Online Advertising





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The New York Times

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Times Reporter Will Not Be Called to Testify in Leak Case

By MATT APUZZIO 9:00 PM ET

The decision ends a sevenyear legal fight over whether James Risen could be forced to name the sources of his reports on a botched C.I.A. operation.

#39 Comments

France Ordere



The Jacobou Bay Bridge, which cost \$2.3 billion, is the world's longest see-crossing bridge

Yes Survey Solvey via Assertable! Press

The Opinion Pages

Choke First, Ask Questions Later

By THE EDITORIAL BOARD

A new report suggests that this disavowed tactic has never gone away and sometimes officers use it as a first, not last, resort.

- Editorial: United in Outrage
- Sheryl Sandberg and Adam Grant: Speaking While Female
- Taking Note: The Sony Hack and the Gender Pay Gap
- The Stone: Why Life Is Absurd

A Swarm in 'Dead City'

By GABBRICLLE SELZ.

At 14, I tried to run away. But millions of molting cicadas came between me and my freedom.

- Blow: Tamir Rice and the Value of Life
- Krugman: For the Love of Carbon
- Room for Debate: When Satire Cuts Both Ways
- Bruni, Douthat: Movies and Our Still-Wrenching History



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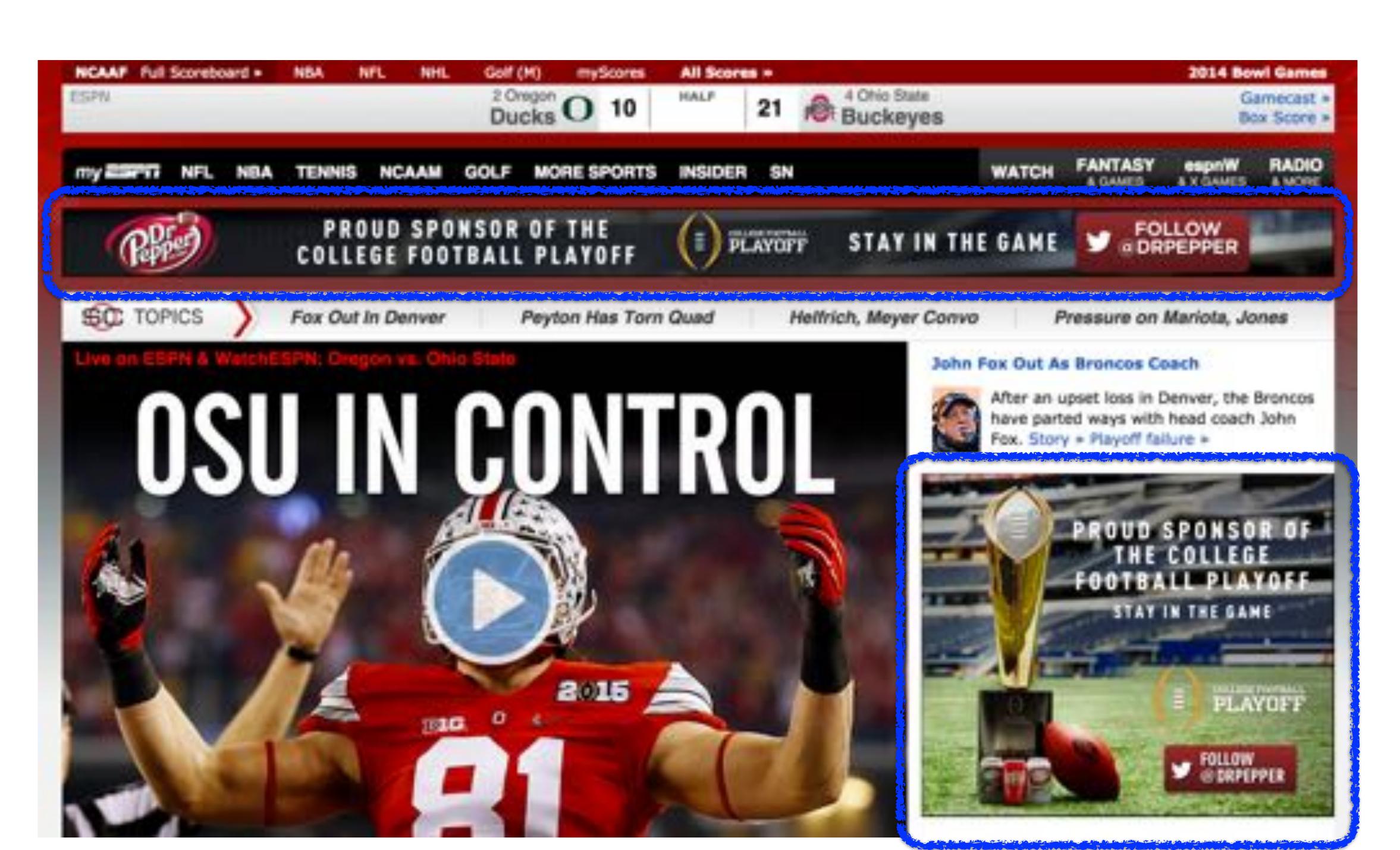
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Online Advertising is Big Business

Multiple billion dollar industry

\$43B in 2013 in USA, 17% increase over 2012 [PWC, Internet Advertising Bureau, April 2013]

Higher revenue in USA than cable TV and nearly the same as broadcast TV [PWC, Internet Advertising Bureau, Oct 2013]

Large source of revenue for Google and other search engines



Canonical Scalable ML Problem

Problem is hard; we need all the data we can get!

 Success varies by type of online ad (banner, sponsor search, email, etc.) and by ad campaign, but can be less than 1% [Andrew Stern, iMedia Connection, 2010]



Lots of Data

- Lots of people use the internet
- Easy to gathered labeled data





The Players

Publishers: NYTimes, Google, ESPN

Make money displaying ads on their sites

Advertisers: Marc Jacobs, Fossil, Macy's, Dr. Pepper

- Pay for their ads to be displayed on publisher sites
- They want to attract business

Matchmakers: Google, Microsoft, Yahoo

- Match publishers with advertisers
- In real-time (i.e., as a specific user visits a website)

Why Advertisers Pay?

