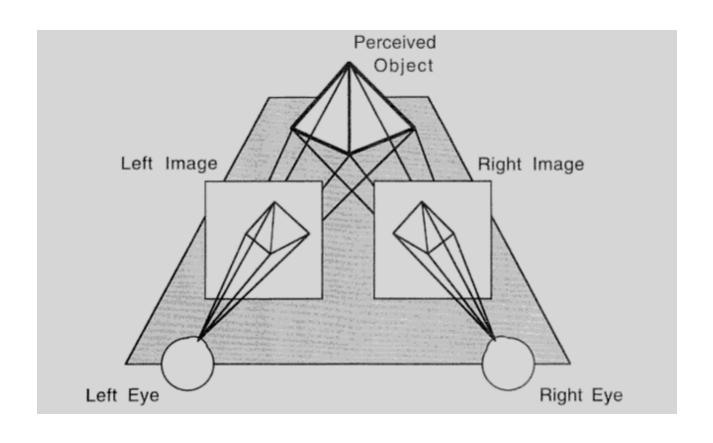
Binocular Stereopsis

How multiple views enable one to reconstruct depth in the world

Jitendra Malik
UC Berkeley

Binocular Stereopsis



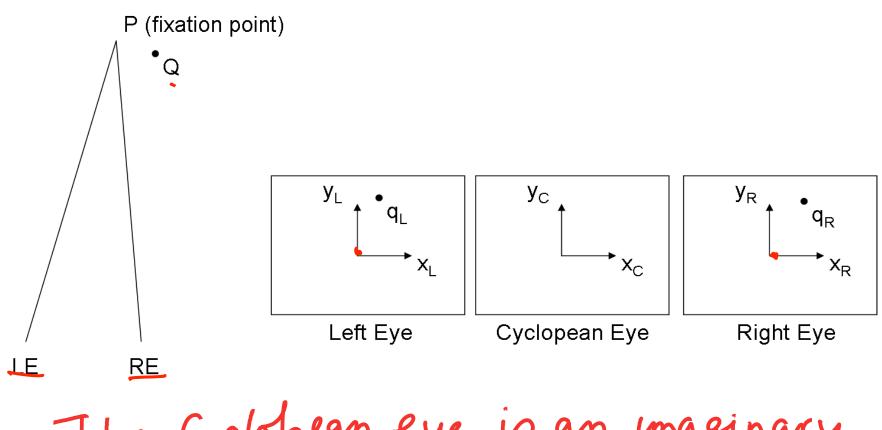
Various camera configurations

Single point of fixation where optical axes intersect

Optical axes parallel (fixation at infinity)

