

Functional Programming WS 2010/11

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October 27, 2010

Today's Topics

- Intermediate Wrap-Up
- User-Defined Types / Trees
- Input and Output



Prelude Functions You Should Know

infix operators and special syntax

$$(<=), (<), (==), (>=), (>), (||), (-), (,), (:), (/=), (.), (*), (&&), (+), [], [\langle m \rangle..\langle n \rangle]$$

other Prelude functions

abs, compare, concat, const, div, drop, error, even, filter, foldr, fromInteger, fst, head, init, last, length, lines, map, max, min, mod, negate, not, null, otherwise, product, putStrLn, read, replicate, reverse, show, signum, snd, splitAt, sum, tail, take, unlines, unwords, words, zip, zipWith

- anonymous functions / functions without names
 - ($\x -> 2*x$) -- an anonymous function for doubling
- infix operators and sections

$$(+) = (\x y \rightarrow x + y) \text{ infix to prefix}$$

$$x `f` y = f x y \text{ prefix to infix}$$

$$(a>) = (\x \rightarrow a > x) \text{ argument smaller than a?}$$

$$(>b) = (\x \rightarrow x > b) \text{ argument greater than b?}$$

• patterns and guards

```
headIfPositive xs = case xs of x:  | x > 0 \rightarrow x
```

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type signatures, annotate functions by types

type synonyms, mnemonic names for types

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type classes and class constraints - for every function f,
 specific to class C, type inference adds a C-constraint to type

Example - Type Constraints

• without type signature, we get

```
ghci> :t range
range :: (Ord a, Num a) => a -> a -> [a]
```

- m > n, hence m and n of class Ord and m and n of same type
- m+1, hence m of class Num
- m and n of same type, hence n of class Num

Equational Reasoning

- a function definition in Haskell is a (set of conditional) equation(s)
- if conditions are met, we may "replace equals by equals"
- in this way we may evaluate function calls by applying equations stepwise, until we reach final result

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Kinds of Conditions

- "if $\langle b \rangle$ then $\langle t \rangle$ else $\langle e \rangle$ " is $\langle t \rangle$, when $\langle b \rangle$ is true; and $\langle e \rangle$, otherwise
- "case $\langle e \rangle$ of $\{ \langle p_1 \rangle \rightarrow \langle e_1 \rangle; \dots; \langle p_n \rangle \rightarrow \langle e_n \rangle \}$ " is $\langle e_i \rangle$, if $\langle e \rangle$ first matches $\langle p_i \rangle$

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Primitive Operations

- for primitive operations (like (+), (*), ...), we assume predefined equations
- e.g., 1 + 2 = 3, 0 * 10 = 0, ...

definition

```
zip (x:xs) (y:ys) = (x,y) : zip xs ys
zip _ = []
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```
factorial n \mid n \le 1 = 1
| otherwise = n * factorial (n-1)
```

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• evaluate prod [5,6]

User-Defined Types / Trees

Data Declarations / Algebraic Data Types

new types are introduced by

- where $\langle T \rangle$ is the name of the new type (starting with a capital letter) taking n type parameters α_1 to α_n
- and $\langle C_i \rangle$ is the name of the *i*-th (data) constructor, taking m_i arguments of types τ_{i1} to τ_{im_i} (which may contain only type variables among α_1 to α_n)

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Examples

- data Bool = False | True
- data List a = Nil | Cons a (List a)
- data Pair a b = Pair a b

constructors and type names live in different name spaces

Automatically Deriving Type Class Instances

- for some type classes it is possible to automatically derive instances for algebraic data types
- e.g.,

```
data List a = Nil | Cons a (List a)
  deriving (Eq, Show, Read)
```

now, we are able to use (==), show, and read for Lists

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Examples

```
ghci> Nil == Cons 1 Nil
False
ghci> show (Cons 1 (Cons 2 Nil))
"Cons 1 (Cons 2 Nil)"
ghci> read it :: List Int
Cons 1 (Cons 2 Nil)
```

Definition - Tree

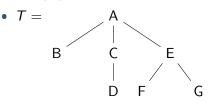
- (rooted) tree T = (N, E)
- with set of nodes N
- and set of edges/vertices $E \subseteq N \times N$
- unique root of T ($root(T) \in N$) without predecessor
- all other nodes have exactly one predecessor

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Example

- $N = \{A, B, C, D, E, F, G\}$
- $E = \{(A, B), (A, C), (A, E), (C, D), (E, F), (E, G)\}$
- root(T) = A



Trees in Haskell

possible type for trees with arbitrary nodes

```
data Tree a = Empty | Node a [Tree a]
```

 a tree is either empty (0 nodes) or there is at least one node with content of type a and an arbitrary number of successor trees

