

# On the Joint Security of Encryption and Signature in EMV

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# Outline



- 1 Background on EMV
- 2 A New Attack on EMV
- 3 Positive Results
- 4 Concluding Remarks

# The EMV Standard

- EMV stands for Europay, Mastercard and VISA, and it is the **de facto global standard** for IC credit/debit cards – *Chip & PIN*.



- As of Q3 2011, there were more than 1.34 billion EMV cards in use worldwide.
- The standard specifies the inter-operation of IC cards with Point-Of-Sale terminals (POS) and Automated Teller Machines (ATM) .

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# EMV Cards



- EMV cards contain a 'Chip' which allows them to perform cryptographic computations.
- All EMV cards contain a **symmetric key** which they share with the Issuing Bank.
- Most cards are also equipped with **RSA keys** to compute signatures for card authentication and transaction authorization, and encrypt the PIN between the terminal and the card.
- The terminal authenticates the card's public keys through its copy of the brand's public key, and a **chain of certificates** which the card supplies.

# Transaction Flow



An EMV transaction progresses over three stages:

**Card Authentication:** Static Data Authentication (SDA),  
Dynamic Data Authentication (DDA/CDA).

**Cardholder Verification:** paper Signature, PIN – online/offline  
– encrypted/cleartext.

**Transaction Authorization:** A successful transaction ends with  
the card producing a **Transaction Certificate (TC)** – a MAC  
computed over the transaction details.

**CDA** cards additionally compute a **digital signature** over the  
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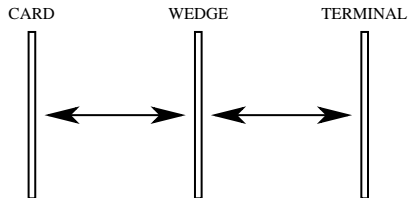


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# The Cambridge Attack

- At Oakland '10 the following **Wedge Attack** was presented, it allows an attacker to make transactions without the card's PIN.
- The wedge manipulates the communication between the card and the terminal so that the terminal believes PIN verification was successful, while the card thinks that a paper signature was used instead.



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- The wedge manipulates the communication between the card and the terminal so that the terminal believes PIN verification was successful, while the card thinks that a paper signature was used instead.
- The card's view of the cardholder verification is transmitted to the terminal in a format which it may not comprehend, and the attack can go undetected even during **online** and **CDA** transactions.
- The attack can easily be prevented, by ensuring that the terminal inspects the card's view of the cardholder verification.

# Our Contribution



- The EMV standard allows the **same RSA key-pair** to be used for both encryption and signature.
- Folklore dictates key separation, but sharing keys reduces processing and storage costs.
- No formal analysis exists that shows whether this is detrimental for the security of EMV or not.
- This is exactly the aim of our paper, we present an attack that exploits key reuse in EMV, together with positive results about upcoming versions of the standards.

# A New Attack on EMV



- Our attack exploits the reuse of RSA keys in an EMV card to allow an attacker to make transactions **without** the card's PIN.
- The attack is only applicable to a **CDA** card in an **offline** transaction.
- If the countermeasure against the Cambridge attack is in place our attack would still work!
- The attack builds on Bleichenbacher's attack against RSA with PKCS#1 encoding (CRYPTO '98).

# The Bleichenbacher Attack



- PKCS#1 v1.5 specified that the plaintext be encoded as:

$$m = 00 \parallel 02 \parallel \text{Padding String} \parallel 00 \parallel \text{Data}$$

- Assume access to a ciphertext-validity oracle **Valid**(·).
- If **Valid**( $c$ ) then  $2B \leq m < 3B$ , where  $B = 2^{8(k-2)}$ .
- Using the multiplicative homomorphism of RSA, it is possible to construct a sequence of related ciphertexts such that:
  - a Each ciphertext is valid with probability one half.
  - b Each valid ciphertext found, narrows down the range by half.
- For a 1024-bit RSA modulus, roughly a **million** oracle queries are required to recover  $m$  (due to setup overheads).



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# PIN Encryption in EMV



- The encoding used in EMV for PIN is encryption is as follows:

**7F || PIN Block || ICC Challenge || Random Padding**

where the PIN block and the ICC Challenge are 8 bytes long.

- Upon decryption the card performs 3 checks:
  - a Is the ICC Challenge equal to the one it produced?
  - b Is the Header byte equal to '7F'?
  - c Does the PIN in the PIN Block match the one stored in the card?
- If test **b** is carried out first, and its success or failure can be distinguished (**e.g. Timing or Power Analysis**), then a Bleichenbacher-style attack is possible.

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# Bleichenbacher's Attack in EMV



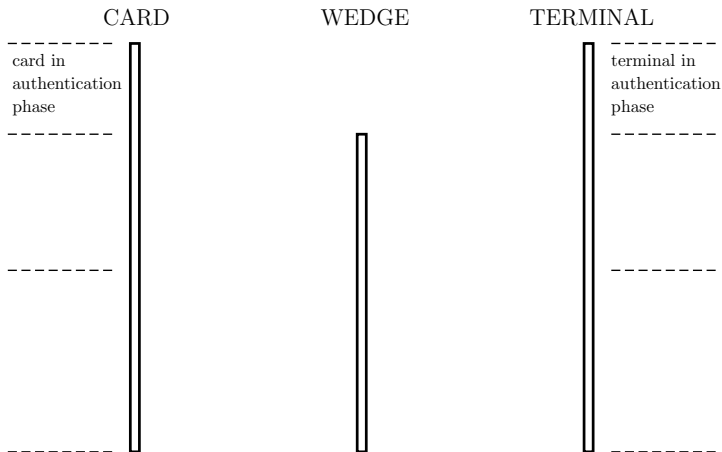
- View Bleichenbacher's attack as a black box, which when given a valid ciphertext  $c$  and access to a ciphertext-validity oracle recovers the underlying (encoded) message  $m$ .
- Alternatively we can view  $m$  as the signature of some message whose **encoding** is  $c$ , since  $m = c^d \bmod N$ .
- Thus when a single key pair is used, Bleichenbacher's attack allows us to sign messages whose encodings happen to be also valid ciphertexts.
- In order to sign an arbitrary encoded message  $\mu$ , we blind it with an integer  $\rho$  such that  $\rho^e \mu$  is a valid ciphertext.