Impressions

- Get message to target audience
- e.g., brand awareness campaign

Performance

- Get users to do something
- e.g., click on ad (pay-per-click) Most common
- e.g., buy something or join a mailing list

Efficient Matchmaking

Idea: Predict probability that user will click each ad and choose ads to maximize probability

- Estimate $\mathbb{P}(\text{click} | \text{predictive features})$
- Conditional probability: probability given predictive features

Predictive features

- Ad's historical performance
- Advertiser and ad content info
- Publisher info
- User info (e.g., search / click history)



Publishers Get Billions of Impressions Per Day

But, data is high-dimensional, sparse, and skewed

- Hundreds of millions of online users
- Millions of unique publisher pages to display ads
- Millions of unique ads to display
- Very few ads get clicked by users

Massive datasets are crucial to tease out signal

Goal: Estimate P(click | user, ad, publisher info)

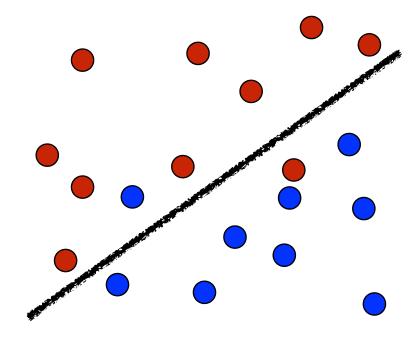
Given: Massive amounts of labeled data

Linear Classification and Logistic Regression





Classification

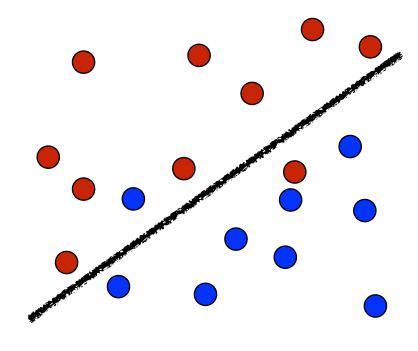


Goal: Learn a mapping from observations to discrete labels given a set of training examples (supervised learning)

Example: Spam Classification

- Observations are emails
- Labels are {spam, not-spam} (Binary Classification)
- Given a set of labeled emails, we want to predict whether a new email is spam or not-spam

Classification

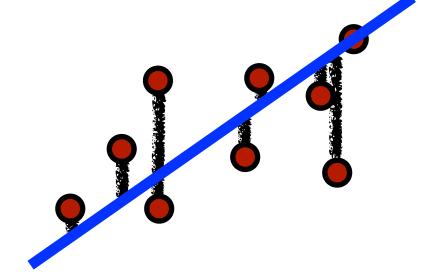


Goal: Learn a mapping from observations to discrete labels given a set of training examples (supervised learning)

Example: Click-through Rate Prediction

- Observations are user-ad-publisher triples
- Labels are {not-click, click} (Binary Classification)
- Given a set of labeled observations, we want to predict whether a new user-ad-publisher triple will result in a click

Reminder: Linear Regression



Example: Predicting shoe size from height, gender, and weight

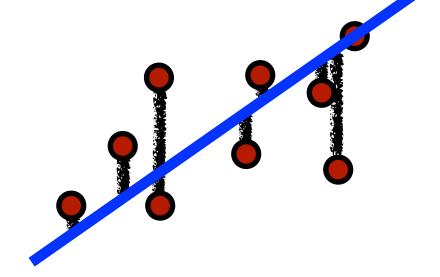
For each observation we have a feature vector, x, and label, y

$$\mathbf{x}^{\top} = \begin{bmatrix} x_1 & x_2 & x_3 \end{bmatrix}$$

We assume a *linear* mapping between features and label:

$$y \approx w_0 + w_1 x_1 + w_2 x_2 + w_3 x_3$$

Reminder: Linear Regression



Example: Predicting shoe size from height, gender, and weight

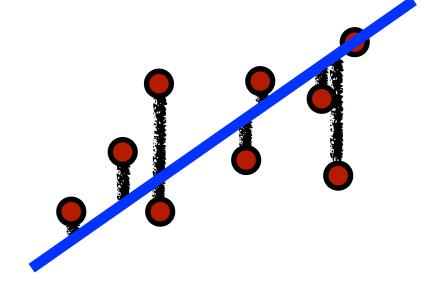
We can augment the feature vector to incorporate offset:

$$\mathbf{x}^{\top} = \begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix}$$

We can then rewrite this linear mapping as scalar product:

$$y \approx \hat{y} = \sum_{i=0}^{3} w_i x_i = \mathbf{w}^{\mathsf{T}} \mathbf{x}$$

Why a Linear Mapping?



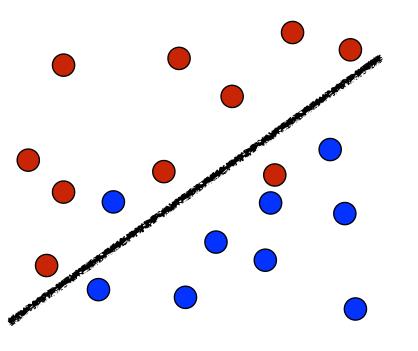
Simple

Often works well in practice

Can introduce complexity via feature extraction

Can we do something similar for classification?

Linear Regression ⇒ Linear Classifier •...•



Example: Predicting rain from temperature, cloudiness, and humidity

Use the same feature representation: $\mathbf{x}^{\top} = \begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix}$

How can we make class predictions?

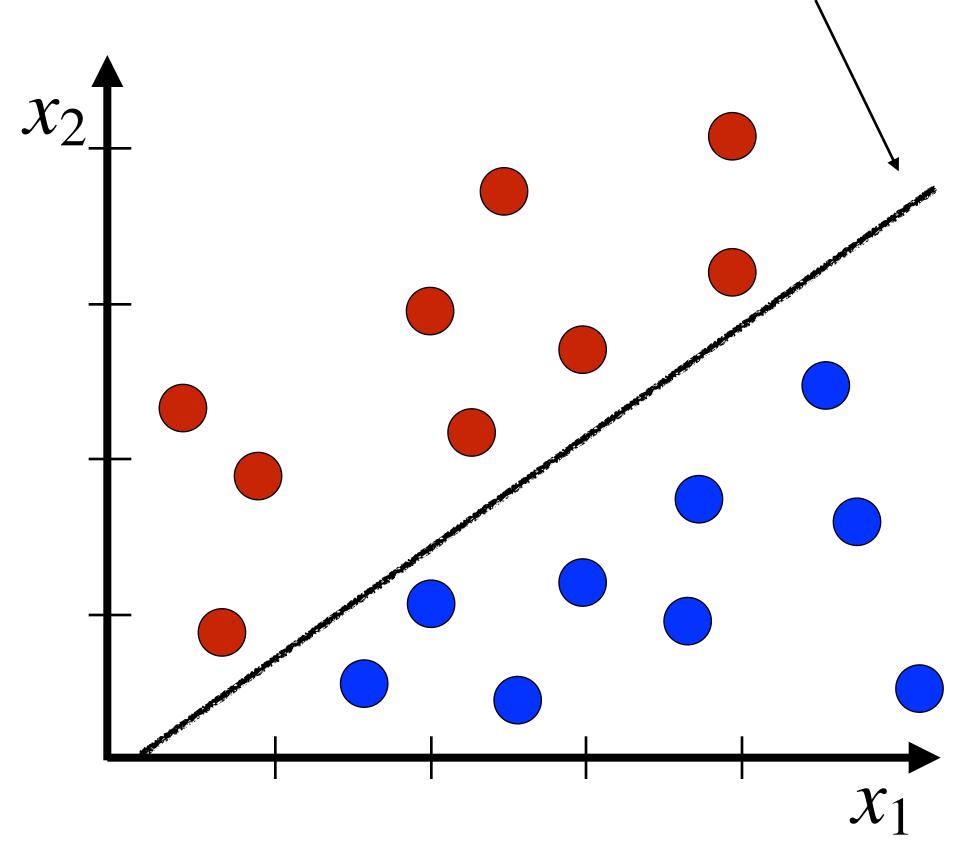
- {not-rain, rain}, {not-spam, spam}, {not-click, click}
- We can threshold by sign

