{Option} \rightarrow \text{Option}$

Is an endomorphism



Event sourcing example

Partial application of Bind

```
let bindFns = [  
  Option.bind (fun x->  
    if x > 1 then Some (x*2) else None)  
  Option.bind (fun x->  
    if x < 10 then Some x else None)  
]
```

```
let bindAll = // Option->Option  
  bindFns |> List.reduce (>>)
```

```
Some 4 |> bindAll // Some 8
```

```
Some 5 |> bindAll // None
```

Predicates as monoids

Not an endomorphism

```
type Predicate<'A> = 'A -> bool
```

```
let predAnd pred1 pred2 x =  
  if pred1 x  
  then pred2 x  
  else false
```

```
let predicates = [  
  isMoreThan10Chars      // string -> bool  
  isMixedCase            // string -> bool  
  isNotDictionaryWord    // string -> bool  
]
```

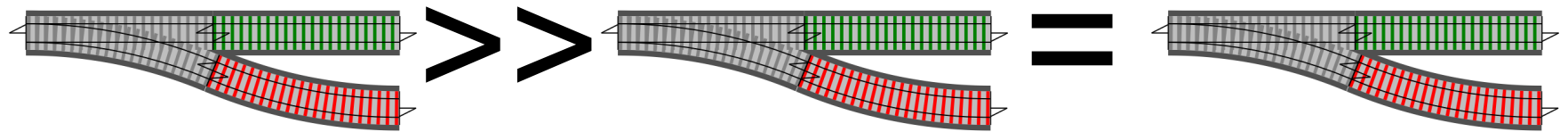
But can still be combined

```
let combinedPredicate = // string -> bool  
  predicates |> List.reduce (predAnd)
```

Pattern:

Monads are monoids

Series combination

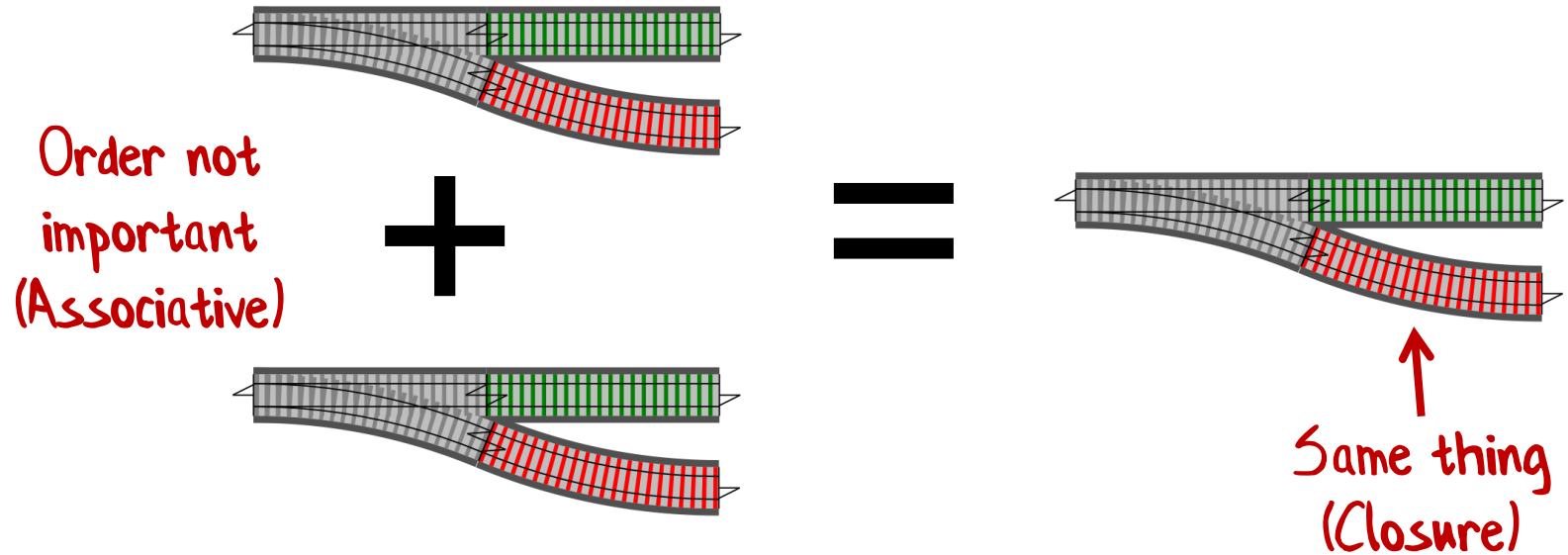


↑
Order not
important
(Associative)

Monoid!

↑
Result is same
kind of thing
(Closure)

Parallel combination



Monoid!

Monad laws

- The Monad laws are just the monoid definitions in disguise
 - Closure, Associativity, Identity
- What happens if you break the monad laws?
 - You lose monoid benefits such as aggregation



**A monad is just a monoid in
the category of endofunctors!**



THANKS!

More F#
here!