$$\text{Sign}(\mu) = \rho^{-1} c^d \bmod N$$

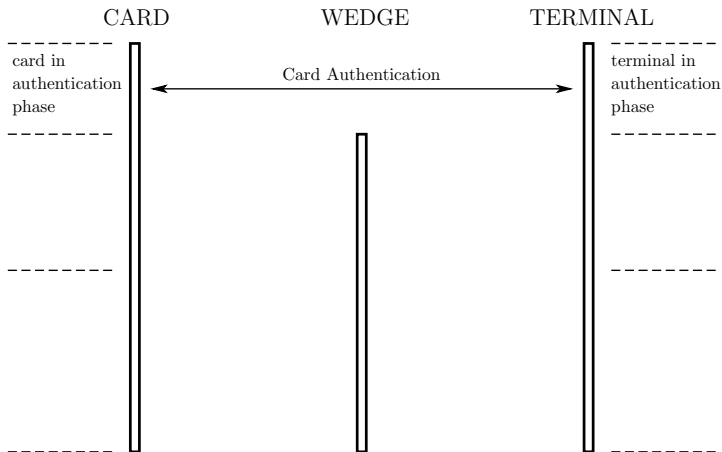
# The Attack on a CDA Transaction



Royal Holloway  
University of London  
Information Security Group

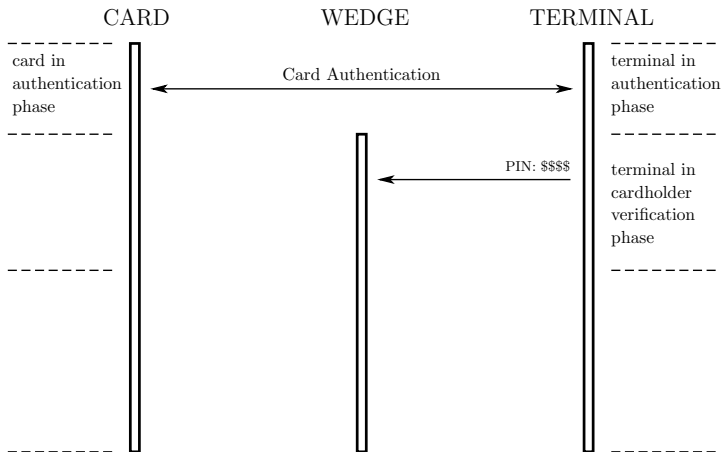


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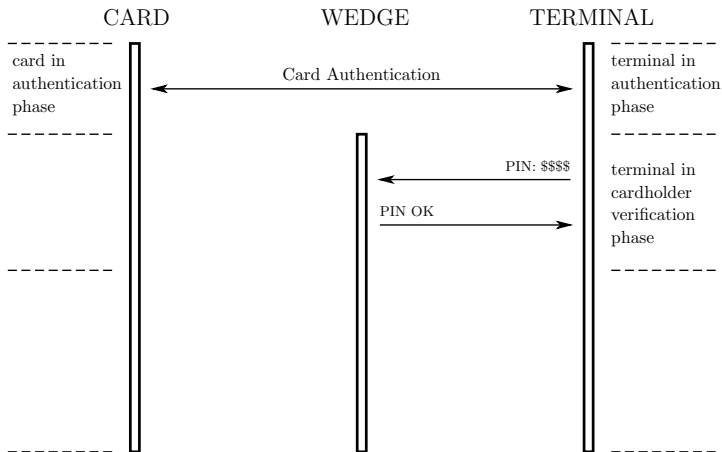




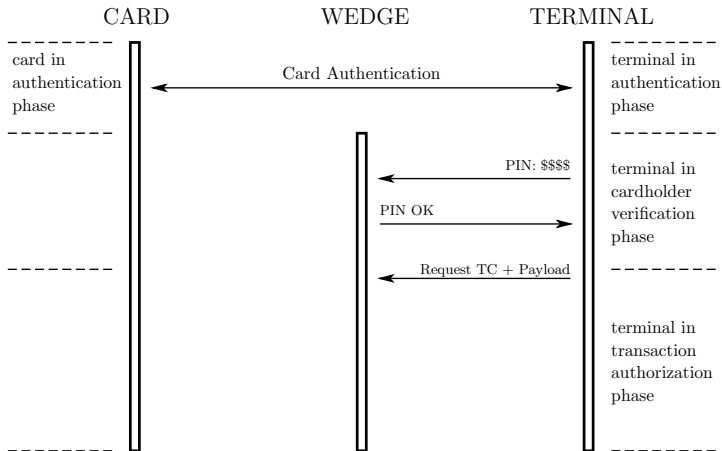
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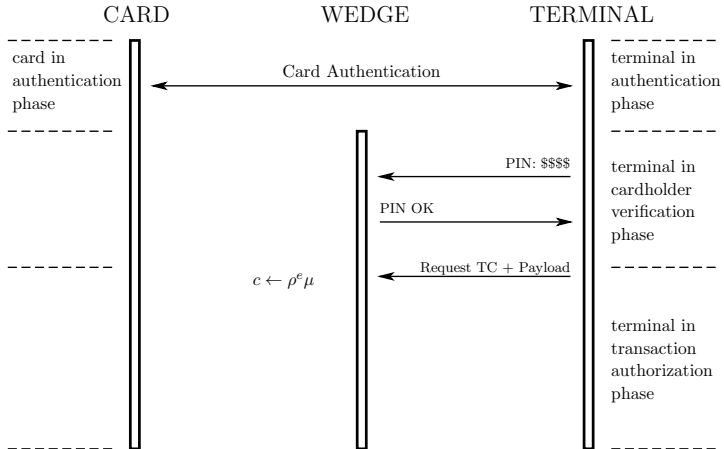
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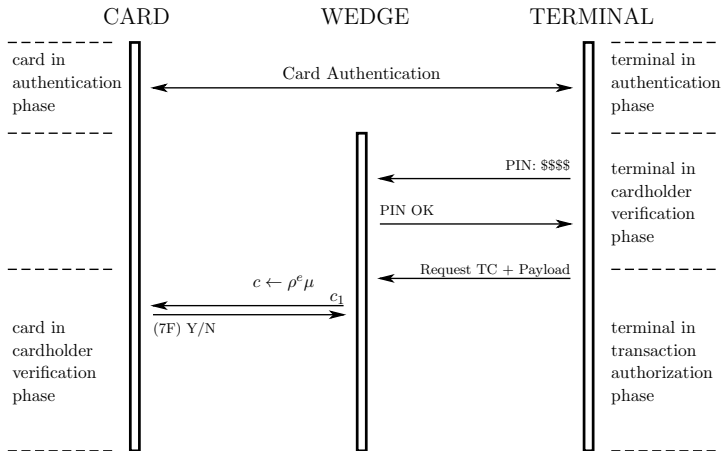
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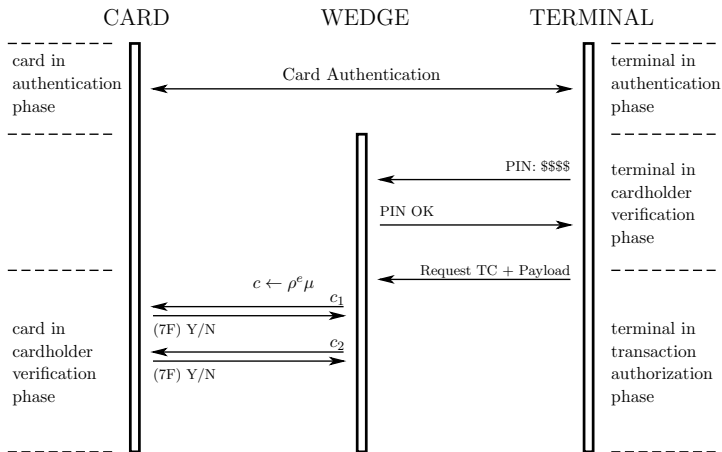
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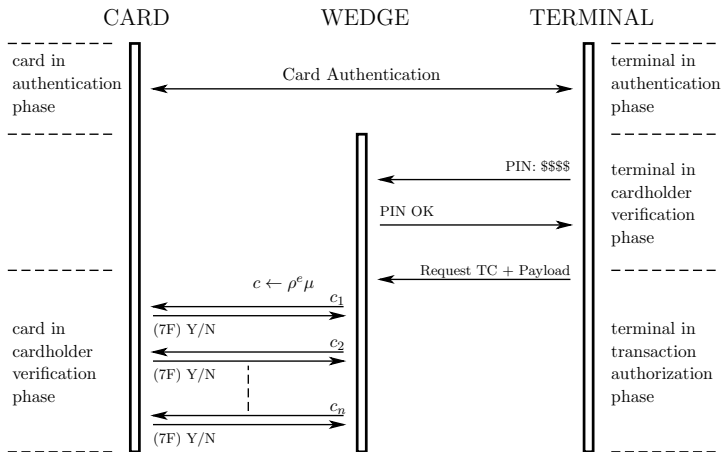
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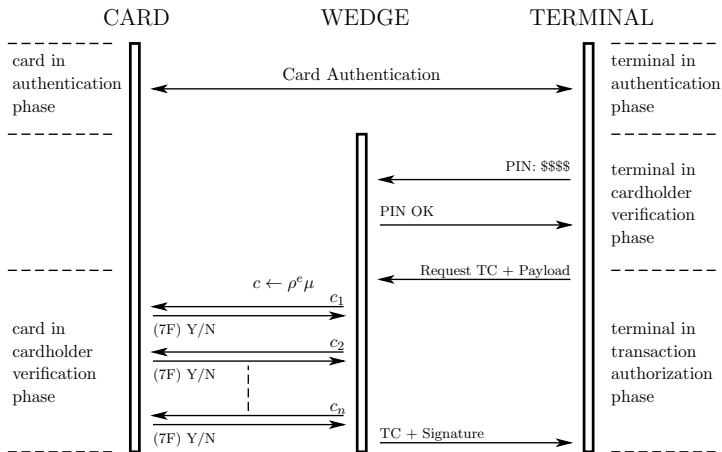
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# Practical Considerations