$$\hat{y} = \sum_{i=0}^{3} w_i x_i = \mathbf{w}^{\top} \mathbf{x} \implies \hat{y} = \text{sign}(\mathbf{w}^{\top} \mathbf{x})$$

Linear Classifier Decision Boundary

Decision

Boundary
$$3x_1 - 4x_2 - 1 = 0$$



Imagine
$$\mathbf{w}^{\top} = \begin{bmatrix} -1 & 3 & -4 \end{bmatrix}$$

$$\mathbf{x}^{\top} = \begin{bmatrix} 1 & 2 & 3 \end{bmatrix} : \mathbf{w}^{\top} \mathbf{x} = -7$$

$$\mathbf{x}^{\top} = \begin{bmatrix} 1 & 2 & 1 \end{bmatrix} : \mathbf{w}^{\top} \mathbf{x} = 1$$

$$\mathbf{x}^{\top} = \begin{bmatrix} 1 & 5 & .5 \end{bmatrix} : \mathbf{w}^{\top} \mathbf{x} = 12$$

$$\mathbf{x}^{\top} = \begin{bmatrix} 1 & 3 & 2.5 \end{bmatrix} : \mathbf{w}^{\top} \mathbf{x} = -2$$

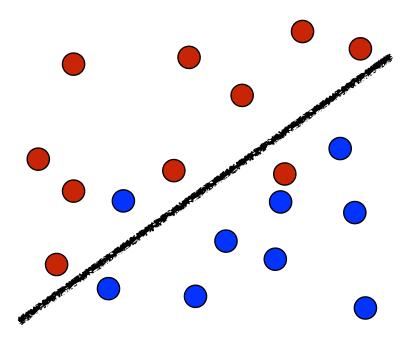
Let's interpret this rule: $\hat{y} = sign(\mathbf{w}^{\top} \mathbf{x})$

$$\hat{\mathbf{y}} = 1 : \mathbf{w}^{\top} \mathbf{x} > 0$$

$$\hat{\mathbf{y}} = -1 : \mathbf{w}^{\mathsf{T}} \mathbf{x} < 0$$

• Decision boundary: $\mathbf{w}^{\top}\mathbf{x} = 0$

Evaluating Predictions



Regression: can measure 'closeness' between label and prediction

- Song year prediction: better to be off by a year than by 20 years
- Squared loss: $(y \hat{y})^2$

Classification: Class predictions are discrete

• 0-1 loss: Penalty is 0 for correct prediction, and 1 otherwise

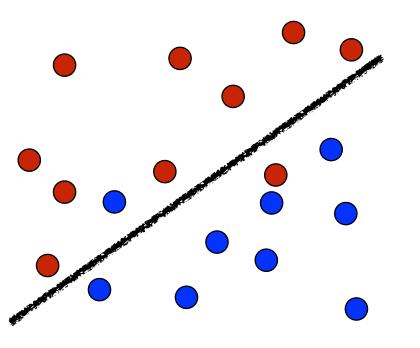
0/1 Loss Minimization

$$\ell_{0/1}(z) = \begin{cases} 1 & \text{if } z < 0 \\ 0 & \text{otherwise} \end{cases}$$

$$\mathbf{0-1}$$
 Let $y \in \{-1, 1\}$ and define $z = y \cdot \mathbf{w}^{\top} \mathbf{x}$

z is positive if y and $\mathbf{w}^{\top}\mathbf{x}$ have same sign, negative otherwise

How Can We Learn Model (w)?



Assume we have n training points, where $\mathbf{x}^{(i)}$ denotes the ith point

Recall two earlier points:

- Linear assumption: $\hat{y} = sign(\mathbf{w}^{\top} \mathbf{x})$
- We use 0-1 loss: $\ell_{0/1}(z)$