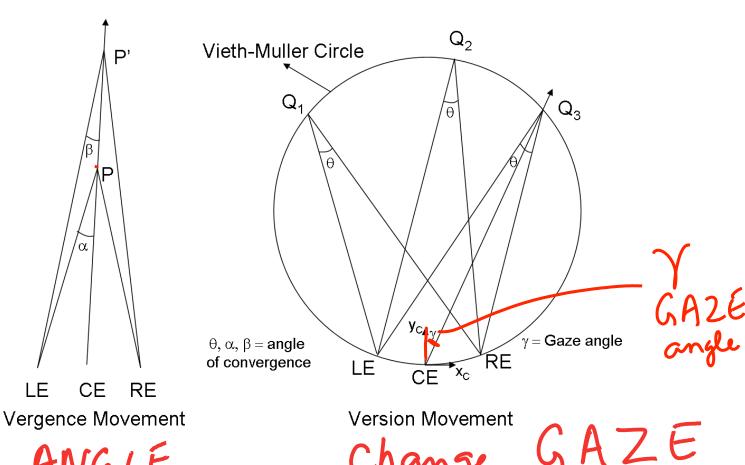
General case

Disparity for a fixating binocular system

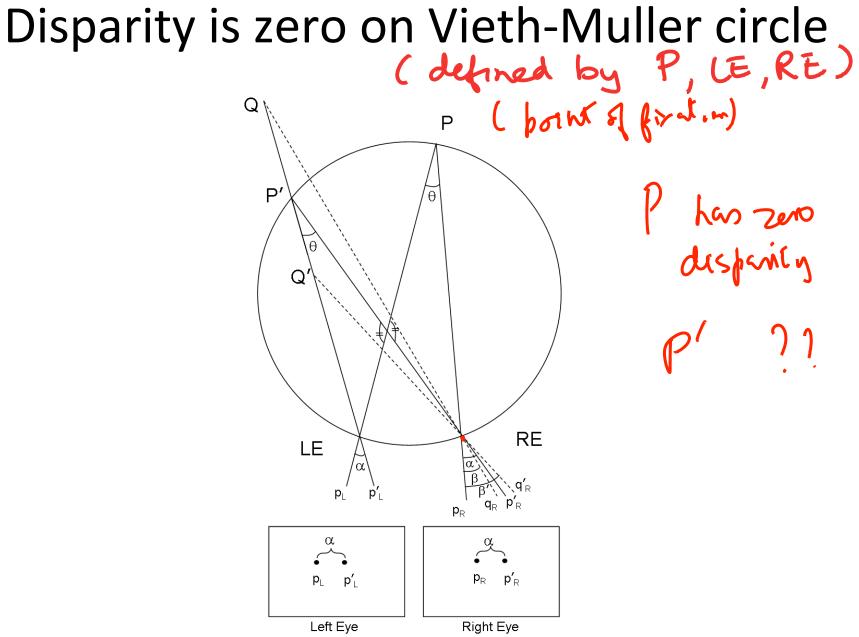


The Cyclopean eye is an imaginary eye at the midbint of LE & RE

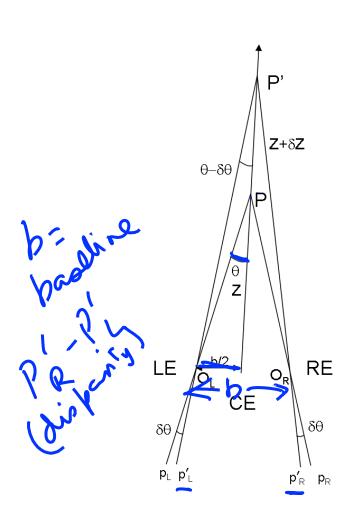
The two basic binocular eye movements



Change GAZE



Relation between disparity and depth



$$tom \theta = \frac{b/2}{Z}$$

 $tom \theta = \frac{b/2}{Z}$ $tom (0-80) = \frac{b/2}{Z+87}$

For small angles $\tan \theta \approx \theta$

$$\theta = \frac{b/2}{Z}$$

$$(\theta - \delta\theta) = \frac{b/2}{Z + \delta Z}$$

$$\delta\theta = \frac{b/2}{Z} - \frac{b/2}{Z + \delta Z}$$

$$\approx \frac{b\delta Z}{2Z^2}$$

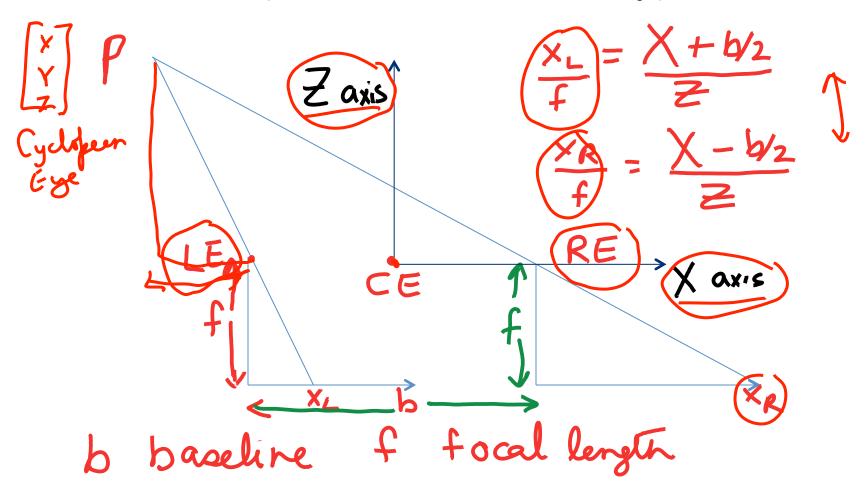
Various camera configurations

Single point of fixation where optical axes intersect

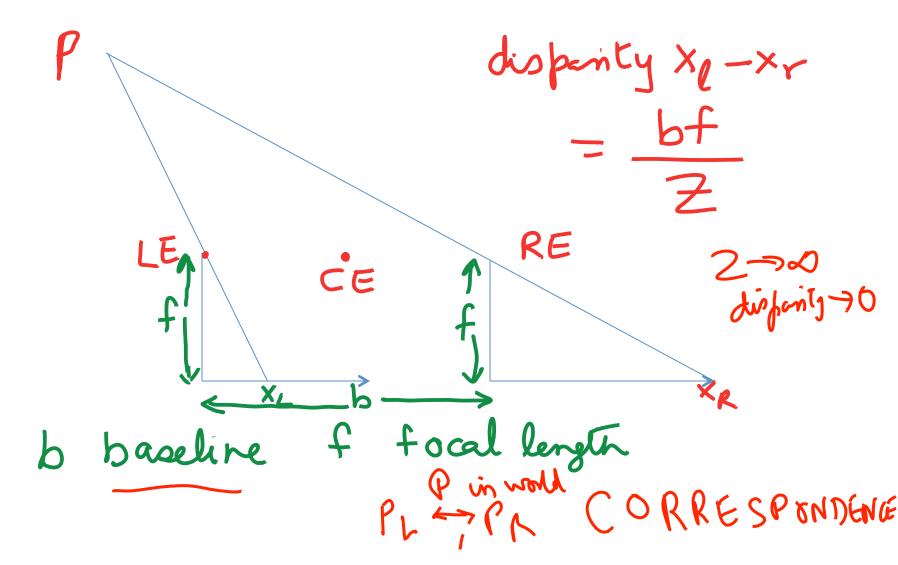
Optical axes parallel (fixation at infinity)