- We stress that we did not implement the attack in practice.
- Because the header is only 1 byte long, for a 1024-bit RSA modulus we need roughly **2000** queries to forge a signature.
- EMV cards may maintain both a **PIN try** counter and a **decryption failure** counter. Our attack would not affect the PIN try counter. In the EMV CPA specification the latter is specified to be a 2-byte counter.
- Other factors such as transaction time-outs and the inability to reproduce the '7F' oracle may limit the practicality of our attack.

# On the Positive Side



- EMV Co is considering to adopt elliptic curve based algorithms in future versions of the EMV standards.
- More specifically, to use:
  - ECIES (ISO/IEC 18033-2) for PIN encryption.
  - EC-DSA or EC-Schnorr (ISO/IEC 14888-3:2006) to compute digital signatures.
- We show that the two resulting configurations are **jointly secure**, meaning that the security of the individual constituent schemes still holds when they share the same key pair.

# Joint Security



- We define a **combined scheme**:

(KGen, Sign, Verify, KEM.Enc, KEM.Dec)

- EUF-CMA security is augmented by giving the adversary additional access to a decapsulation oracle.
- Similarly IND-CCA security is extended by giving the adversary additional access to a signing oracle.
- A combined scheme is jointly secure if it is **both** EUF-CMA secure in the presence of a decapsulation oracle, and IND-CCA secure in the presence of a signing oracle.

# ECIES + EC-Schnorr

In the Random Oracle Model:

Result	Scheme	Security	Assumptions
1	ECIES-KEM	IND-gCCA	gap-DH
2	EC-Schnorr	EU-F-CMA	DLP
New	Combined Scheme	Joint Security	gap-DH, gap-DLP

[1] Abdalla, Bellare and Rogaway. *CT-RSA 2001*

[2] Pointcheval and Stern. *J. Cryptology 2000*

## ECIES + EC-DSA

Assuming the group is ideal (Generic Group Model):

Result	Scheme	Security	Assumptions
3	ECIES-KEM	IND-CCA	DDH, KDF <sup>†</sup>
4	EC-DSA	EUFCMA	$f_{conv}^{\ddagger}$ , Hash <sup>†§</sup>
New	Combined Scheme	Joint Security	DDH, $f_{conv}^{\ddagger}$ , Hash <sup>†§</sup>

[3] Smart. *Coding and Cryptography 2001*

[4] Brown. *Advances in Elliptic Curve Cryptography 2005*

<sup>†</sup>Uniform

<sup>‡</sup>Almost Invertible

<sup>§</sup>Collision Resistant and Zero-Finder Resistant

# Conclusions



- Our attack illustrates the problems in reusing the same key-pair for encryption and signature in the current EMV standards.
- We show that the security of the individual EC-based schemes extends to the **joint setting** under the same assumptions.
- Thus for the elliptic curve based schemes under consideration, one can 'reuse keys' and gain substantial efficiency benefits while retaining a similar security margin.



# New Constructions of Efficient Simulation-Sound Commitments Using Encryption and Their Applications

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NTT Information Sharing  
Platform Laboratories

Session ID: **CRYP-202**

Session Classification: Advanced

**RSACONFERENCE2012**

# Quick Overview

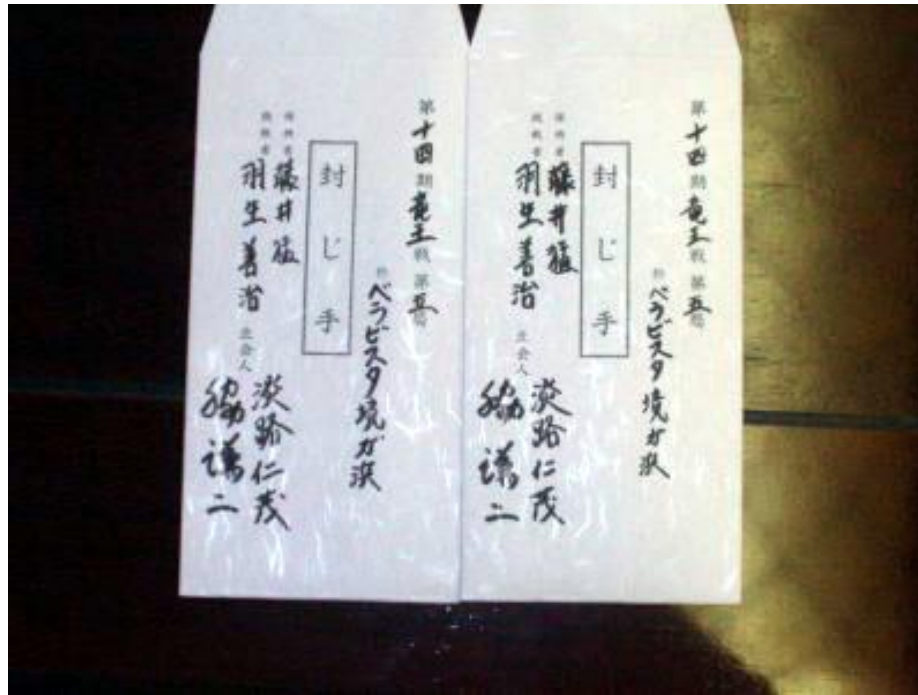
- New frameworks for constructing simulation-sound trap-door commitments (SSTCs)
  - 2-move and 5-move
- Efficient instantiations
  - 2-move assuming CDH in bilinear group.
  - 5-move assuming Factoring.
- What is strong and weak?
  - Strong: ***Tight*** reduction to ***weak (good)*** assumptions.
    - Implies efficient instantiations in the same security level.
  - Weak: Require ***Interactions*** (2-move or 5-move)
    - Previous Works : non-interactive = 1-move