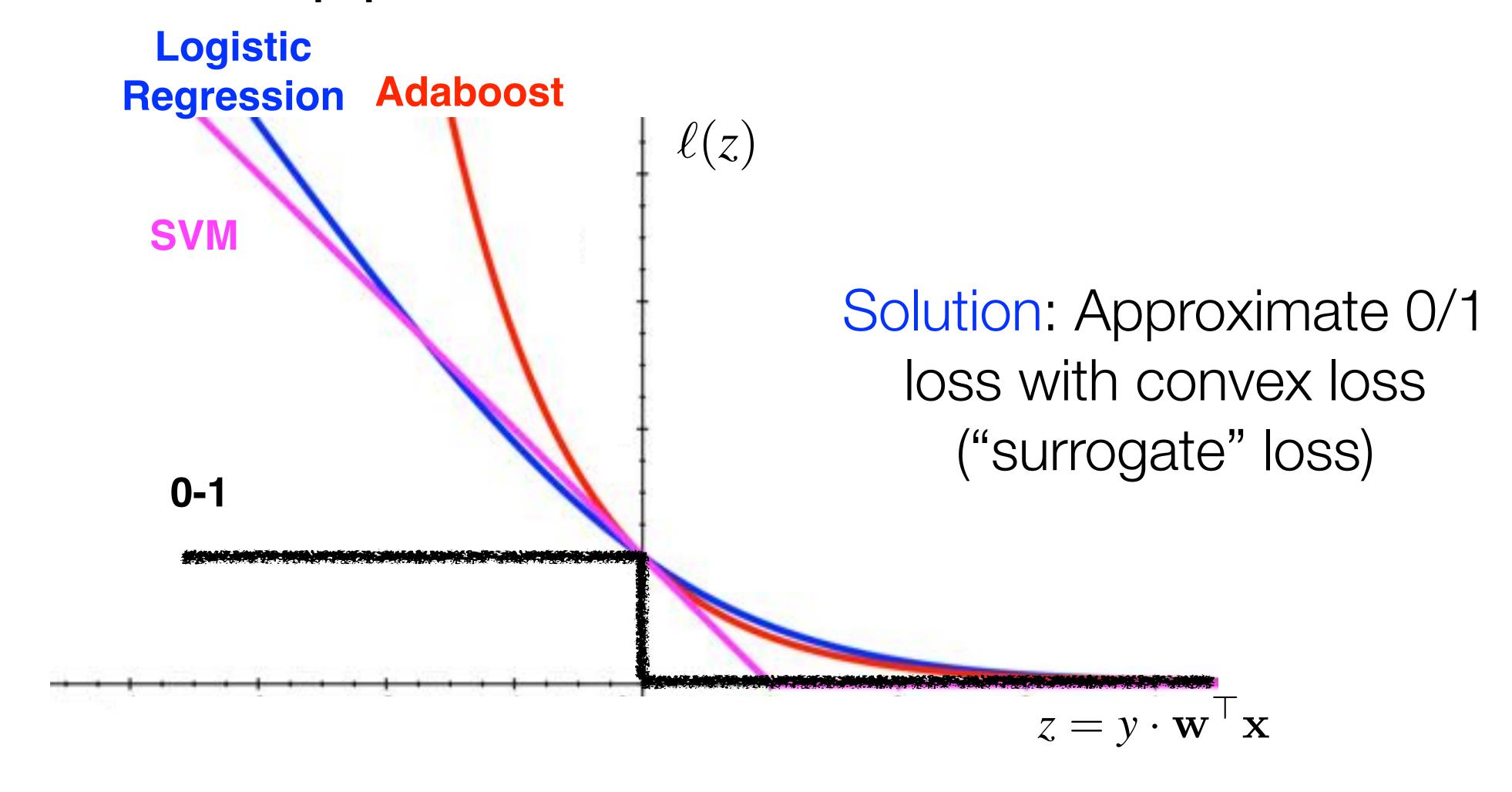
Idea: Find w that minimizes average 0-1 loss over training points:

$$\min_{\mathbf{w}} \sum_{i=1}^{n} \ell_{0/1} \left(y^{(i)} \cdot \mathbf{w}^{\top} \mathbf{x}^{(i)} \right)$$

0/1 Loss Minimization

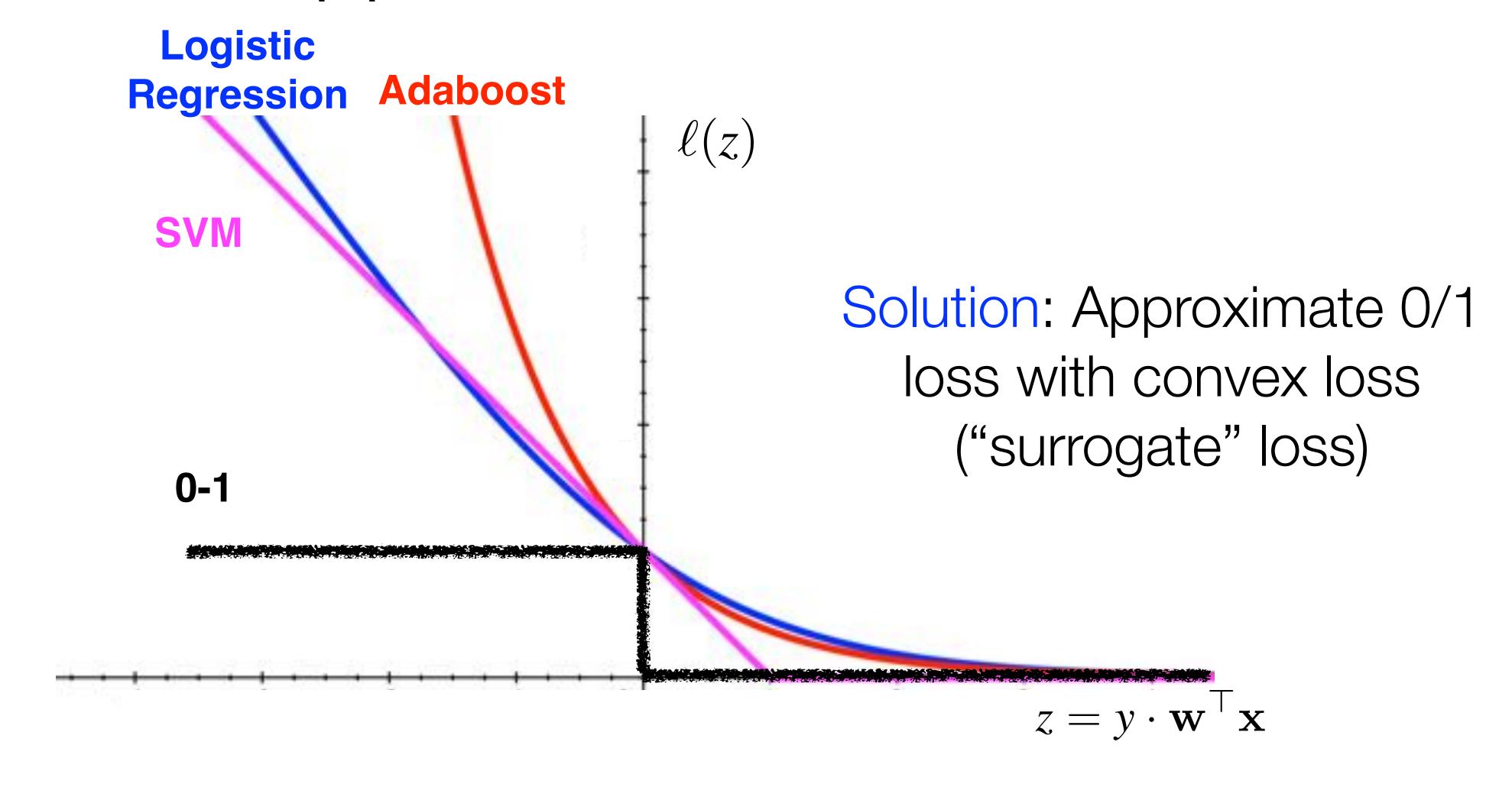
z is positive if y and $\mathbf{w}^{\top}\mathbf{x}$ have same sign, negative otherwise

Approximate 0/1 Loss



SVM (hinge), Logistic regression (logistic), Adaboost (exponential)