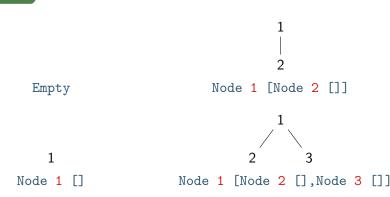
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Examples



Binary Trees

- restrict number of successors (maximal 2)
- type

```
data BTree a = Empty | Node a (BTree a) (BTree a)
deriving (Eq, Show, Read)
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Functions on Binary Trees

• computing the number of nodes

```
size :: BTree a -> Integer
size Empty = 0
size (Node _ l r) = size l + size r + 1
```

• height - length of longest path from root to some leaf plus one

```
height :: BTree a -> Integer
height Empty = 0
height(Node _ l r) = max (height l) (height r) + 1
```

Creating Trees from List

the easy way

```
fromList [] = Empty
fromList (x:xs) = Node x Empty (fromList xs)
```

• the fair way

ordered

Transforming Trees into Lists

```
flatten Empty = []
flatten (Node x l r) = flatten l ++ [x] ++ flatten r
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A Sorting Algorithm for Lists

sort = flatten . searchTree



An Initial Example

write the file welcomeIO.hs

```
main = do
  putStrLn "Greetings! What's your name?"
  name <- getLine
  putStrLn (
    "Welcome to Haskell's IO, " ++ name ++ "!")</pre>
```

compile it with GHC via

```
$ ghc --make welcomeIO.hs
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• and run it

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Notes

- putStrLn prints a string + newline
- getLine reads a line from standard input
- new: do and <-

IO and the Type System

consider

```
ghci> :load welcomeIO.hs
ghci> :t putStrLn
putStrLn :: String -> IO ()
ghci> :t getLine
getLine :: IO String
ghci> :t main
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• IO a is the type of IO actions delivering results of type a (in addition to their IO operations)

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Examples

- String -> IO () after supplying a string, we obtain an IO action (in the case of putStrLn, "printing")
- IO () just IO (in the case of main, run our program)
- IO String do some IO and deliver a string (in the case of getLine, the user-input)

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Implications

- once we are inside an IO action, we cannot escape
- strict separation between purely functional code and IO
- when IO a does not appear inside type signature, we can be absolutely sure that no IO ("side-effect") is performed

Using Pure Code Inside IO Actions

consider the program reply.hs

```
reply :: String -> String
reply name =
  "Pleased to meet you, " ++ name ++ ".\n" ++
  "Your name contains " ++ n ++ " characters."
  where n = \text{show (length name)}
main :: IO ()
main = do
  putStrLn "Greetings again. What's your name?"
  name <- getLine</pre>
  let niceReply = reply name
  putStrLn niceReply
```

• i.e., we may use **let** $\langle x \rangle = \langle f \rangle$ (there is no **in** here!) to bind the result of the pure function $\langle f \rangle$ to the name $\langle x \rangle$

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- writeFile :: FilePath -> String -> IO ()
- appendFile :: FilePath -> String -> IO ()

Examples - Imitating Some GNU Commands

cat.hs - print file contents

```
main = do
  [file] <- getArgs</pre>
  s <- readFile file
  putStr s
```

wc.hs - count newlines/words/bytes in input

```
count s = ns ++ " ++ ws ++ " ++ bs ++ "\n"
 where ns = show (length (lines s))
       ws = show (length (words s))
       bs = show (length s)
main = interact count
```

uniq.hs - omit repeated lines of input

```
main = interact (unlines . nub . lines)
```

• sort.hs - sort input main = interact (unlines . sort . lines)

Notes

- getArgs :: IO [String] is in System.Environment
- nub :: Eq a => [a] -> [a] is in Data.List; eliminates duplicates
- sort :: Ord a => [a] -> [a] is in Data.List; sorts a list

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Do Some IO Action for Each Argument

```
foreach :: [a] -> (a -> IO ()) -> IO ()
 foreach [] io = return ()
 foreach (a:as) io = do {io a; foreach as io}

    better cat.hs
```

```
main = do
  files <- getArgs</pre>
  foreach files readAndPrint
  where readAndPrint file = do
           s <- readFile file</pre>
           putStr s
```

Exercises (for November 5th)

- 1. read chapter 7 of Real World Haskell
- evaluate the two function calls foldr (-) 0 [1,2,3] and foldl (-) 0 [1,2,3] by equational reasoning (using the definitions from the standard Prelude)
- 3. implement the predicate
 isSorted :: Ord a => BTree a -> Bool, checking
 whether the given tree is a search tree
- 4. write a program Grep.hs that, given a string, echos every line of its standard input, containing this string
- 5. modify Grep.hs to also print line numbers of matching lines
- 6. implement a function
 showBTree :: Show a => BTree a -> String that prints
 a nice ASCII version of a binary tree