# Commitments

In a *Shogi* game (a Japanese traditional board game)



# Commitments

We focus on commitments in the common reference string model.

CRS: common reference string



Alice

secret

$$x \in \{0,1\}^*$$

$r$  : randomness

*Commit Phase*

$$c = \text{Com}(x; r)$$



Bob

Hiding :

Bob does get no information about secret  $x$  in the commit phase.

*Open Phase*

$$(x, r)$$



$$\begin{matrix} ? \\ c = \text{Com}(x; r) \end{matrix}$$

Binding :

Alice cannot open  $c$  in a different way.



# Why we study SSTCs ?

Simulation-sound trap-door commitments are a key ingredient.

- **SSTCs**  $\rightarrow$  cNMo commitments [MY04]
  - cNMo: concurrent non-malleable w.r.t. opening
- $\Sigma$ -protocols + **SSTCs**  $\rightarrow$  cNM ZK PoKs [Gen04]
  - cNM: concurrent non-malleable
- $\Omega$ -protocols + **SSTCs**  $\rightarrow$  UC ZKs [GM03,MY04]
  - UC: universally composable
- Mix commitments + **SSTCs**  $\rightarrow$  UC commitments [DN02,DG03]
  - Notes: UC commitments  $\rightarrow$  any UC 2-party and multi-party computation.



# Agenda

- SSTC = TC + SS binding
  - Trap-door commitment (TC)
  - Simulation-Sound Binding
- $\Sigma$ -protocols implies TC
- Previous Construction of SSTC
- New frameworks from Encryption (Tag-KEMs)
  - Idea
  - 2 and 5-move Instantiations
- Comparison



# Trap-door Commitments

Simulator



CRS: common reference string



secret  $x \in \{0,1\}^*$   
Trap-door key:  $tk$

w/  $(x, r)$

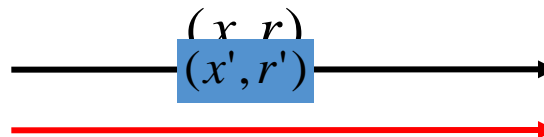
*Commit Phase*

$$c = \text{Com}(x; r)$$



Simulator can open  
commitment to **any**  $x'$ .

*Open Phase*



$$\begin{aligned} c &= \text{Com}(x; r) \\ c &= \text{Com}(x'; r') \end{aligned}$$

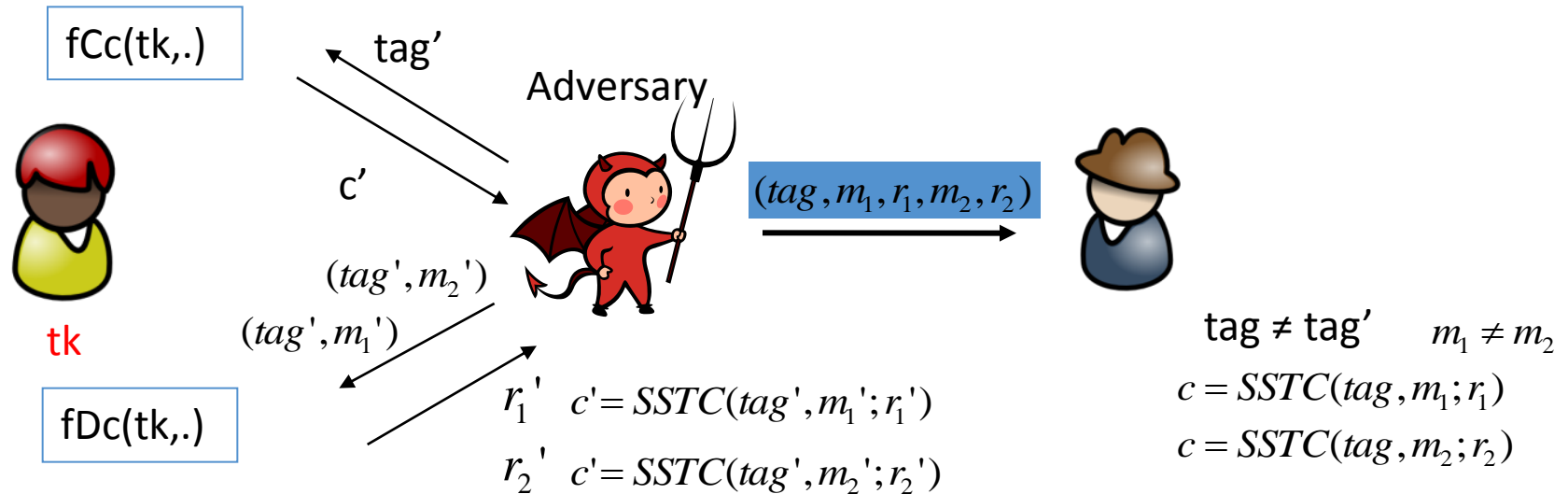
Ex. Pedersen's Commitment:

$$\text{CRS} = \{g, h\} \quad tk = \{s\} \quad \text{s.t.} \quad h = g^s \quad r' = (x - x')/s + r \quad c = g^x h^r = g^{x'} h^{r'}$$



# Simulation-Sound (SS) TCs

Simulation-sound binding: Adv is negl. in the following game



$$\text{Adv}_{A, \text{SSTC}}^{\text{ss-bind}}(n) \triangleq$$

$$\Pr \left[ \begin{array}{l} (pk, tk) \leftarrow \text{TKGen}(1^n); \\ (tag, m_1, m_2, r_1, r_2, c) \leftarrow A^{fCc_{tk}, fDc_{tk}}(pk) : \\ c = \text{SSTC}(pk, tag, m_1, r_1) = \text{SSTC}(pk, tag, m_2, r_2) \\ \wedge (m_1 \neq m_2) \wedge tag \notin Q \end{array} \right],$$



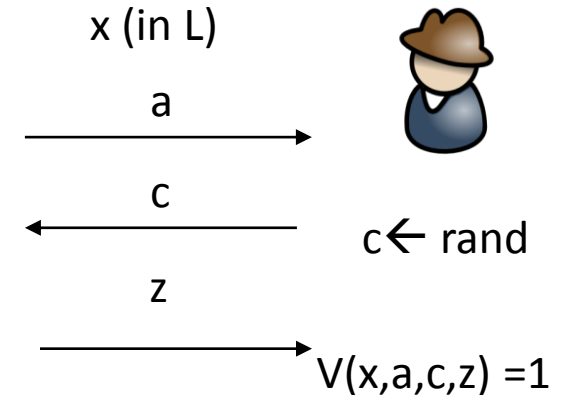
# $\Sigma$ -protocol implies TC [FS89,90]

- $\Sigma$ -protocol on language L.