Approximate 0/1 Loss



Logistic loss (logloss): $\ell_{log}(z) = \log(1 + e^{-z})$

Logistic Regression Optimization

Logistic Regression: Learn mapping (w) that minimizes logistic loss on training data

$$\min_{\mathbf{w}} \sum_{i=1}^{n} \ell_{log} \left(y^{(i)} \cdot \mathbf{w}^{\top} \mathbf{x}^{(i)} \right)$$

- Convex
- Closed form solution doesn't exist

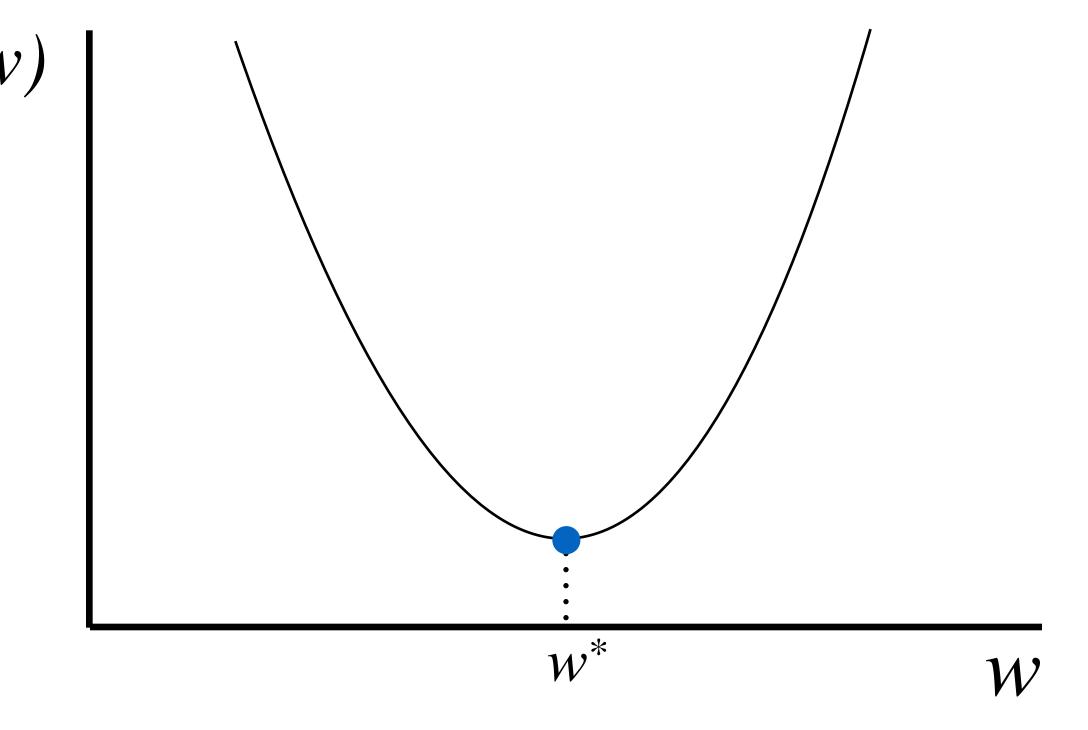
Logistic Regression Optimization

Goal: Find w* that minimizes

$$f(\mathbf{w}) = \sum_{i=1}^{n} \ell_{log} \left(y^{(i)} \cdot \mathbf{w}^{\top} \mathbf{x}^{(i)} \right)$$

Can solve via Gradient Descent

Step Size



Update Rule:
$$\mathbf{w}_{i+1} = \mathbf{w}_i - \alpha \nabla f(\mathbf{w})$$

$$\sum_{j=1}^n \left[1 - \frac{1}{1 + \exp(-y^{(j)} \mathbf{w}_i^\top \mathbf{x}^{(j)})} \right] \left(-y^{(j)} \mathbf{x}^{(j)} \right)$$

Gradient

Logistic Regression Optimization

Regularized

Logistic Regression: Learn mapping (w) that minimizes logistic loss on training data with a regularization term

$$\min_{\mathbf{w}} \sum_{i=1}^{n} \frac{1}{\ell_{log} \left(y^{(i)} \cdot \mathbf{w}^{\top} \mathbf{x}^{(i)} \right)} + \frac{\lambda ||\mathbf{w}||_{2}^{2}}{|\mathbf{w}||_{2}^{2}}$$

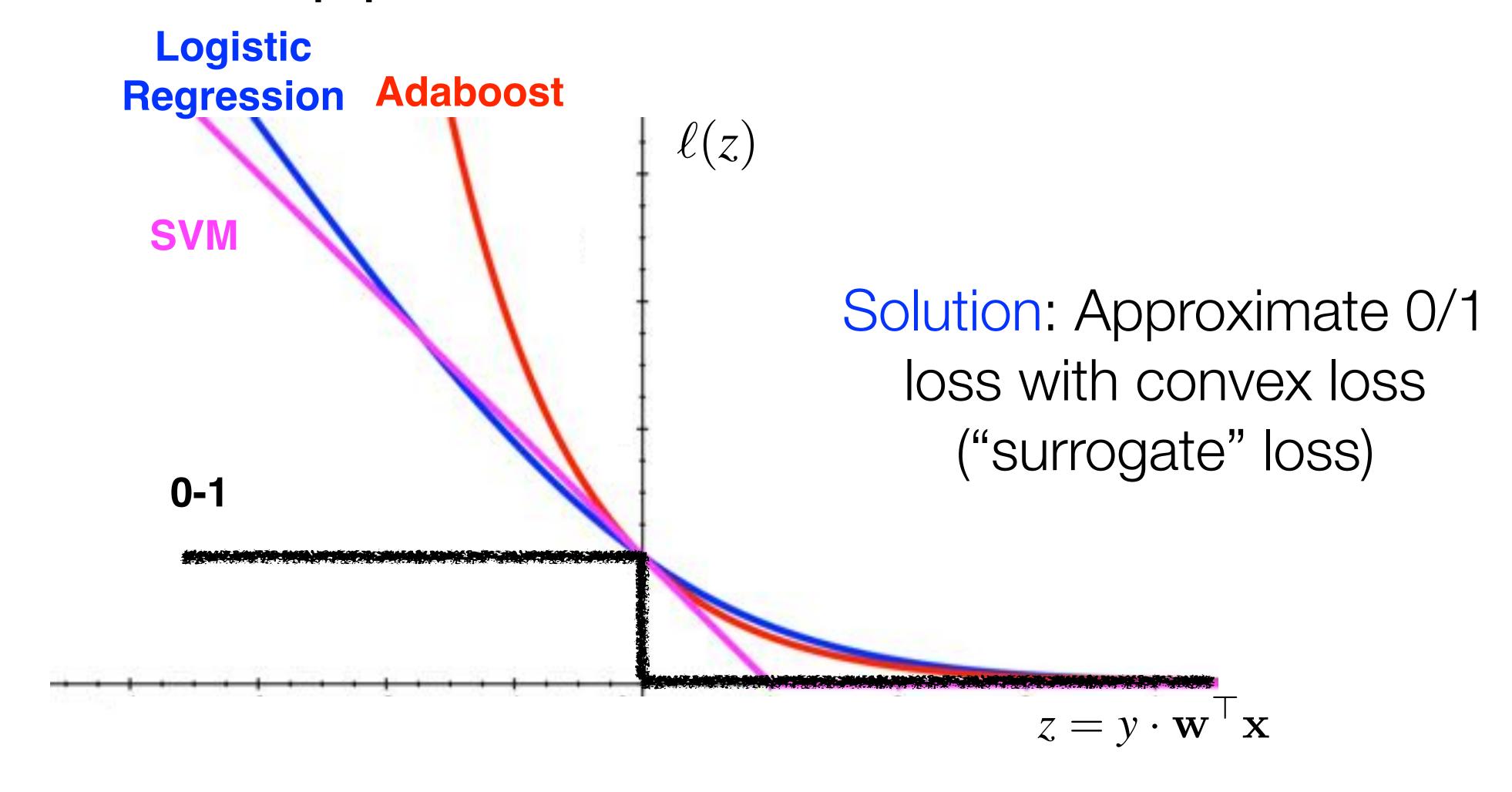
- Convex
- Closed form solution doesn't exist
- Can add regularization term (as in ridge regression)