General case

Parallel Optical Axes (fixation at infinity)

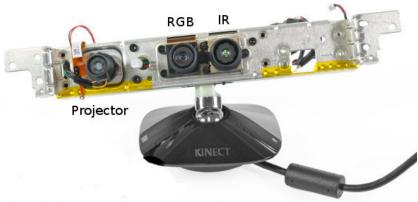


Parallel Optical Axes (fixation at infinity)

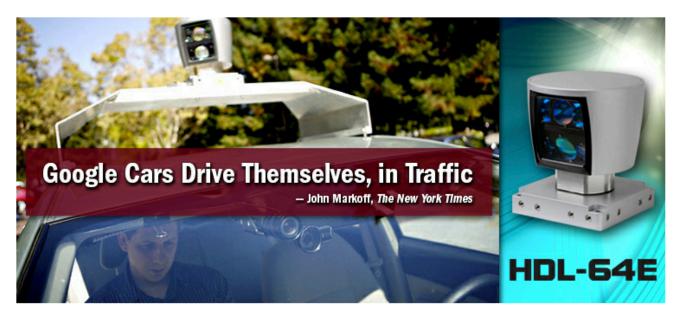


Range Sensors





primesense sensor (used in Kinect)



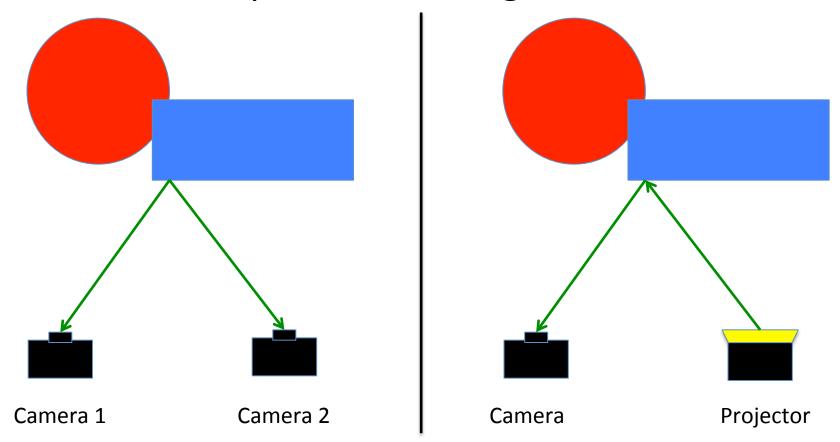
Velodyne LIDAR Sensor

http://www.primesense.com/, http://www.ifixit.com/,

http://mirror.umd.edu/roswiki/kinect calibration(2f)technical.html

http://velodynelidar.com/lidar/lidar.aspx

Depth from Triangulation

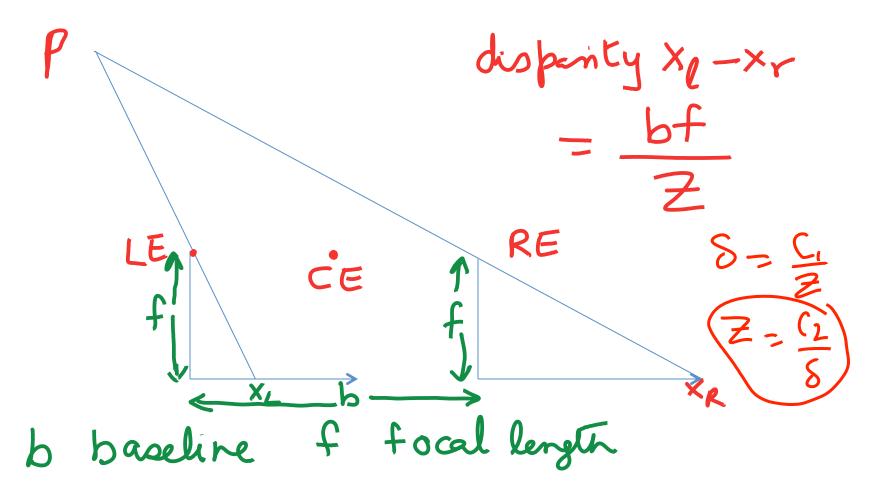


Passive Stereopsis

Active Stereopsis

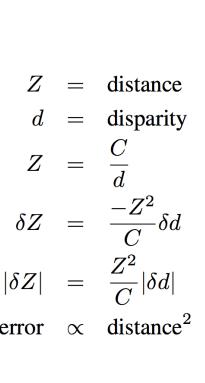
Active sensing simplifies the problem of estimating point correspondences