- $x$ : an instance in L;  $w$ : a witness of  $x$ .
- 3-move public-coin HVZK
- Completeness
- Special soundness
- Special honest verifier ZK
  - $(a, z) \leftarrow \text{Sim}\Sigma(x, c)$



$w$ : witness



- Trap-door commitment (TC) derived from  $\Sigma$ -protocol on L

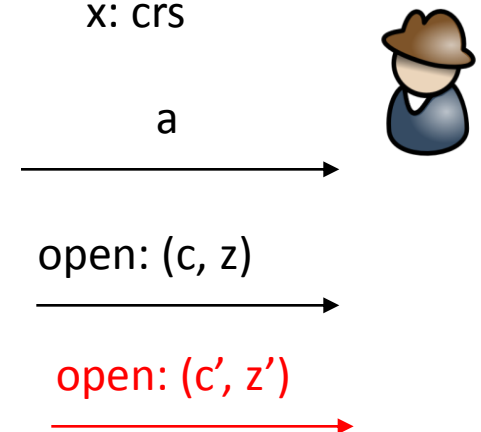
- $x$  (in L): common reference string.
- $c$ : message (a challenge in  $\Sigma$ )
- $a$ : commitment to  $c$ , where  $(a, z) \leftarrow \text{Sim}\Sigma(x, c)$ .

Prover in TC  
 $\equiv$  Simulator in TC  
 $\equiv$  Simulator in  $\Sigma$   
 $\equiv$  Prover in  $\Sigma$



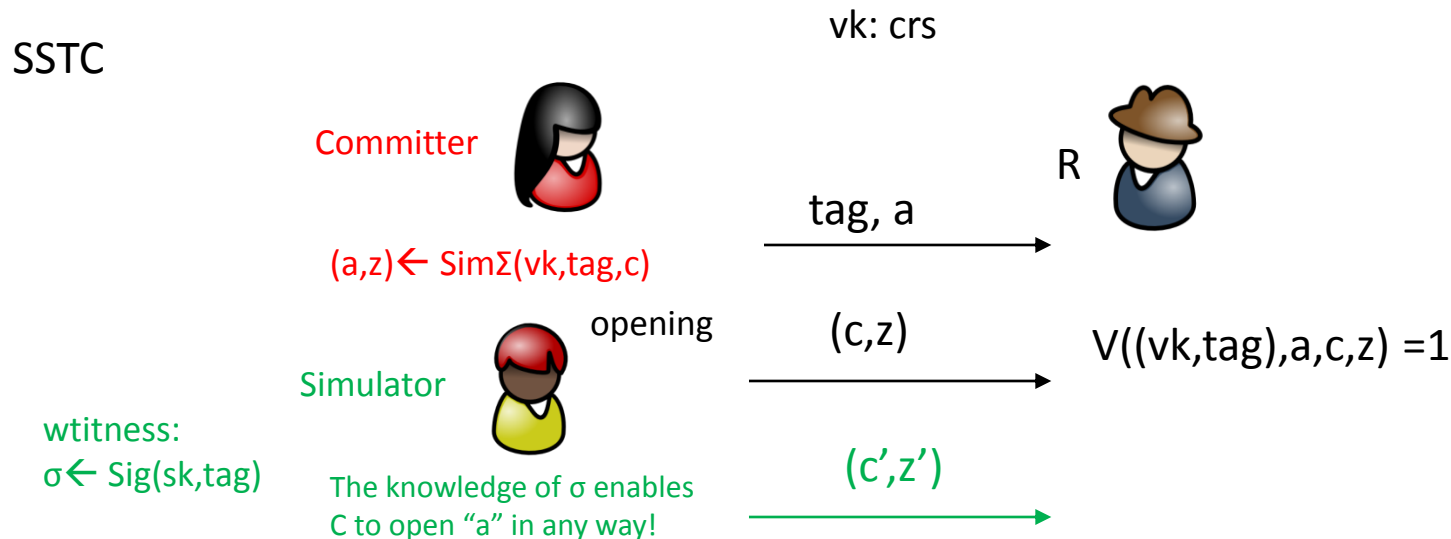
$(a, z) \leftarrow \text{Sim}\Sigma(x, c)$

$x$ : crs



# Previous framework for SSTC [MY04]

- Assume a  $\Sigma$ -protocol such that the prover knows signature  $\sigma$  on “tag”.
- Commit Phase:
  - Committer: Running the simulator instead of the real  $\Sigma$  protocol. Then send the first message “a” of the simulator. Note that he does not know  $\sigma$ ; Hence, he commits to challenge “c”.
  - Simulator (with  $\sigma$ ) : Running the real  $\Sigma$ -protocol such that he knows signature  $\sigma$ . Then send the first message “a” of the  $\Sigma$ -protocol.
- Open Phase:
  - Committer: Send  $(c,z)$ .
  - Simulator (with  $\sigma$ ): Open “a” to any value  $c'$  with  $z'$  by using witness  $\sigma$ .





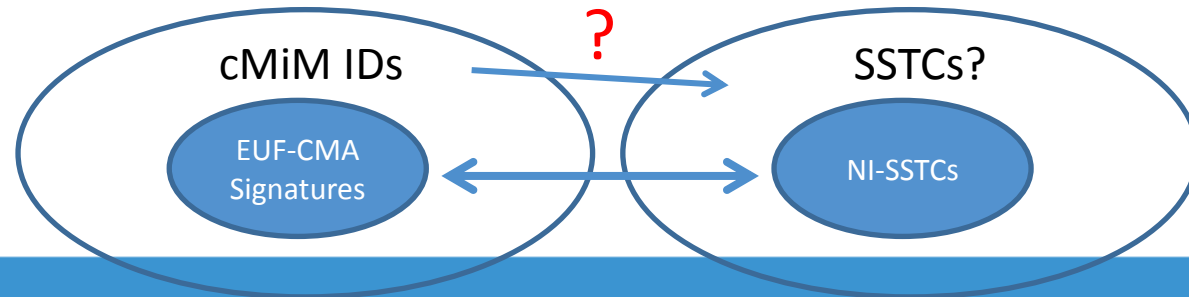
# Previous Work (SSTC)