Logistic Regression: Probabilistic Interpretation





Approximate 0/1 Loss



SVM (hinge), Logistic regression (logistic), Adaboost (exponential)

Probabilistic Interpretation

Goal: Model conditional probability: $\mathbb{P}[y=1 | \mathbf{x}]$

Example: Predict rain from temperature, cloudiness, humidity

- $\mathbb{P}[y = \text{rain} | t = 14^{\circ}F, c = LOW, h = 2\%] = .05$
- $\mathbb{P}[y = \text{rain} | t = 70^{\circ}\text{F}, c = \text{HIGH}, h = 95\%] = .9$

Example: Predict click from ad's **h**istorical performance, user's click **f**requency, and publisher page's **r**elevance

- $\mathbb{P}[y = \text{click} | h = \text{GOOD}, f = \text{HIGH}, r = \text{HIGH}] = .1$
- $\mathbb{P}[y = \text{click} | h = \text{BAD}, f = \text{LOW}, r = \text{LOW}] = .001$

Probabilistic Interpretation

Goal: Model conditional probability: $\mathbb{P}[y=1 | \mathbf{x}]$

First thought:
$$\mathbb{P}[y=1 | \mathbf{x}] \neq \mathbf{w}^{\top}\mathbf{x}$$

• Linear regression returns any real number, but probabilities range from 0 to 1!

How can we transform or 'squash' its output?

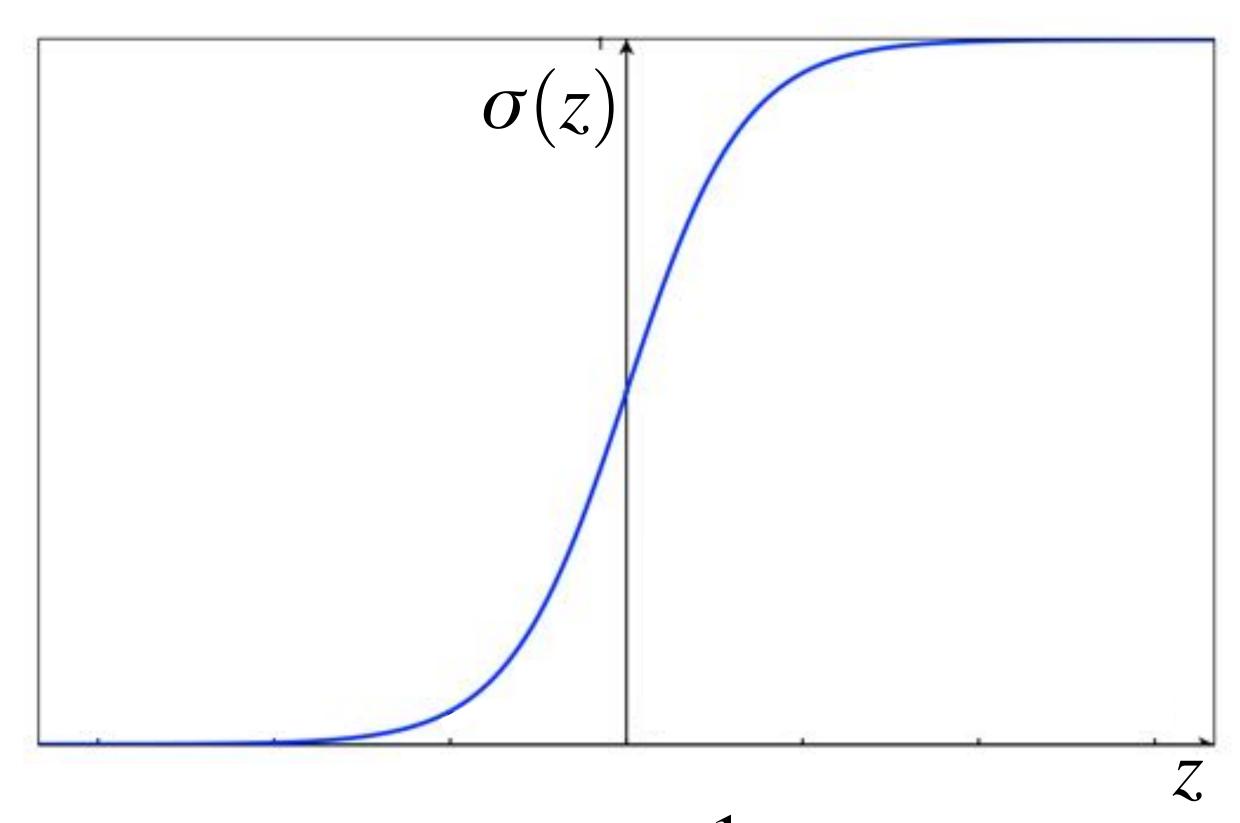
Use logistic (or sigmoid) function:

$$\mathbb{P}[y=1 \mid \mathbf{x}] = \sigma(\mathbf{w}^{\top}\mathbf{x})$$

Logistic Function

Maps real numbers to [0, 1]

- Large positive inputs $\Rightarrow 1$
- Large negative inputs $\Rightarrow 0$



$$\sigma(z) = \frac{1}{1 + \exp(-z)}$$

Probabilistic Interpretation

Goal: Model conditional probability: $\mathbb{P}[y=1 | \mathbf{x}]$

Logistic regression uses logistic function to model this conditional probability

- $\mathbb{P}[y = 0 \mid \mathbf{x}] = 1 \sigma(\mathbf{w}^{\mathsf{T}}\mathbf{x})$

For notational convenience we now define $y \in \{0, 1\}$

How Do We Use Probabilities?