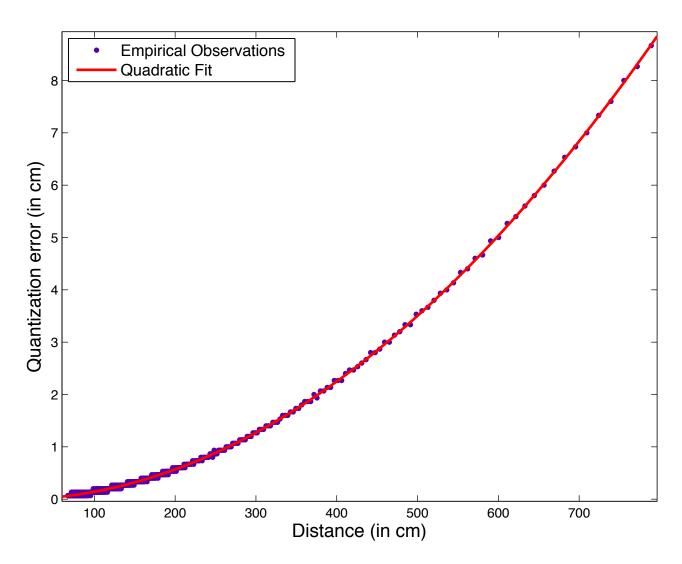
Recall the formula for disparity with parallel optical axes...



error(distance) – Kinect type sensor

Error in distance estimate increases quadratically with the distance





Bessel chose the star 61 Cygni as a likely star to be near the Sun, and therefore to have appreciable parallax. 61 Cygni is not nearly so bright as a Lyræ, but has a very great angular movement or proper-motion among the stars. Bessel used an instrument called a heliometer. Like Struve's telescope, it was mounted so that it could be driven by clock-work to point always at the same star. The object-glass of Bessel's telescope was made by the great optician Fraunhofer, with the intention of cutting it in halves. Fraunhofer died before the time came to carry out this delicate operation, but it was successfully accomplished after his death.

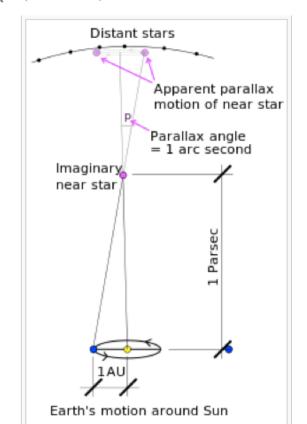
Delicate mechanism was provided for turning the glass, and also for moving the two halves relatively to each other; the amount of movement being very accurately measured by screws. Each half gives a perfect image of any object which is examined, but the two images are shifted by an amount equal to the distance one half of the lens is moved along the other. Thus when a bright star and faint star are looked at, one half of the object-glass can be made to give images S and s, and the other half S' and s'. By moving the screw exactly the right amount s' can be made to coincide with S, and the reading of the screw gives a measure of the angular distance between the two stars. Bessel made observations on 98 nights extending from August 1837 to September 1838. The following table, taken from a report by Main (Mem. R. A. S. vol. xii. p. 29), shows how closely the mean of the observations for each month accords with the supposition that the star has the parallax o".369:-

Mean date.	Observed Displace- ment.	Effect of parallax o":369.	Mean date.	Observed Displace- ment.	Effect of parallax o,, 369.
1837. Aug. 23	+0"197	+0.212	1838. Feb. 5	-o''223	-0.266
Sept. 14	+0,100	+0.100	Мау 14	+0.245	+0.738
Oct. 12	+0.040	-0.024	June 19	+0.360	+0.335
Nov. 22	-0'214	-0.58	July 13	+0.516	+0.335
Dec. 21	-0.322	-0.314	Aug. 19	+0.121	+0.522
1838. Jan. 14	-0.376	-0.318	Sept. 19	+0.040	+0'073

The great and difficult problem which had occupied astronomers for many generations was thus solved for three separate stars in 1838:—

	Parallax.	Distance.	Modern observations.	
	raranax.		Parallax.	Distance.
α Centauri (Henderson)	1,0	200,000	o" ₇₅₀	270,000
61 Cygni (Bessel)	0.314	640,000	.282	700,000
a Lyræ (Struve)	0'262	760,000	.10	2,000,000

(The unit of distance is that from the Earth to the Sun.)



Various camera configurations

Single point of fixation where optical axes intersect

Optical axes parallel (fixation at infinity)

General case