- Using the same framework --- running the simulator of  $\Sigma$ -protocol such that a committer knows a EUF-CMA signature on tag.
  - GMY03: DSA sig. / DSA assumption
  - MY04, Groth03: Cramer-Shoup sig / strong RSA assumption
  - Gen04: BB short sig. / qSDH assumption.
  - DSW08: Waters sig. / CDH assumption
  - NFT10: HW'09 sig. / RSA assumption
- Weakness:
  - The previous schemes have at least one of the following weakness:  
**Strong assumption, loose reduction, or lack of efficiency**
    - Q: The weakness mainly comes from the weakness of digital signatures. So, what's if starting with Waters dual-system based signatures based on DLIN with a tight reduction ?
    - A: It depends on whether the dual-system signature has an efficient  $\Sigma$ -protocol. Still, the resulting scheme has at least 7 group elements! Not so practical



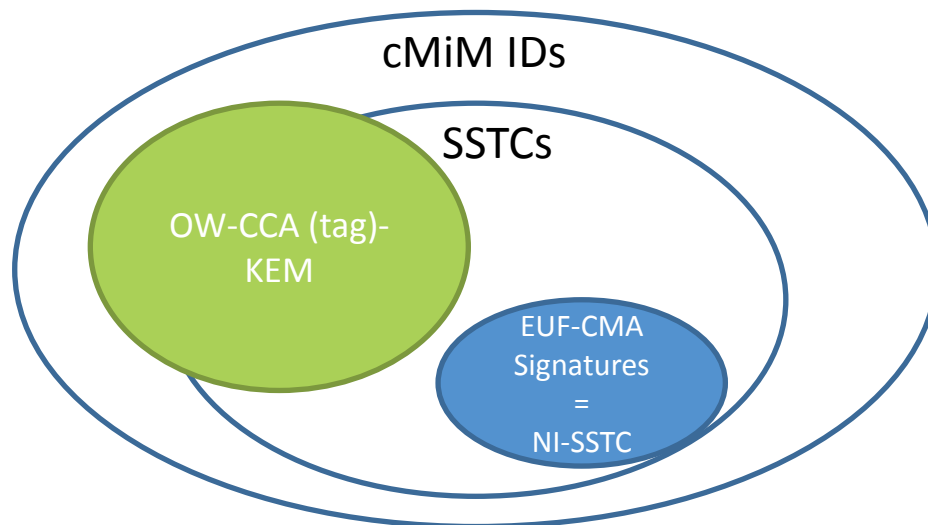
# Consider More Efficient Constructions

- Forget non-interactive (NI) SSTCs
  - EUF-CMA signatures imply NI-SSTCs and *vice versa*.
    - Therefore, constructing an efficient NI SSTC is at least as difficult as constructing an efficient EUF-CMA signature scheme.
- Can we bypass signature schemes ?
  - Observation: EUF-CMA sigs imply cMiM IDs.
  - *So, what if starting with (interactive) cMiM identifications?*



# Relation between cMiM IDs and SSTCs

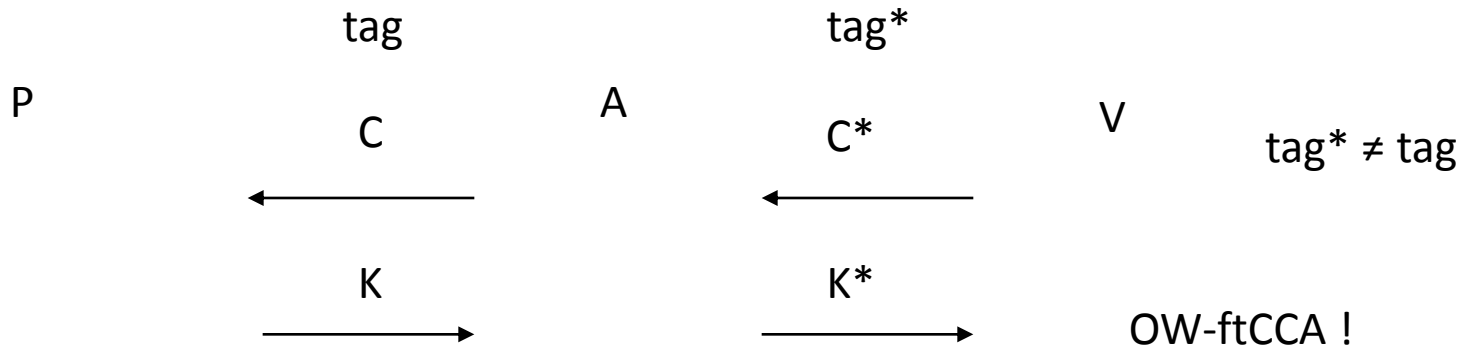
- By observation, SSTCs  $\rightarrow$  cMiM IDs
  - The opposite direction (cMiM IDs  $\rightarrow$  SSTCs) is not known. Maybe false.
- By observation, OW-CCA PKE (or tag-KEM)  $\rightarrow$  cMiM IDs
  - Which paper mentioned it first ? Implicitly, [DDN91]? Explicitly, at least [BFGM01], [AA11] and this work.
- This Work: OW-CCA (tag) KEM + *some conditions*  $\rightarrow$  SSTCs



# cMiM secure ID from OW-ftCCA Tag-KEM

$$\begin{array}{lcl}
 P(pk, sk, tag) & & V(pk, tag) \\
 & \xleftarrow{C} & (C, K) \leftarrow \text{Enc}(pk, tag) \\
 K' := \text{Dec}(sk, tag, C) & \xrightarrow{K'} & \text{accepts if and only if} \\
 & & K' = K
 \end{array}$$

cMiM Attack



# Top-level Idea: SSTC from Tag-KEM

pk: crs

Committer



$(a, z) \leftarrow \text{Sim}\Sigma(\text{pk}, \text{tag}, C, m)$   
as if she knows  $K$  (but she  
does not know  $K$ ).

Receiver



$(C, K) \leftarrow \text{Enc}(\text{pk}, \text{tag})$

$C$

$a$

Apparently good, but what if the receiver sends a fake ciphertext  $C$ ?  
Then, there is no  $K$ , which implies that the trap-door property is destroyed!