To make class predictions, we need to convert probabilities to values in $\{0,1\}$

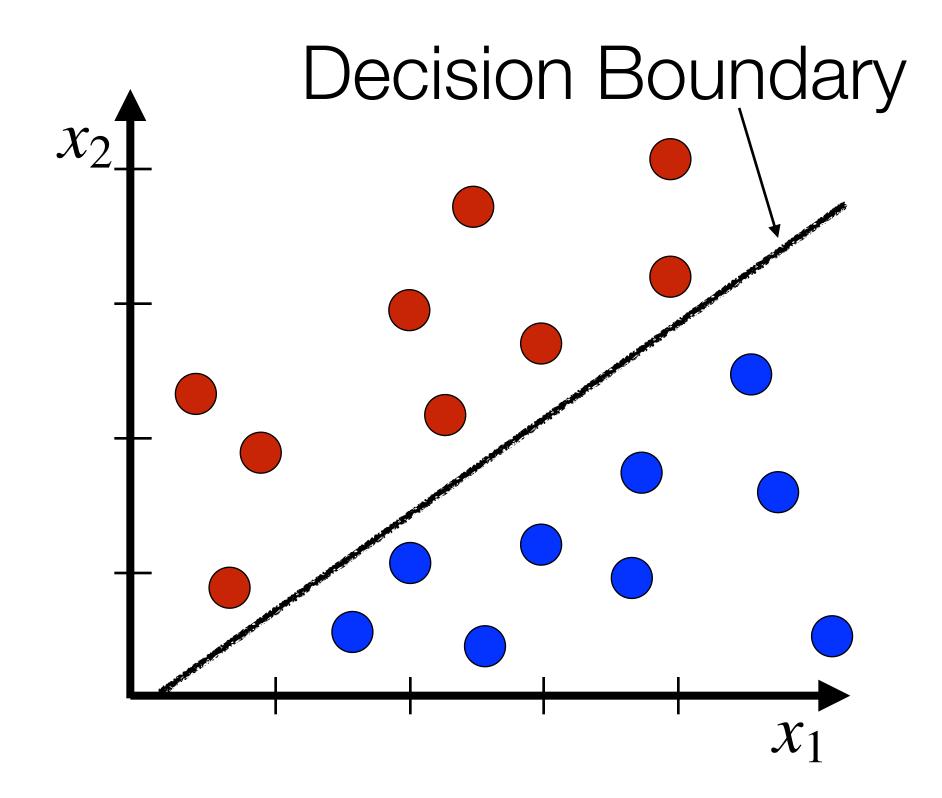
We can do this by setting a threshold on the probabilities

- Default threshold is 0.5

Example: Predict rain from temperature, cloudiness, humidity

- $\mathbb{P}[y = \text{rain} | t = 14^{\circ}F, c = LOW, h = 2\%] = .05$ $\hat{y} = 0$
- $\mathbb{P}[y = \text{rain} | t = 70^{\circ}\text{F}, c = \text{HIGH}, h = 95\%] = .9$ $\hat{y} = 1$

Connection with Decision Boundary?



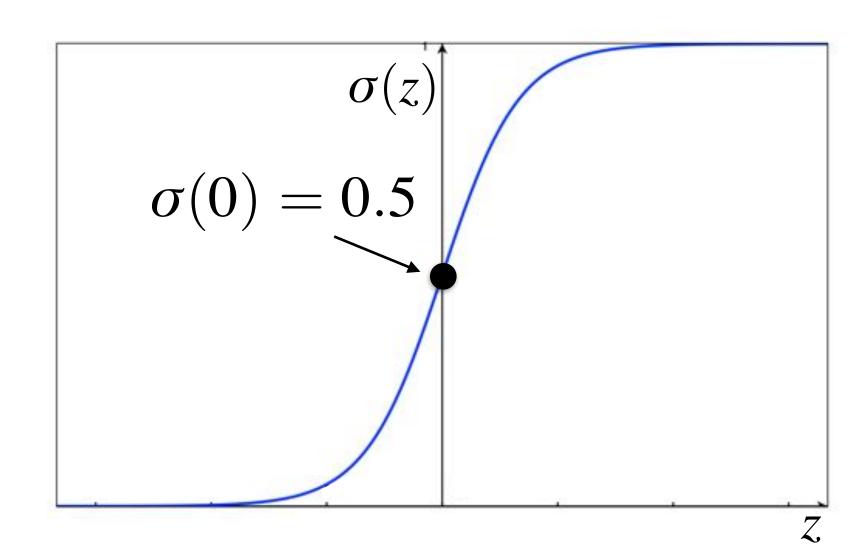
Threshold by sign to make class predictions: $\hat{y} = \text{sign}(\mathbf{w}^{\top}\mathbf{x})$

- $\hat{\mathbf{y}} = 1 : \mathbf{w}^{\mathsf{T}} \mathbf{x} > 0$
- $\hat{\mathbf{y}} = 0 : \mathbf{w}^{\mathsf{T}} \mathbf{x} < 0$
- decision boundary: $\mathbf{w}^{\top}\mathbf{x} = 0$

How does this compare with thresholding probability?

•
$$\mathbb{P}[y=1 \mid \mathbf{x}] = \sigma(\mathbf{w}^{\mathsf{T}}\mathbf{x}) > 0.5 \Longrightarrow \hat{y} = 1$$

Connection with Decision Boundary?



$$\mathbf{w}^{\mathsf{T}}\mathbf{x} = 0 \iff \sigma(\mathbf{w}^{\mathsf{T}}\mathbf{x}) = 0.5$$

Threshold by sign to make class predictions: $\hat{y} = \text{sign}(\mathbf{w}^{\top}\mathbf{x})$

- $\hat{\mathbf{y}} = 1 : \mathbf{w}^{\top} \mathbf{x} > 0$
- $\hat{\mathbf{y}} = 0 : \mathbf{w}^{\mathsf{T}} \mathbf{x} < 0$
- decision boundary: $\mathbf{w}^{\mathsf{T}}\mathbf{x} = 0$

How does this compare with thresholding probability?