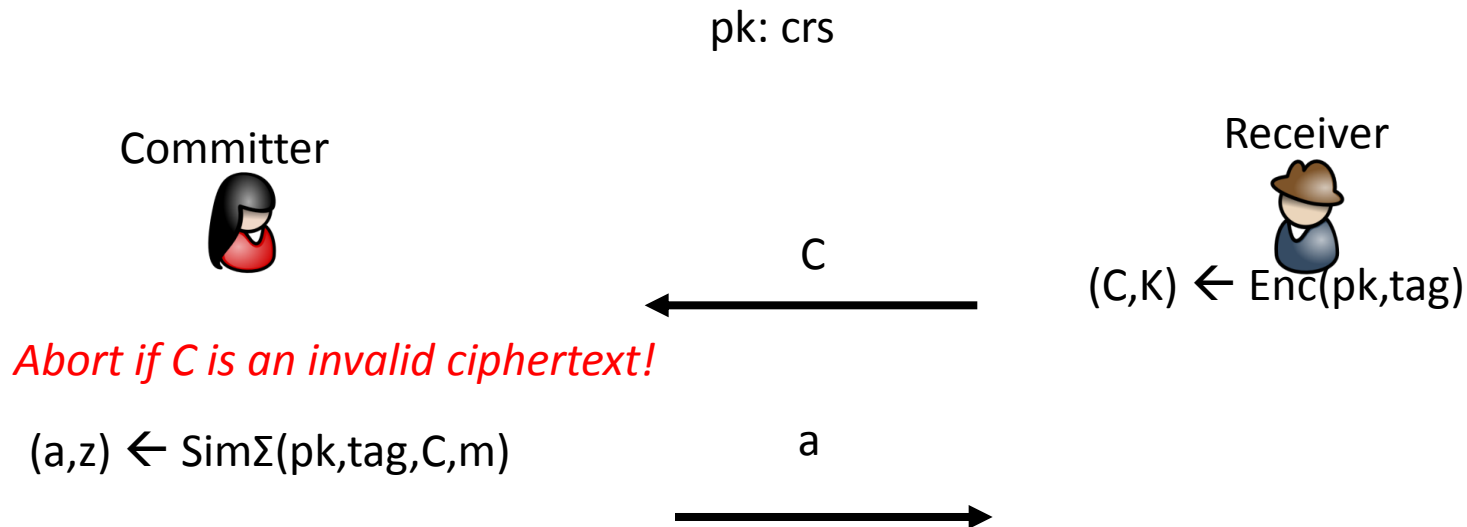
sk

The simulator extracts  
 $K = \text{Dec}(\text{sk}, \text{tag}, C)$  and opens “ $a$ ”  
to any  $m'$  with  $z'$ !

$\forall m', (m', z')$



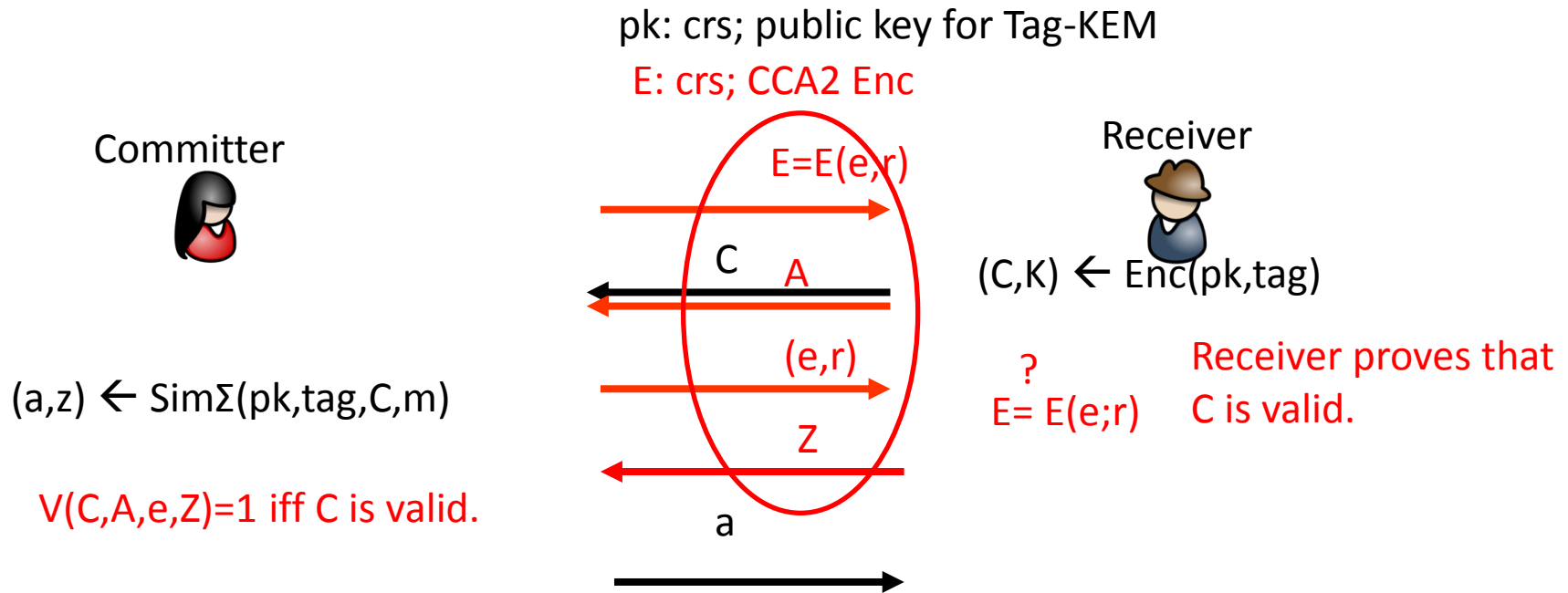
## 2-move SSTC from **publicly-verifiable** Tag-KEM



*Indeed, such publicly-verifiable Tag-KEMs exist based on CDH assumption in bilinear groups" [Kiltz06, Wee10]*



# Trial: SSTC from *non-publicly-verifiable* Tag-KEM



# We need cNM ZK on $L=\{C \mid C \text{ is a valid ciphertext}\}$

pk: crs; public key for Tag-KEM  
E:crs; CCA Enc

Committer (Verifier)



$E=E(e;r)$



Receiver (Prover)



witness R

s.t.  $(C,K) \leftarrow \text{Enc}(\text{pk}, \text{tag}; R)$

$(e,r)$



?  
 $E= E(e;r)$

$V(C,A,e,Z)=1?$



$(A,e,Z)$  is an output of  $\Sigma$ -protocol on common instance C

Concurrent ZKness: OK due to CCA ENC E and  $\Sigma$ -protocol.  
*Soundness: does not hold for an arbitrary  $\Sigma$ -protocol.*





# Wait..

We need cNM ZK in order to construct a SSTC, but cNM ZKs (POK) are usually constructed from SSTCs ...



We do not need cNMZK *Proof of knowledge*, but cNMZK on language. In addition, we only require cNMZK on a special language such that  $L = \{C \mid C \text{ is a valid ciphertext}\}$ .

If Tag-KEM has a special kind of  $\Sigma$ -protocol, denoted *weak extractable  $\Sigma$ -protocol*, then we can prove that the protocol above is cNMZK.

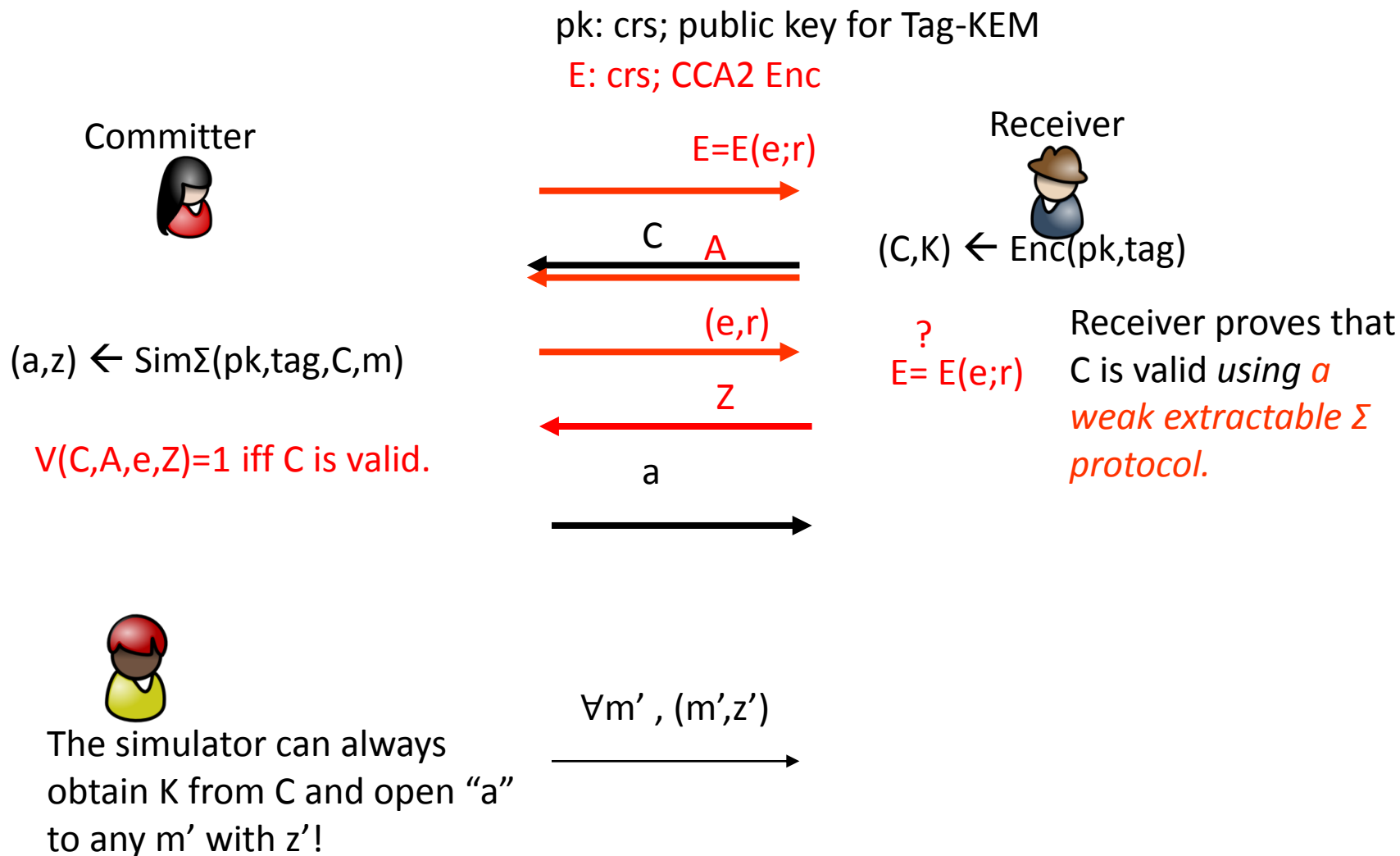


# Weak Extractable Sigma Protocols

- Note that in a  $\Sigma$ -protocol, *if  $x$  not in  $L$* , the first message of simulation “ $a$ ” is a statistically-binding commitment to *challenge “ $c$ ”*.
  - Namely, “ $c$ ” is uniquely determined.
- Informally, a weak extractable  $\Sigma$  protocol is a special  $\Sigma$  protocol in the CRS model, where additionally,
  - Every  $x$  not in  $L$ , every “ $a$ ”, and every “ $c$ ”, one can easily *check* whether there is “ $z$ ” such that  $V(\text{crs}, a, e, z) = 1$ , *if he is given trap-door  $tk$*  (weak extractability).
- Fortunately, several Tag-KEMs including factoring-based one [HK09] has such a special  $\Sigma$  protocol.

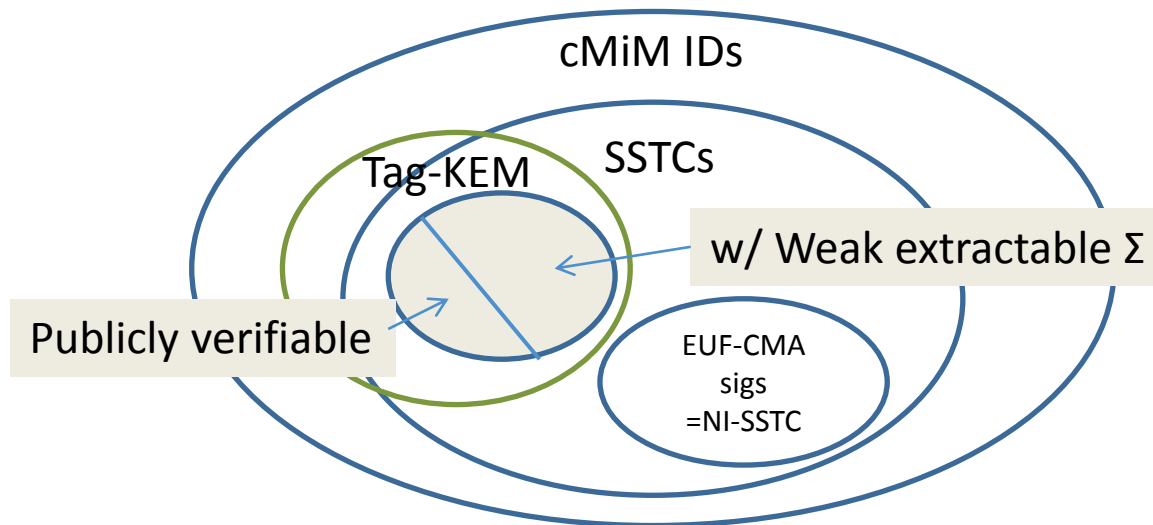


# 5-move SSTC from Tag-KEM w/ **weak extractable $\Sigma$ -protocol**



# To summarize..

- Proposed new frameworks for constructing SSTCs using encryption (Tag-KEM).
- Instantiations
  - 2-move if Tag-KEM is *publicly verifiable*
  - 5-move if Tag-KEM has a *weak extractable  $\Sigma$ -protocol*.



# Comparison

SSTC schemes	Protocol Efficiency	Assumption	Reduction	Type
GMV 03	Efficient	DSA	-----	DSA
MY04/DG 03	Not efficient	sRSA	Tight	Cramer-Shoup sig.
Gen04	Efficient	qSDH	Tight	BB short sig.
DSW08	Efficient but long crs.	CDH	Loose	Waters sig.
NFT10	Inefficient	RSA	Loose	HW sig.
This work (2-move)	Efficient	CDH	Tight	Kiltz's Tag-KEM
This work (5-move)	Efficient	Factoring	Tight	HKTag-KEM



# Thank you..