- $\mathbb{P}[y=1 \mid \mathbf{x}] = \sigma(\mathbf{w}^{\mathsf{T}}\mathbf{x}) > 0.5 \Longrightarrow \hat{y} = 1$
- With threshold of 0.5, the decision boundaries are identical!

Using Probabilistic Predictions





How Do We Use Probabilities?

To make class predictions, we need to convert probabilities to values in $\{0,1\}$

We can do this by setting a threshold on the probabilities

- Default threshold is 0.5

Example: Predict rain from temperature, cloudiness, humidity

- $\mathbb{P}[y = \text{rain} | t = 14^{\circ}F, c = LOW, h = 2\%] = .05$ $\hat{y} = 0$
- $\mathbb{P}[y = \text{rain} | t = 70^{\circ}\text{F}, c = \text{HIGH}, h = 95\%] = .9$ $\hat{y} = 1$

Setting different thresholds

In spam detection application, we model $\mathbb{P}[y = \text{spam} \mid \mathbf{x}]$

Two types of error

- Classify a not-spam email as spam (false positive, FP)
- Classify a spam email as not-spam (false negative, FN)

Can argue that false positives are more harmful than false negatives

Worse to miss an important email than to have to delete spam

We can use a threshold greater than 0.5 to be more 'conservative'

ROC Plots: Measuring Varying Thresholds

ROC plot displays FPR vs TPR

- Top left is perfect
- Dotted Line is random prediction (i.e., biased coin flips)

Can classify at various thresholds (T)

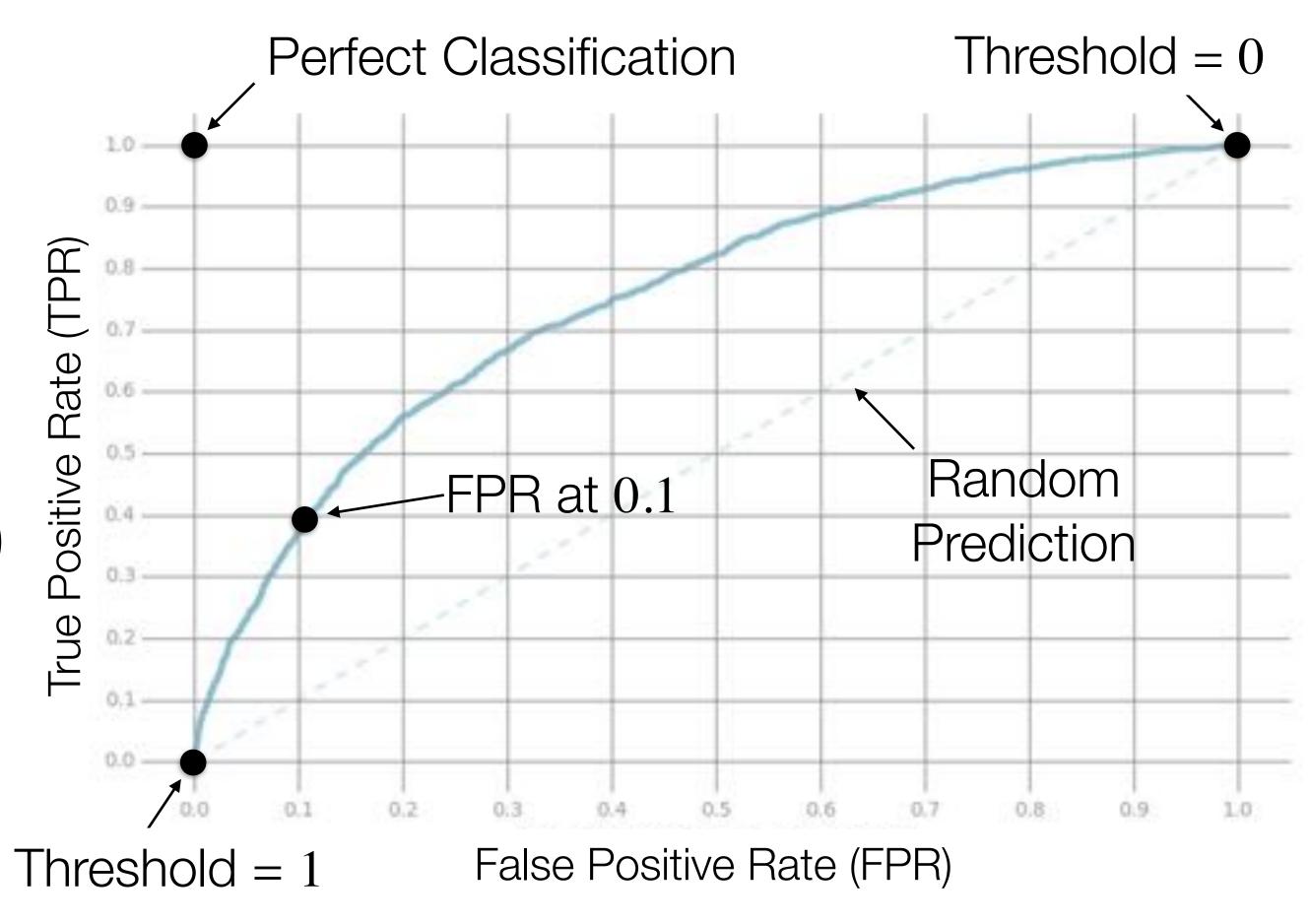
T = 0: Everything is spam

• TPR = 1, but FPR = 1

T = 1: Nothing is spam

• FPR = 0, but TPR = 0

We can tradeoff between TPR/FPR



FPR: % not-spam predicted as spam

TPR: % spam predicted as spam

Working Directly with Probabilities

Example: Predict click from ad's **h**istorical performance, user's click **f**requency, and publisher page's **r**elevance

- $\mathbb{P}[y = \text{click} | h = \text{GOOD}, f = \text{HIGH}, r = \text{HIGH}] = .1 \ \hat{y} = 0$
- $\mathbb{P}[y = \text{click} | h = \text{BAD}, f = \text{LOW}, r = \text{LOW}] = .001$ $\hat{y} = 0$

Success can be less than 1% [Andrew Stern, iMedia Connection, 2010]

Probabilities provide more granular information

- Confidence of prediction
- Useful when combining predictions with other information

In such cases, we want to evaluate probabilities directly

Logistic loss makes sense for evaluation!

Logistic Loss

$$\ell_{log}(p, y) = \begin{cases} -\log(p) & \text{if } y = 1\\ -\log(1 - p) & \text{if } y = 0 \end{cases}$$

When y = 1, we want p = 1

- No penalty at 1
- Increasing penalty away from 1

Similar logic when y = 0

